

# Introduction to cosmology

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# Outline

- **The smooth expanding Universe** [5x3h NR]
  - General Introduction – FRLW metric – Redshift and distances – Friedmann equations – classical universe models – (neo)classical cosmological tests.
- **CMB Basics - Structure formation in the Universe** [4x3h JR]
  - CMB – structure formation : spherical collapse - linear theory - sound waves
- **Thermal history of the Universe** [2x3h NR]
  - Equilibrium distributions - Boltzmann equation - decoupling – relic densities - primordial nucleosynthesis - recombination - reionization
- **Inflation - modified gravity** [2x3h DS]
  - Motivation for inflation - inflationary phase vs. late time acceleration - realisations of inflation - attractor solutions - primordial scalar and tensor power spectra - different models of modified gravity (massive gravity, galileons...)

# Textbooks

- S. Serjeant, *Observational Cosmology*, Cambridge University Press, 2010.
- S. Dodelson, *Modern Cosmology*, Academic Press, 2003.
- J. A. Peacock, *Cosmological Physics*, Cambridge University Press, 1998.
- J. Rich, *Fundamentals of cosmology*, Springer, 2010.
- B. Ryden, *Introduction to cosmology*, Addison-Wesley, 2002,
- M. P. Hobson, G. P. Efstathiou, and A. N. Lasenby, *General Relativity*, Cambridge University Press (look at the chapters on FLRW metric and cosmology)

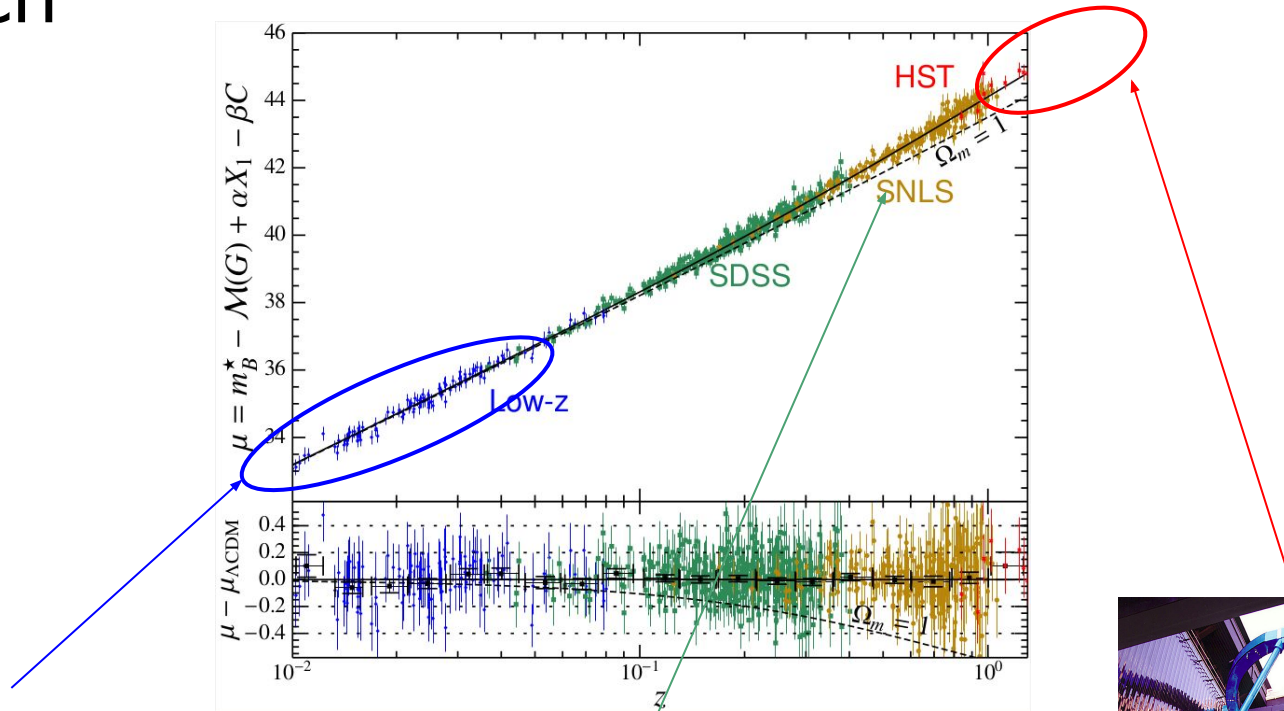
Nicolas Regnault

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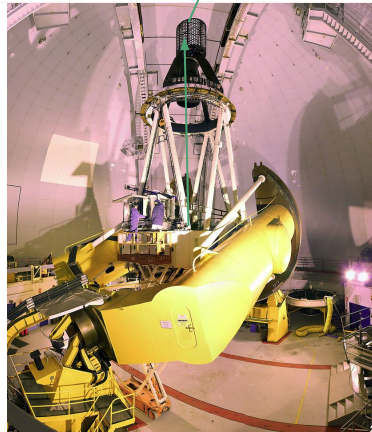
- **LPNHE** (Jussieu campus)
  - Barre 12-22 1st floor
- **LPNHE cosmology group**
  - SN Ia cosmology (LSST, Subaru...)
  - Baryon acoustic oscillations (BOSS, eBOSS, DESI)
  - Weak lensing (LSST)
  - Instrumentation (sensor studies...)

# Research

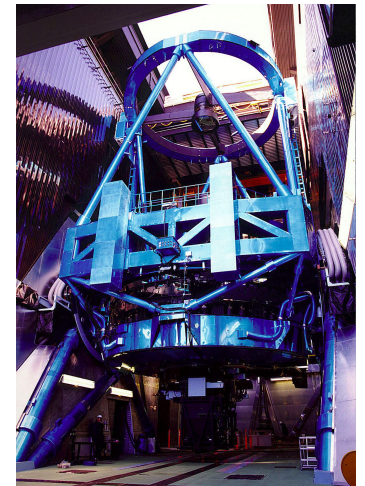
## Hubble diagram of supernovae (Expansion history of the Universe)



ZTF @ Palomar



MegaCam @ CFHT



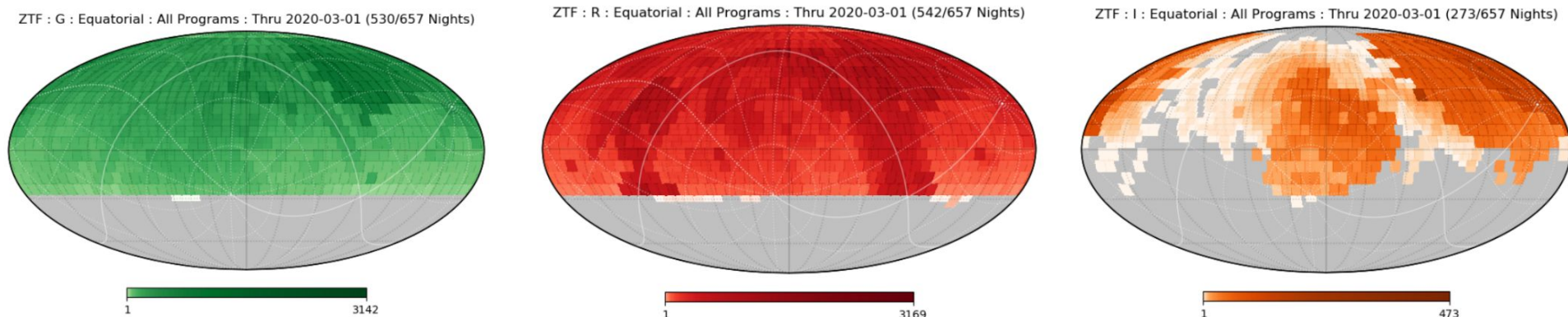
Subaru

# ZTF | Fast (30s exp.) & Large (full visible sky)



We have about 10<sup>5</sup> events/night ; 10% of LSST

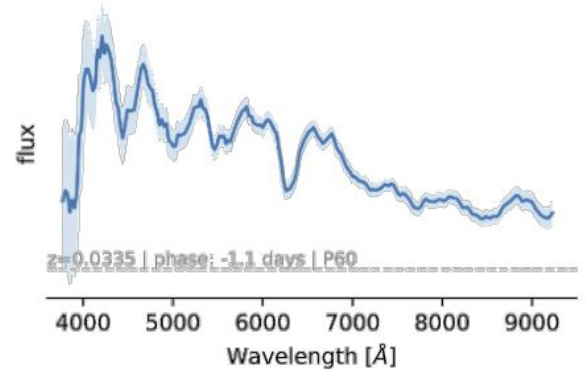
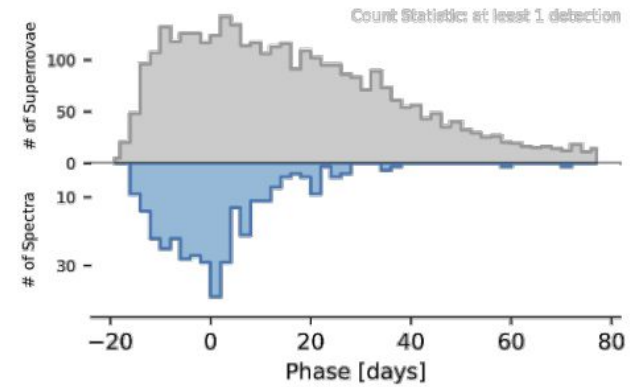
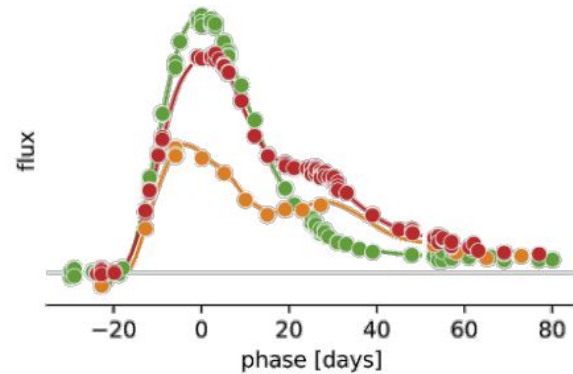
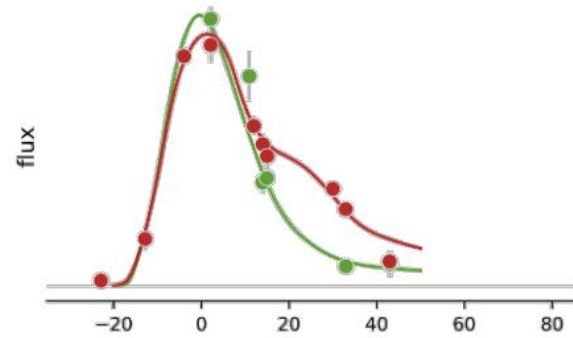
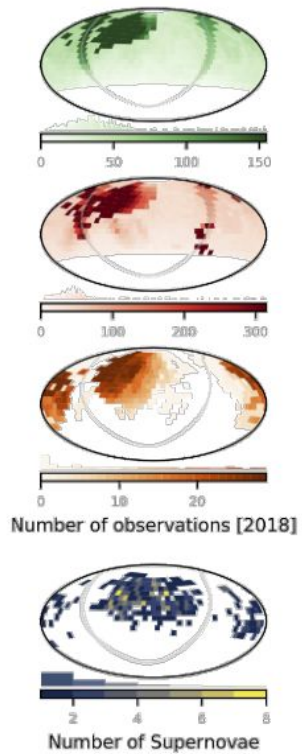
# Survey of the full northern sky



- **3 bands**
  - g,r & I
- **"MSIP" survey**
  - LSST-like survey of northern sky in g & r (2-3 day cadence)
- **Partnership survey**
  - High cadence observations of 10% of the sky (5-6 visits/night)
  - I-band observations of 50% of the sky (~5 day cadence)
- + other partnership programmes (solar system, ToO monitoring of GW events ...)

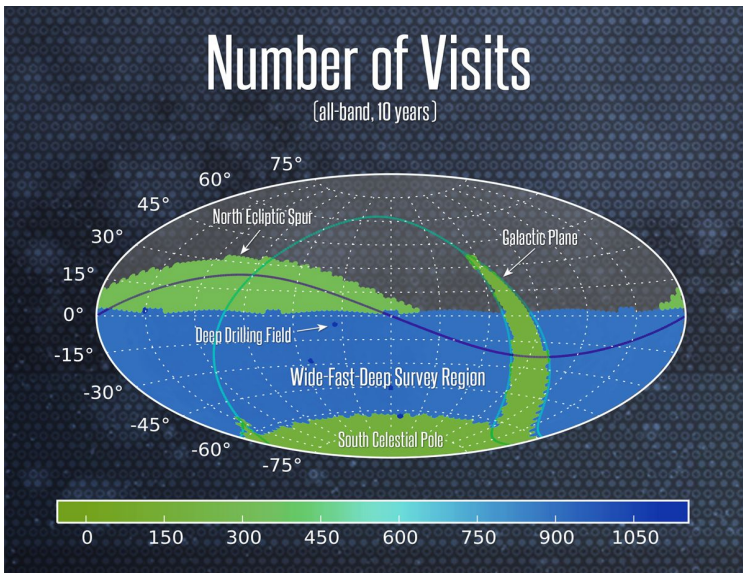
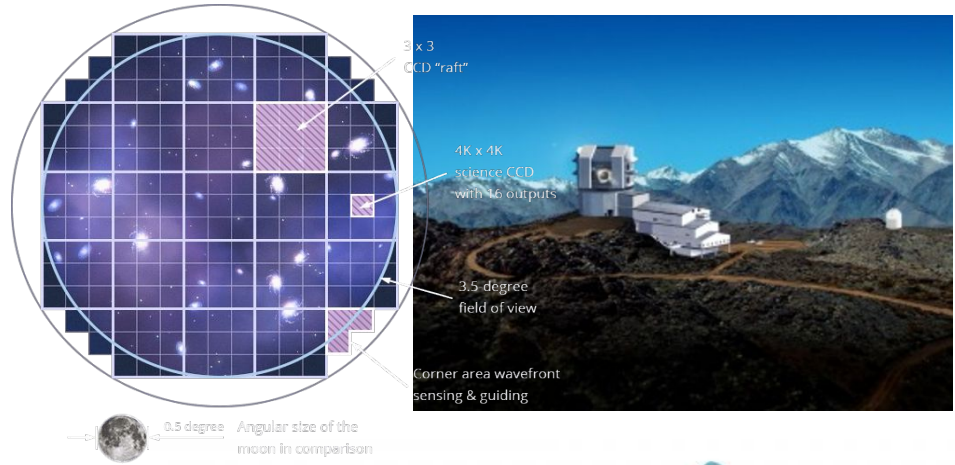


# ZTF DR1 (2019)

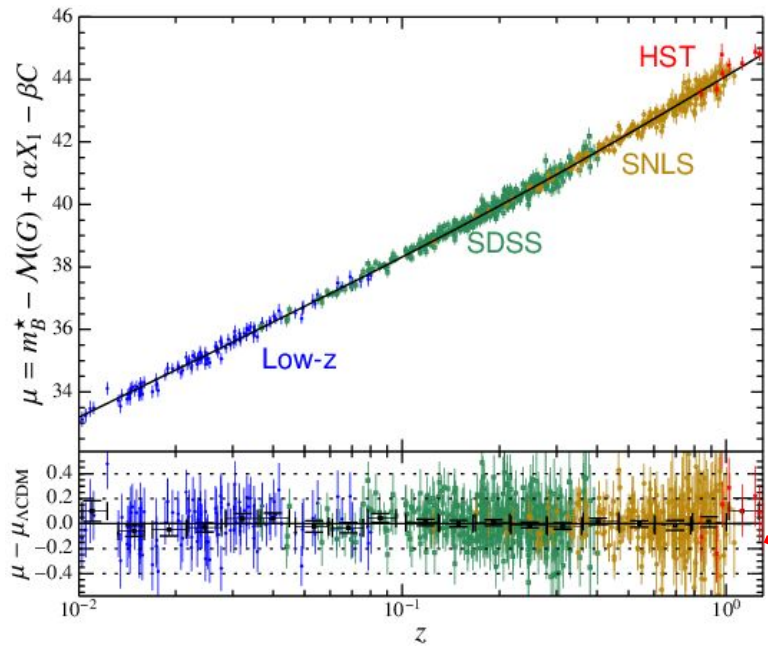


# Research

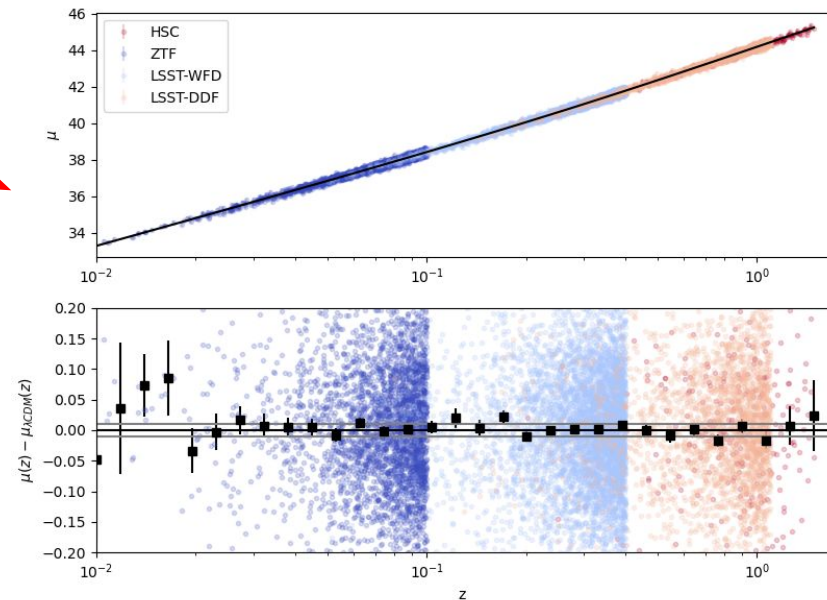
- LSST
- 8.4-m, 9.6 deg<sup>2</sup>
- Chile



# The LSST Era (2024 - ...)



- 2014 : O(1000) SNe (JLA++)
- 2022 : O(5000) SNe
- 2025 : O(10000) SNe



# Outline

- What is cosmology ?
- Cosmology through the ages
- The first revolution (1925) : the Universe is Big !
- The second revolution (1927 - 1931) : the Universe is expanding !
- The hot big-bang model
- Observables
- The third revolution (1999-2003) : accelerated expansion &  $\Lambda$ DCM
- Our strange Universe

# Cosmology ?

- Study of the Universe as a whole
  - Geometry / topology
  - History / age
  - Content (matter, photons, neutrinos, exotic stuff...)
  - Expansion history
  - Thermal history
  - Matter clustering, structure formation
- Messengers photons / gravitons
  - X, UV, visible light, IR, millimetric, radio
- ~~Experimental~~ Observational science
  - We have only one Universe
  - Cannot vary the initial conditions and replay ...



Mihail Minkov

14

APOD 200520



Stars

Milky way

Jupiter

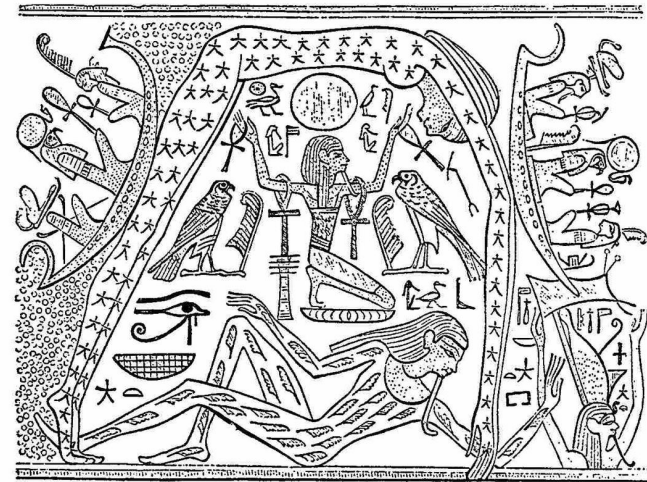
Saturn

Mars

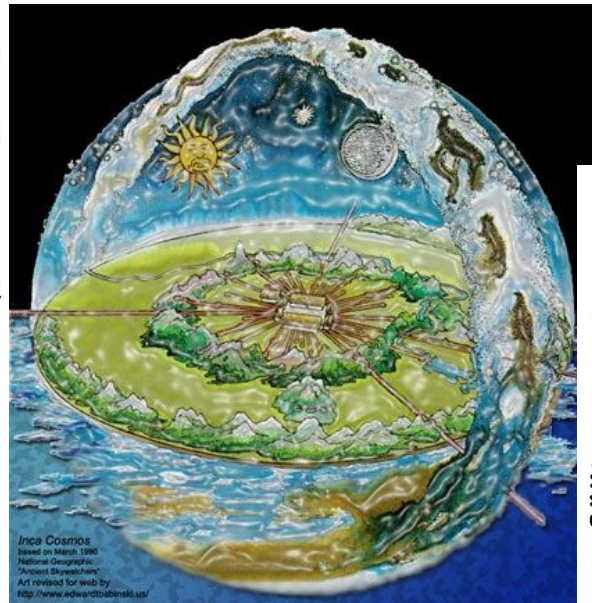
Moon

Mihail Minkov

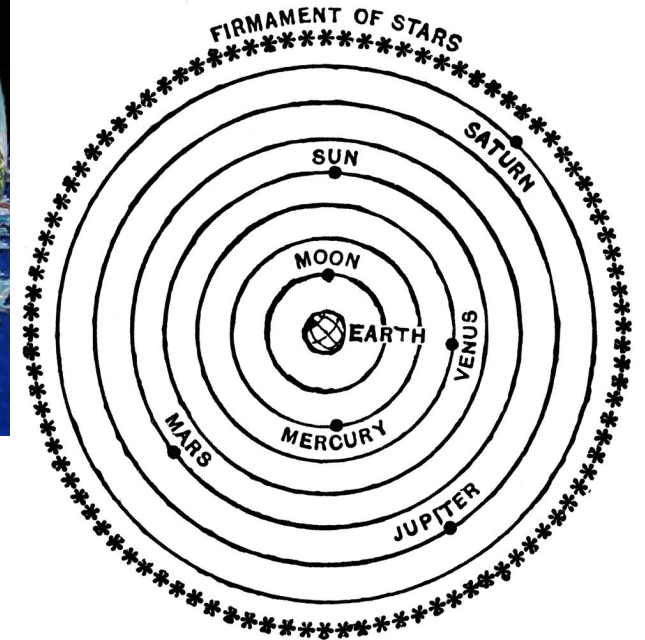
# Past cosmogonies



Egypt



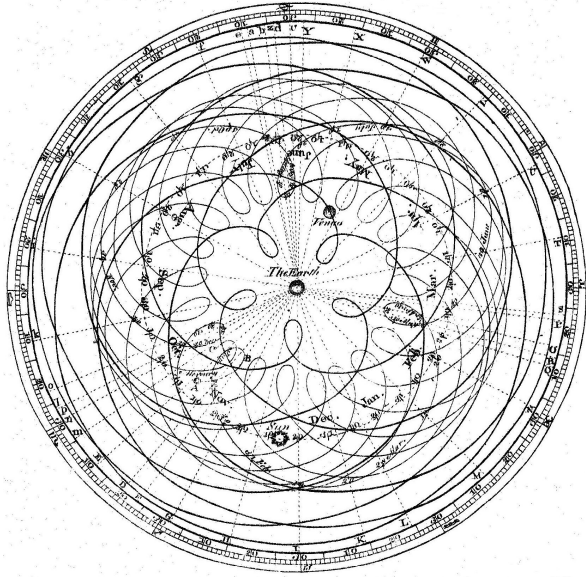
Thales of Miletus  
~ 624 - 547 BC



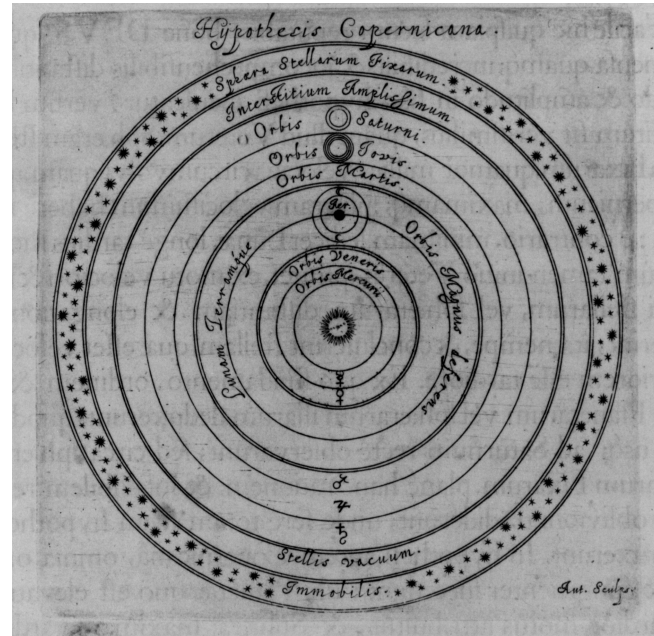
Eudoxus ~ 409 - 356BC  
Hipparchus of Rhodes ~ 190-120 BC



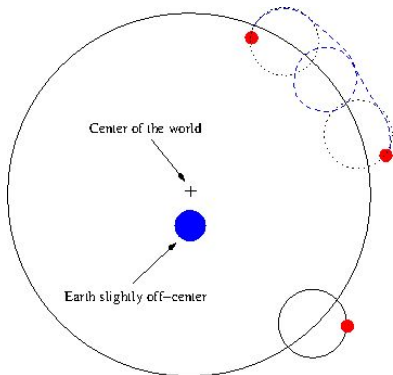
# Motion of planets -> "minor tweaks"



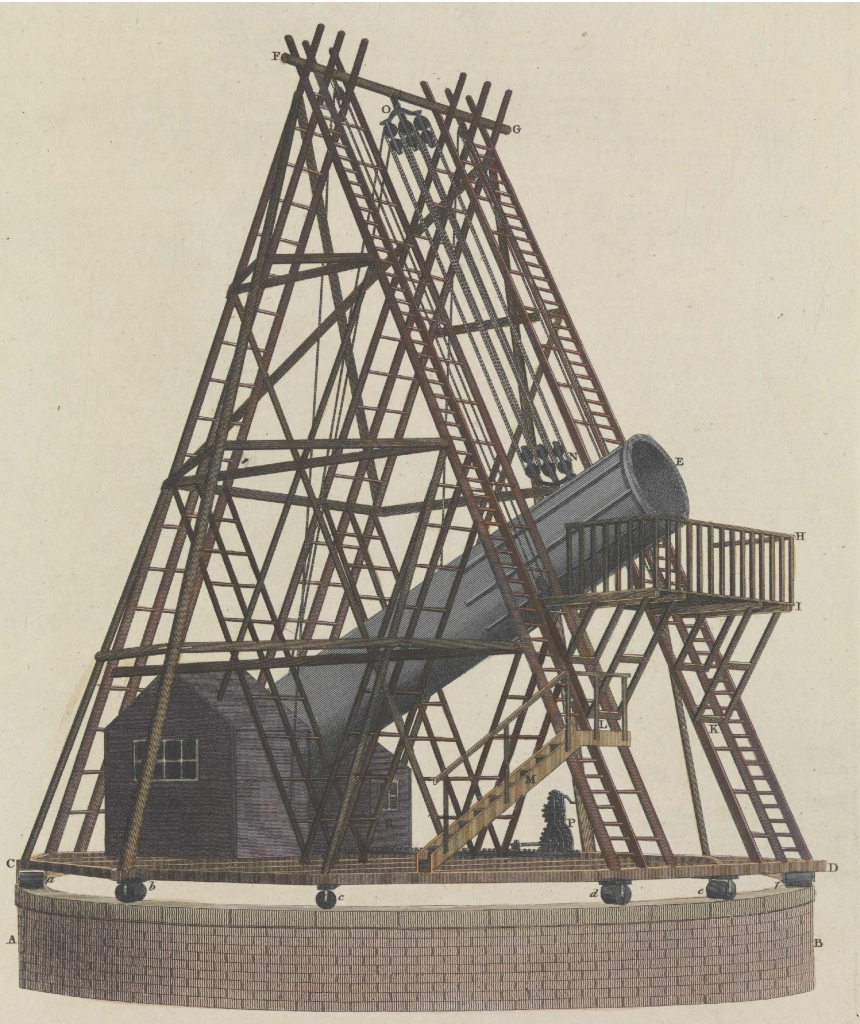
Hipparchus of Rhodes  
Ptolemy (85-165)



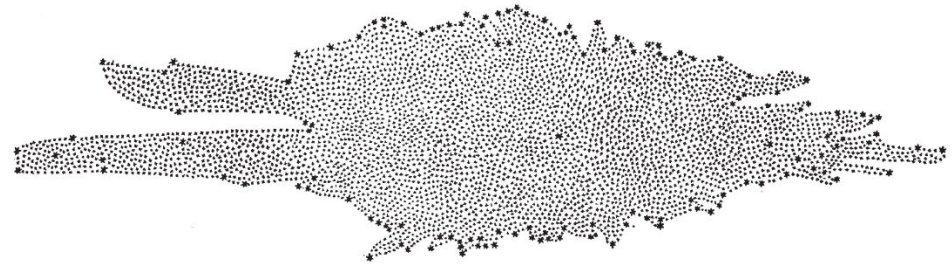
Copernican revolution  
Kepler (elliptical orbits of planets)



# First deep sky surveys

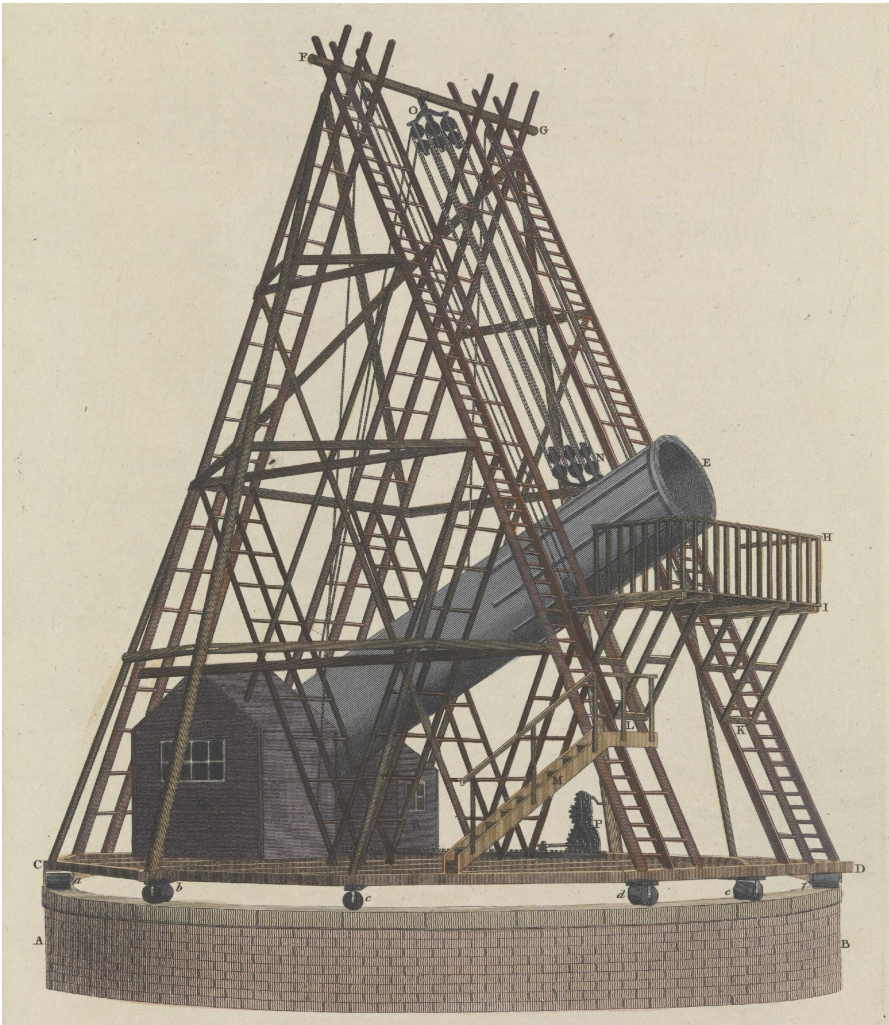


- Herschell (1738 - 1822)
- Discovers more than 2400 "nebulae"
- Star counts reveal anisotropies in star distributions

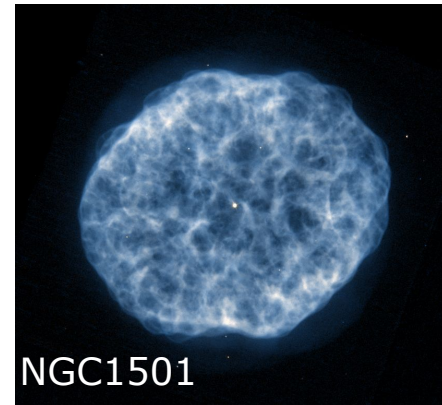


(see 1112.3635)

# First deep sky surveys



Planetary nebulae



NGC1501



Globular clusters

NGC4147

Galaxies



NGC253

The first revolution: the Universe  
is huge !

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M31



MATTEO DUNCHI ©  
21

APOD 150817

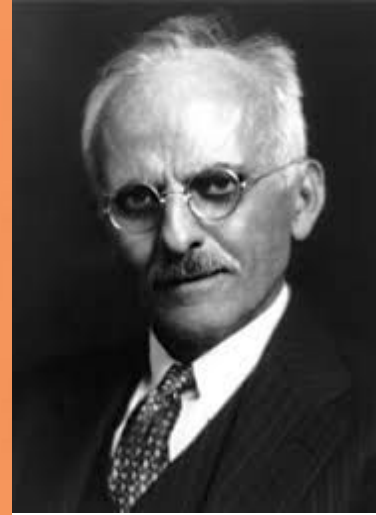
# The scale of the Universe



Harlow  
Shapley

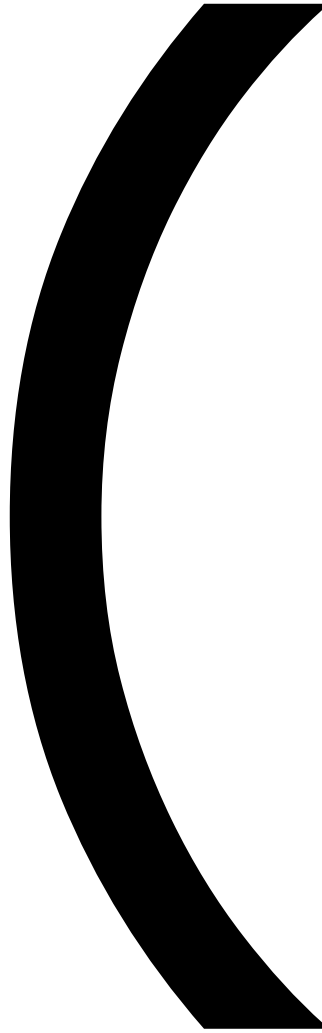
THE SCALE OF THE UNIVERSE  
BY HARLOW SHAPLEY  
Mount Wilson Observatory, Carnegie Institution of Washington  
and  
HEBER D. CURTIS  
Director, Allegheny Observatory

REPRINTED FOR NATURAL SCIENCES 9  
HARVARD UNIVERSITY



Heber D.  
Curtis

I hold, therefore, to the belief that the galaxy is probably not more than 30,000 light-years in diameter; that the spirals are not intra-galactic objects but island universes, like our own galaxy, and that the spirals, as external galaxies, indicate to us a greater universe into which we may penetrate to distances of ten million to a hundred million light-years.

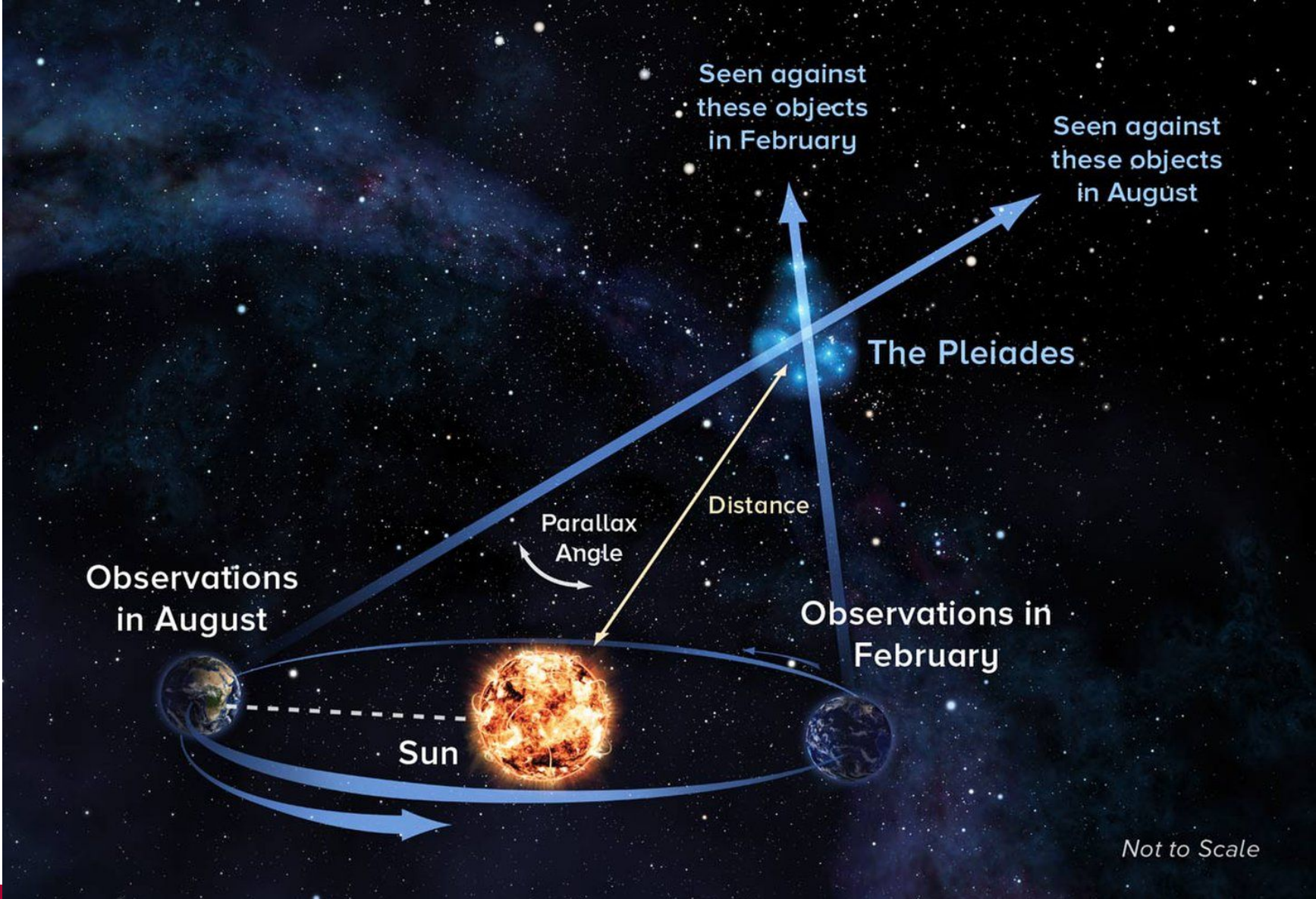


# Measuring distances in the Universe

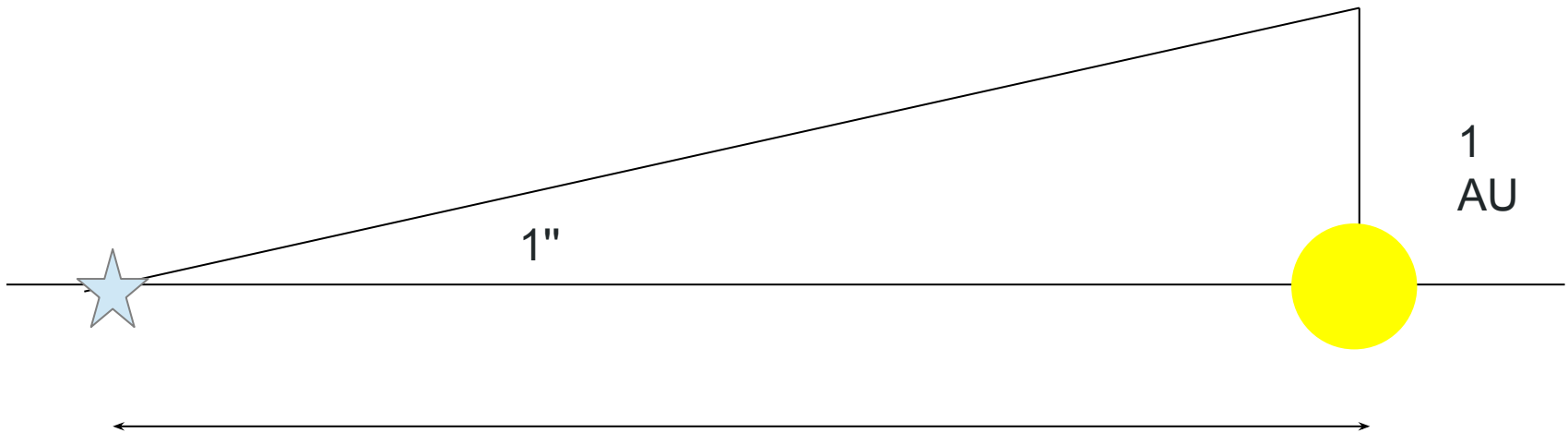




# Parallax



# Parallaxes



1 AU = *average distance earth-sun* = 149 597 870.7 km  
 $\sim 1.5 \cdot 10^{11}$  m

1 pc = ?

# Standard candles

- Objects with a known luminosity

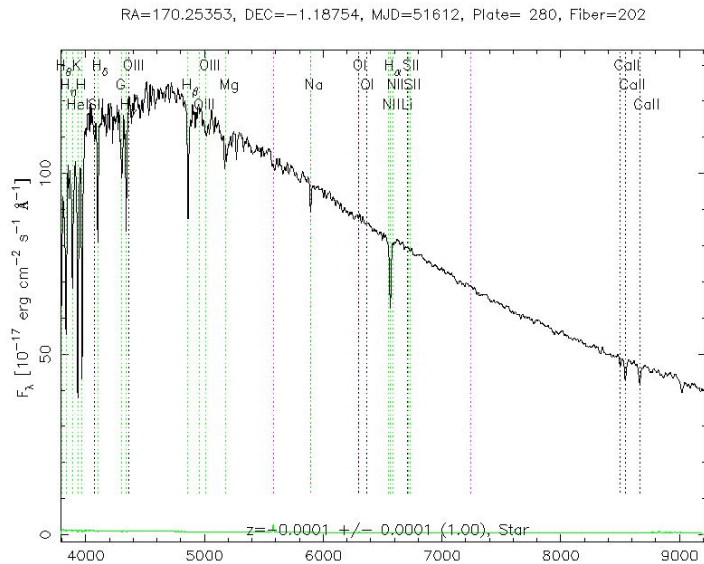
The diagram illustrates the relationship between measured flux, luminosity, and distance. The equation  $f = \frac{\mathcal{L}}{4\pi d_L^2}$  is centered. A green arrow points from the text 'Measured flux' to the variable  $f$ . Another green arrow points from the text 'distance' to the variable  $d_L$  in the denominator. A third green arrow points from the text 'Objects with a known luminosity' (from the list above) to the variable  $\mathcal{L}$  in the numerator.

$$f = \frac{\mathcal{L}}{4\pi d_L^2}$$

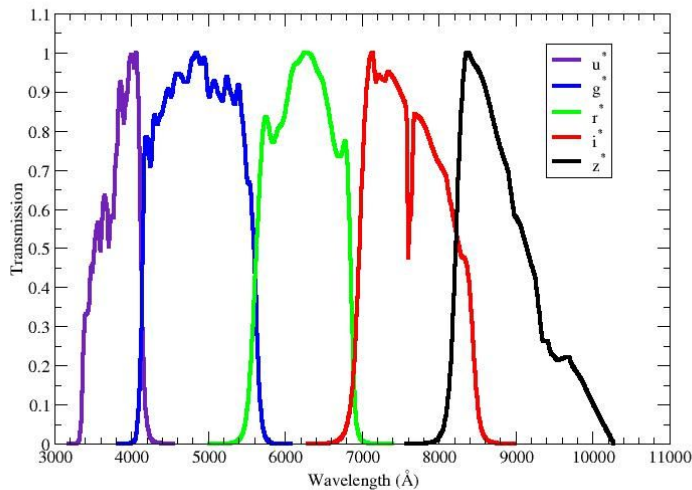
Measured flux

distance

# Stars / stellar photometry



CFHT-Megaprime Filters



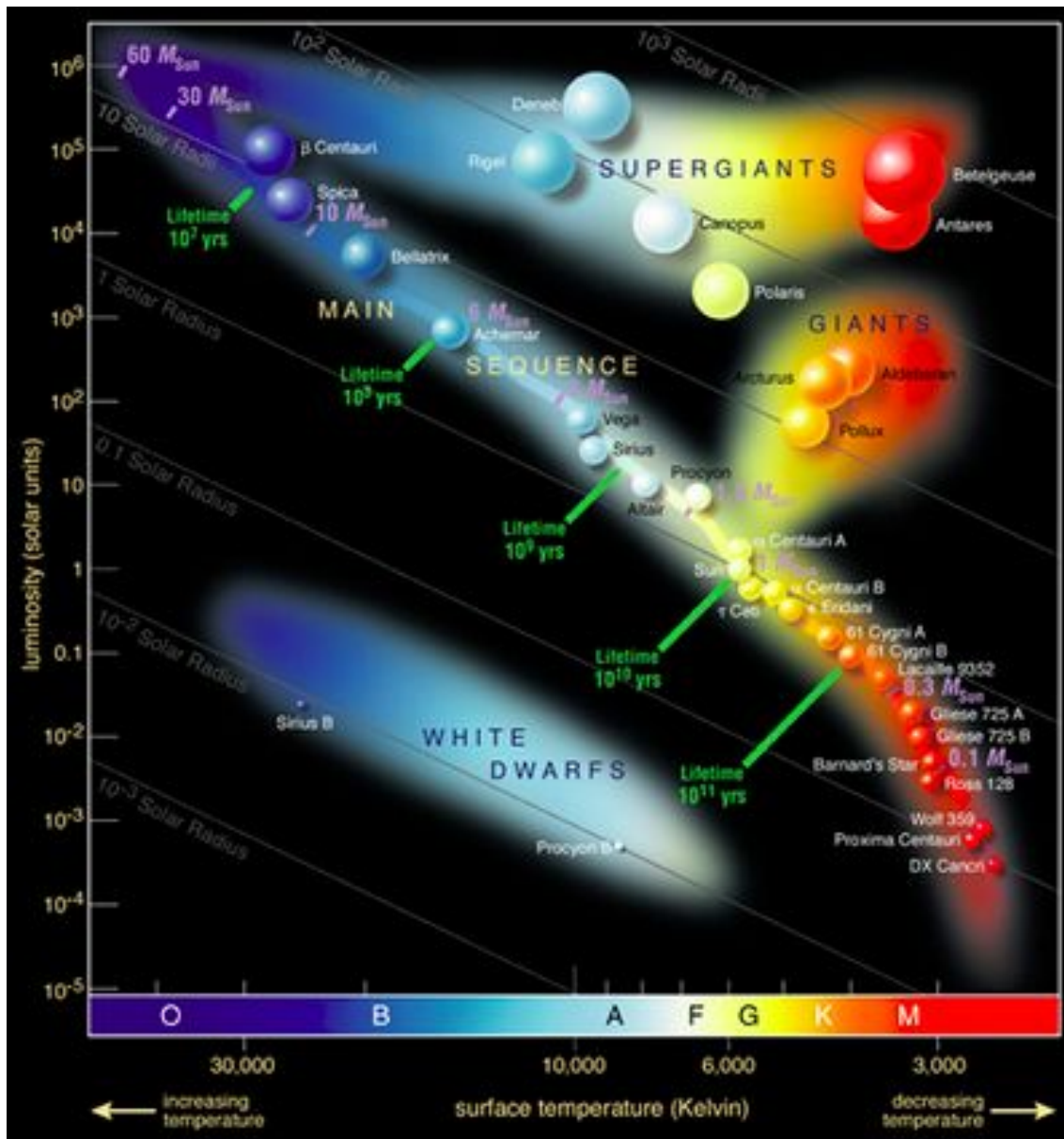
- **Stellar spectrum**
  - Black body
  - Emission / absorption lines
  - Spectral classification
  - OBAFGKM
- **Apparent magnitude**

$$m - m_{\text{ref}} = -2.5 \times \log_{10} \left( \frac{f}{f_{\text{ref}}} \right)$$

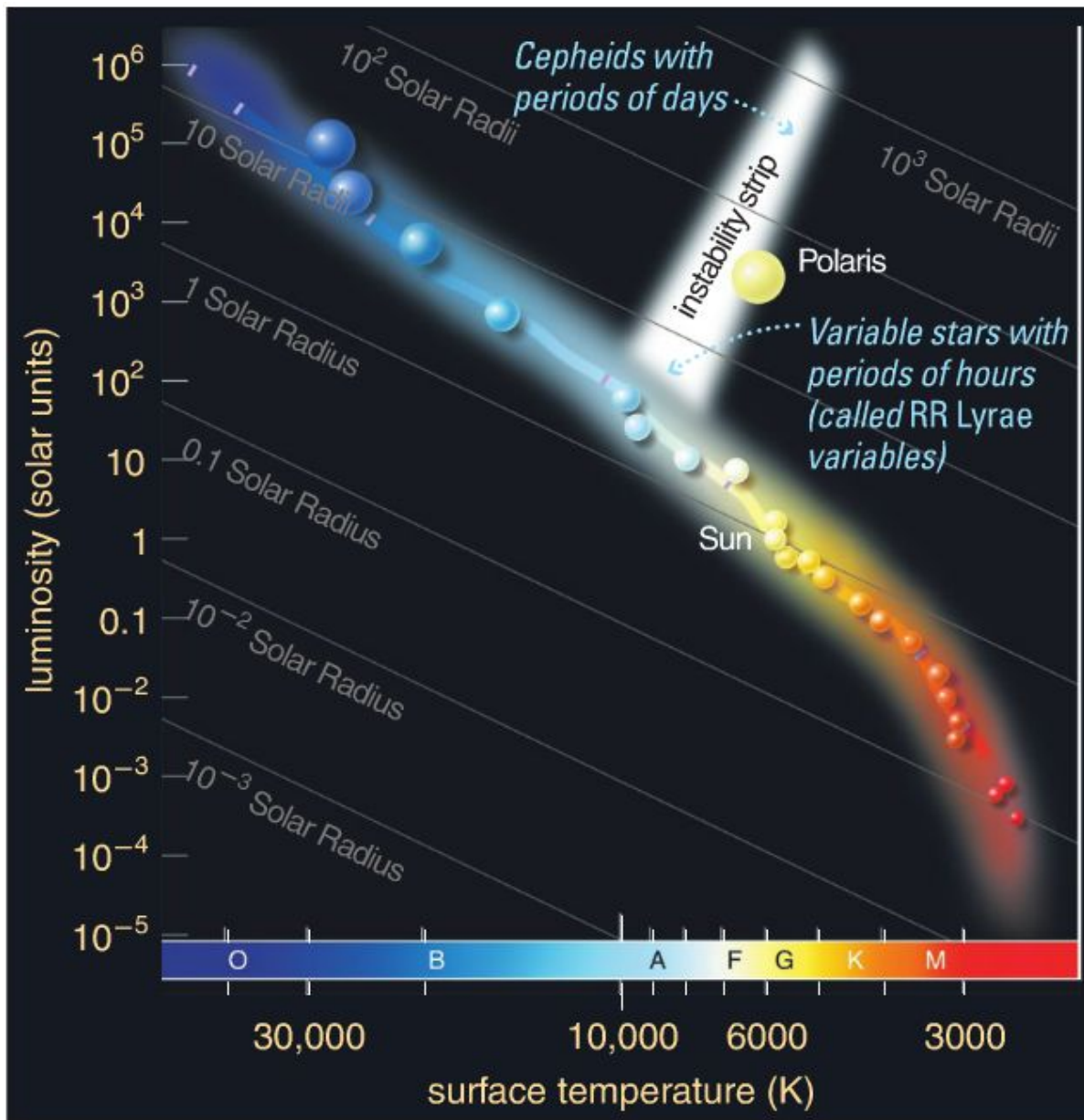
- **Absolute magnitude**
  - Magnitude of the object @ 10pc
- **Distance modulus**

$$\mu = m - M = 5 \log_{10} \left( \frac{d}{10\text{pc}} \right) = 5 \log_{10} d - 5$$

# Absolute luminosity

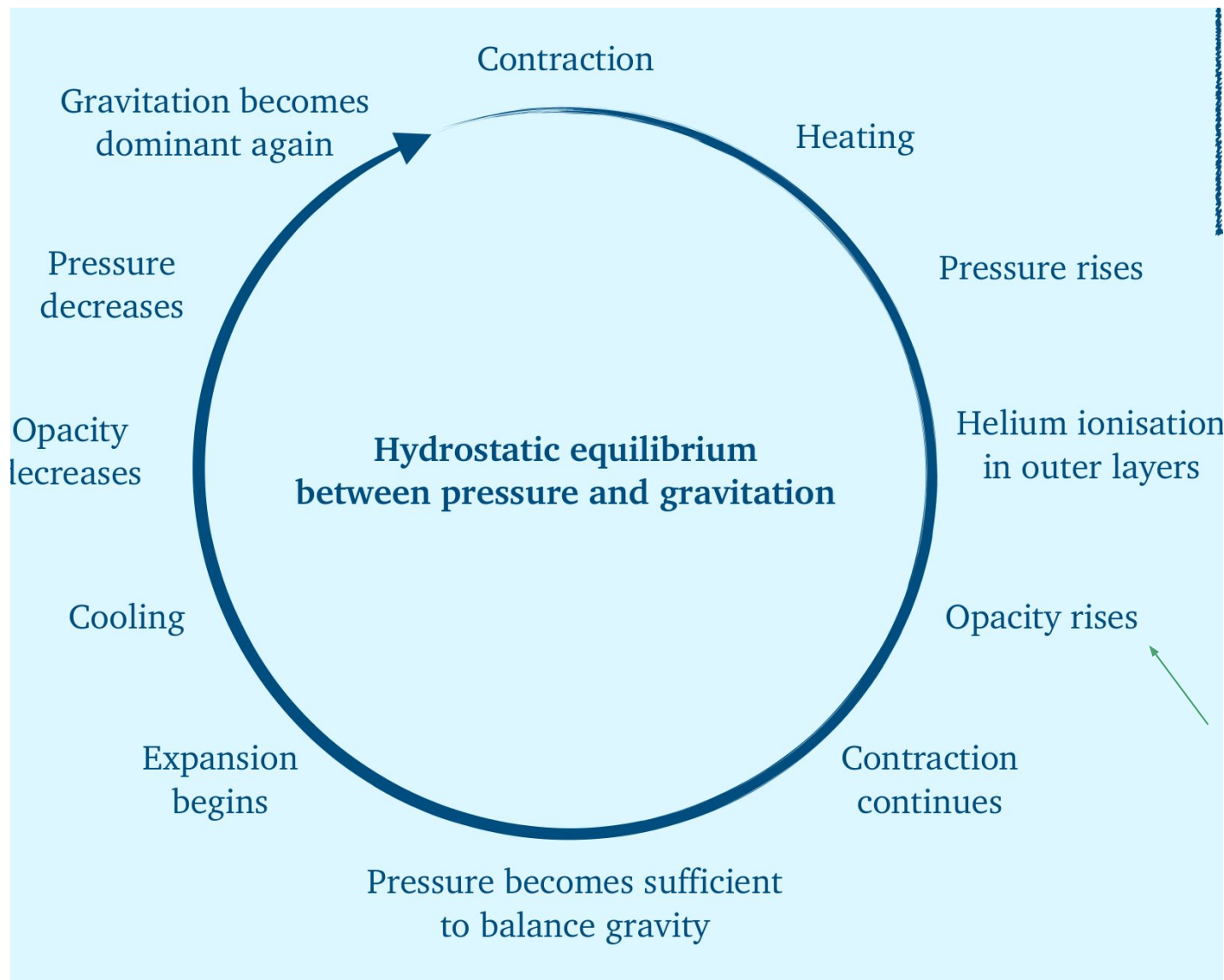


# Color



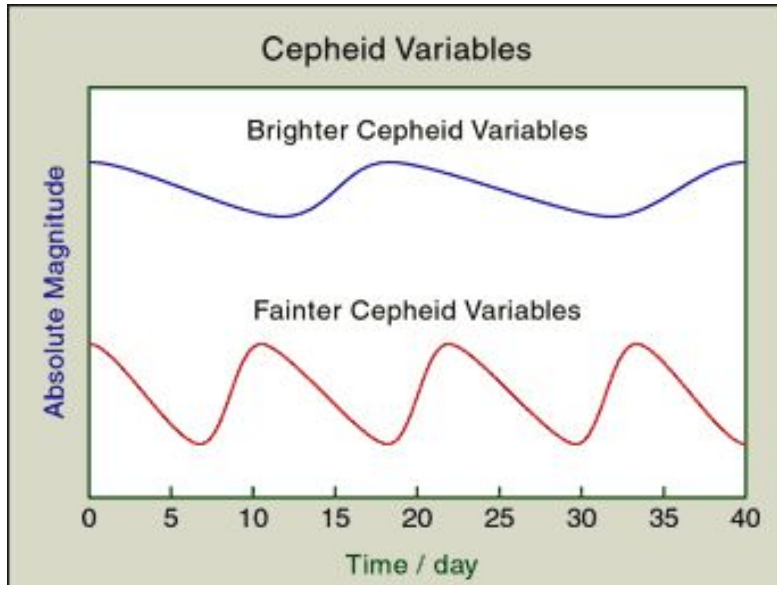
**FIGURE 15.15** An H-R diagram with the instability strip highlighted. Notice that Polaris, the North Star, is a Cepheid variable star.

# Why pulsating ? $\kappa$ -mechanism

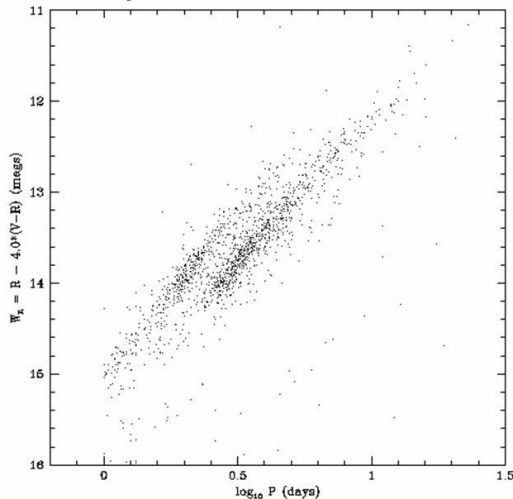


Key thing here. In "normal" stars, opacity decreases with temperature / pressure.

# Pulsating variables



Cepheid P-L Relation



- **Cepheids**
  - Very bright
  - Pulsating,  $P=1-50$  days
  - Rare
  - Distances up to 30 Mpc
- **RR-Lyrae**
  - Pulsating variables
  - $P \sim 0.1 - 1$  days
  - Galaxy / local group



# Henrietta Leavitt

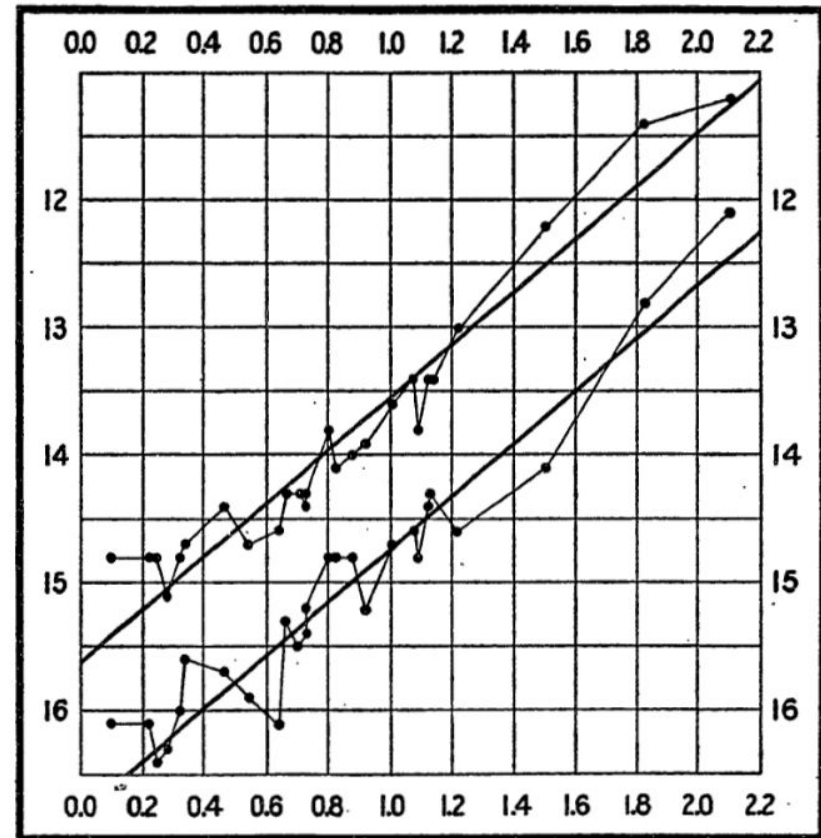


FIG. 2.

Leavitt's PL relation

# Measuring distances with Cepheids

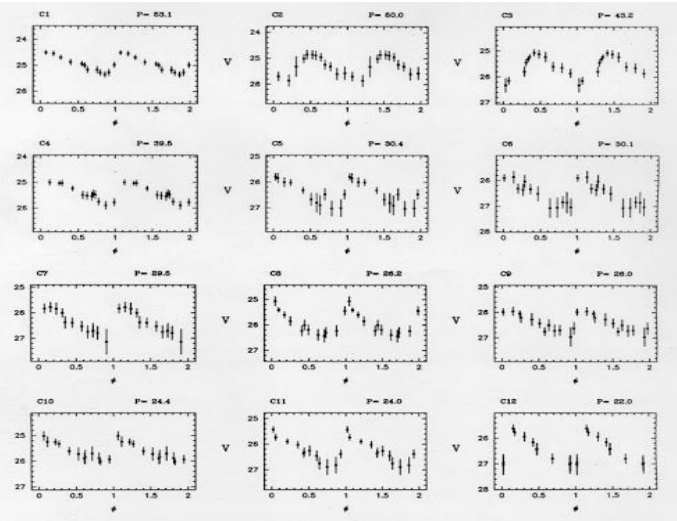
$$m - M = 5 \log_{10} d_{pc} - 5$$

Measure the  
apparent  
magnitude from  
the light curve

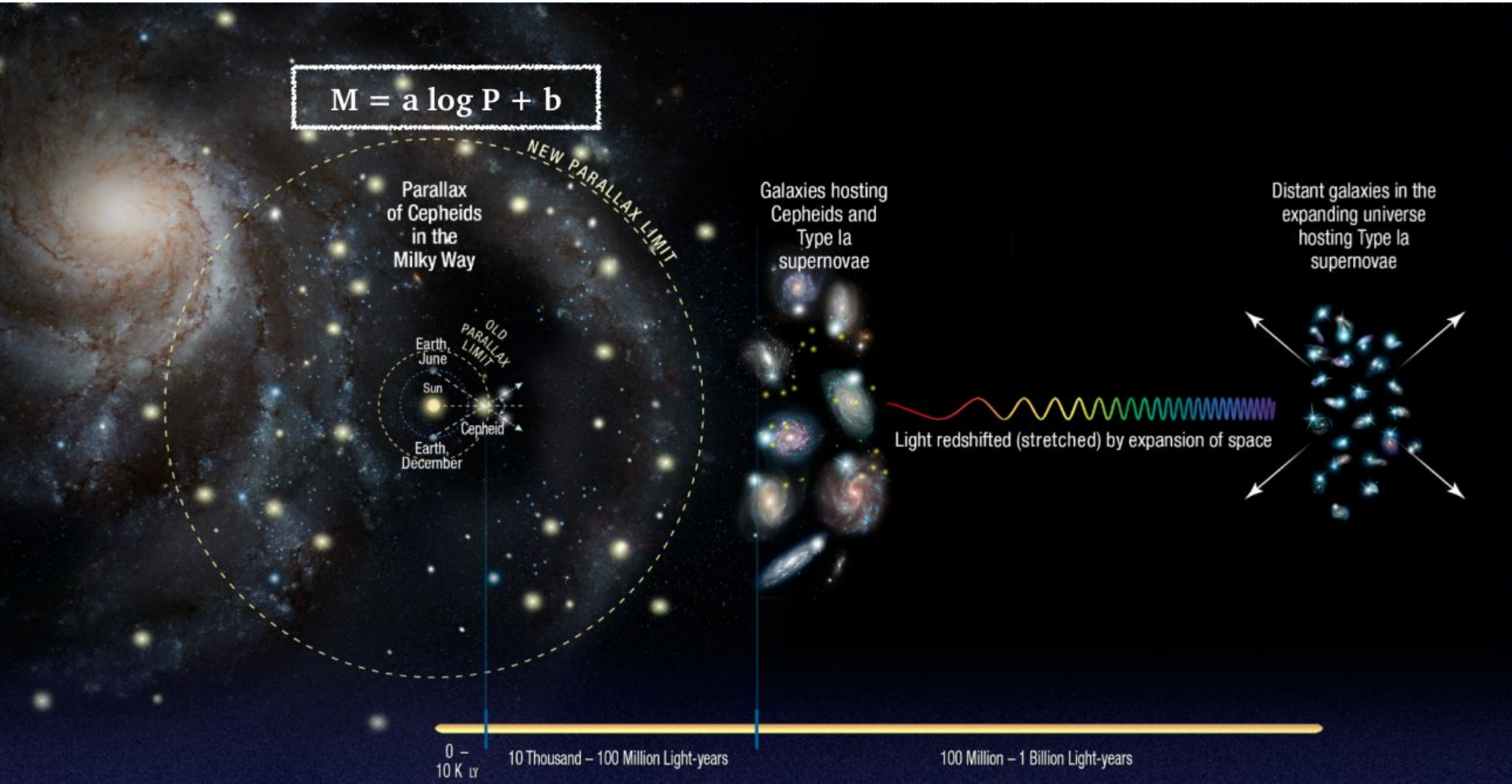
Infer absolute  
magnitude from  
measurement of  
cepheid period, and  
PL relation

$$M = a \log P + b$$

Q: how do we  
calibrate the PL  
relation ?



# Measuring distances with Cepheids



# Distance to M31

## CEPHEIDS IN SPIRAL NEBULAE.

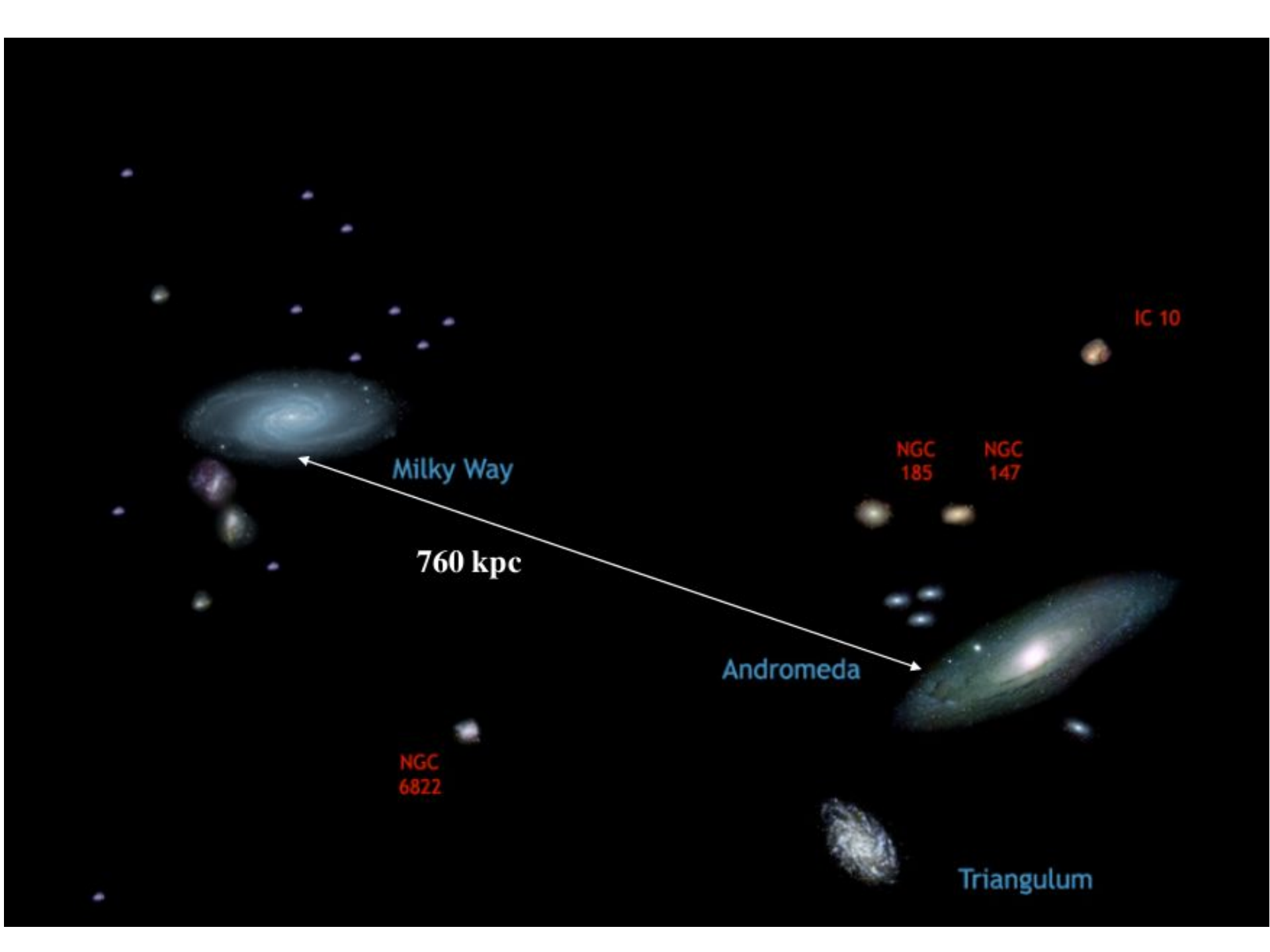
BY EDWIN P. HUBBLE.

Messier 31 and 33, the only spirals that can be seen with the naked eye, have recently been made the subject of detailed investigations with the 100-inch and 60-inch reflectors of the Mount Wilson Observatory.

—21.8 and —21.9 for M 31 and M 33, respectively. These must be corrected by half the average ranges of the Cepheids in the two spirals, and the final values are then on the order of —22.3 for both nebulae.

The corresponding distance is about 285,000 parsecs. The greatest uncertainty is probably in the zero point of Shapley's curve.

This estimate was wrong, by a factor  $\sim 2.5$   
But shows that M31 is well outside Milky Way



Milky Way

760 kpc

Andromeda

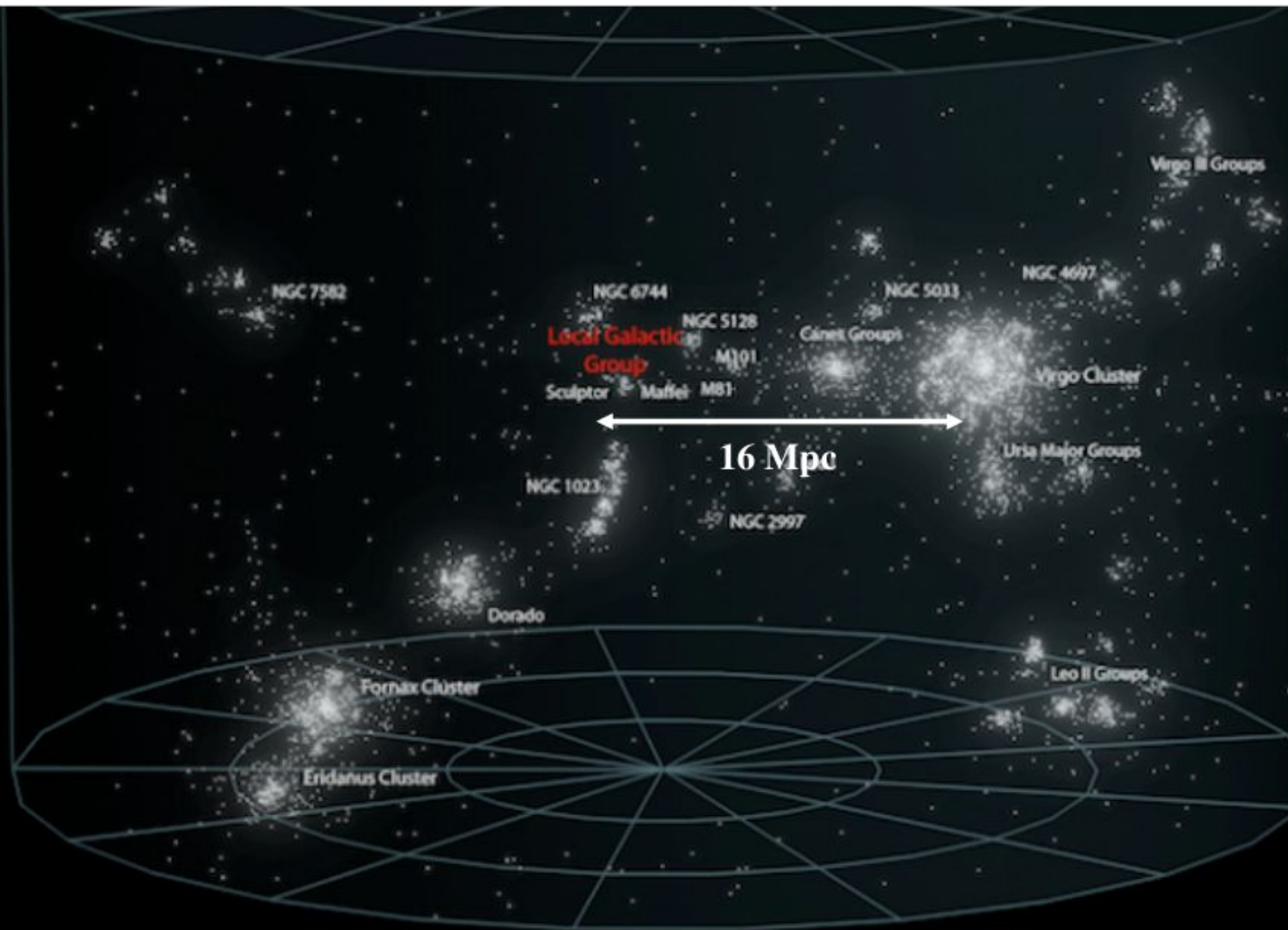
Triangulum

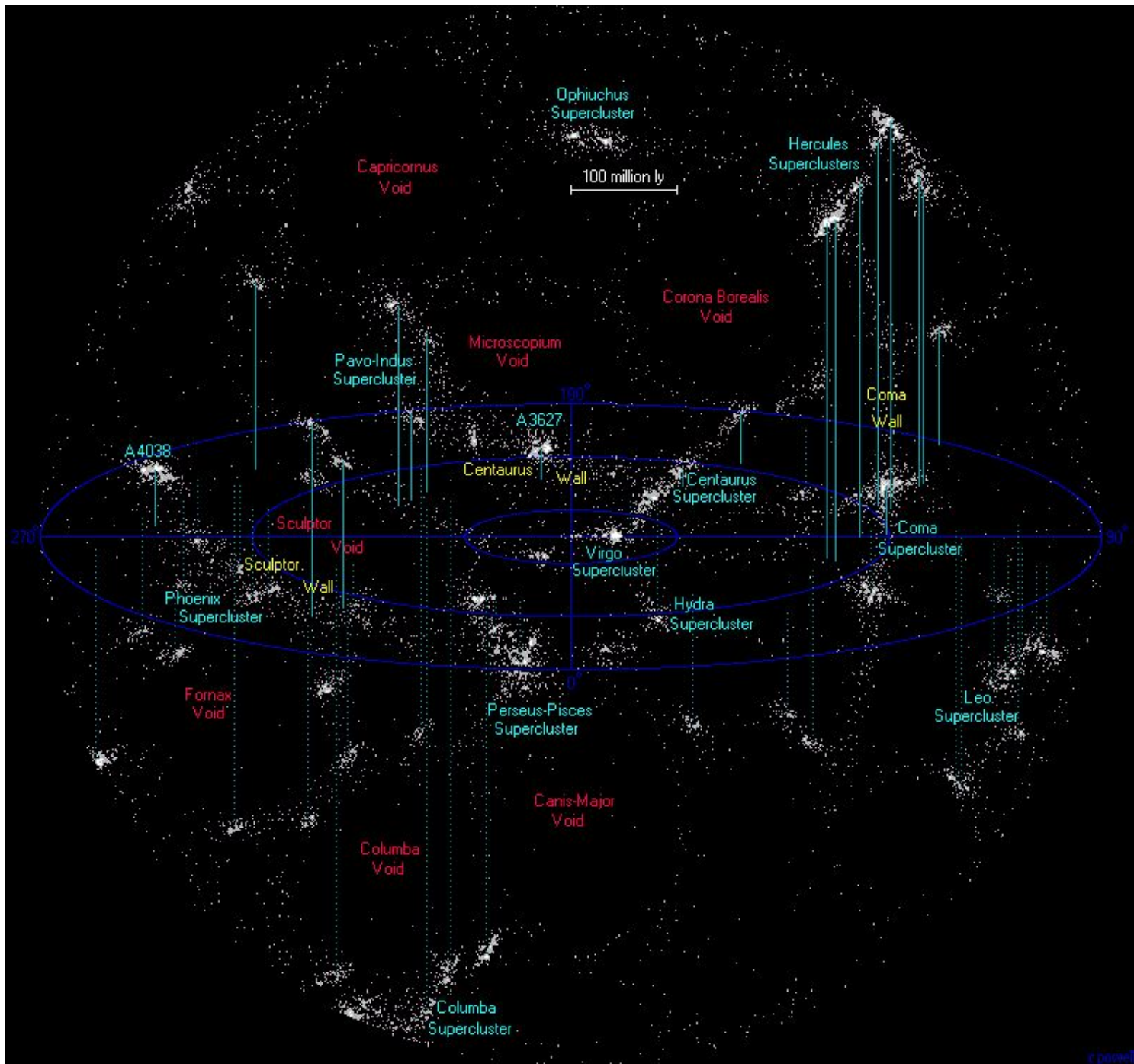
NGC  
185

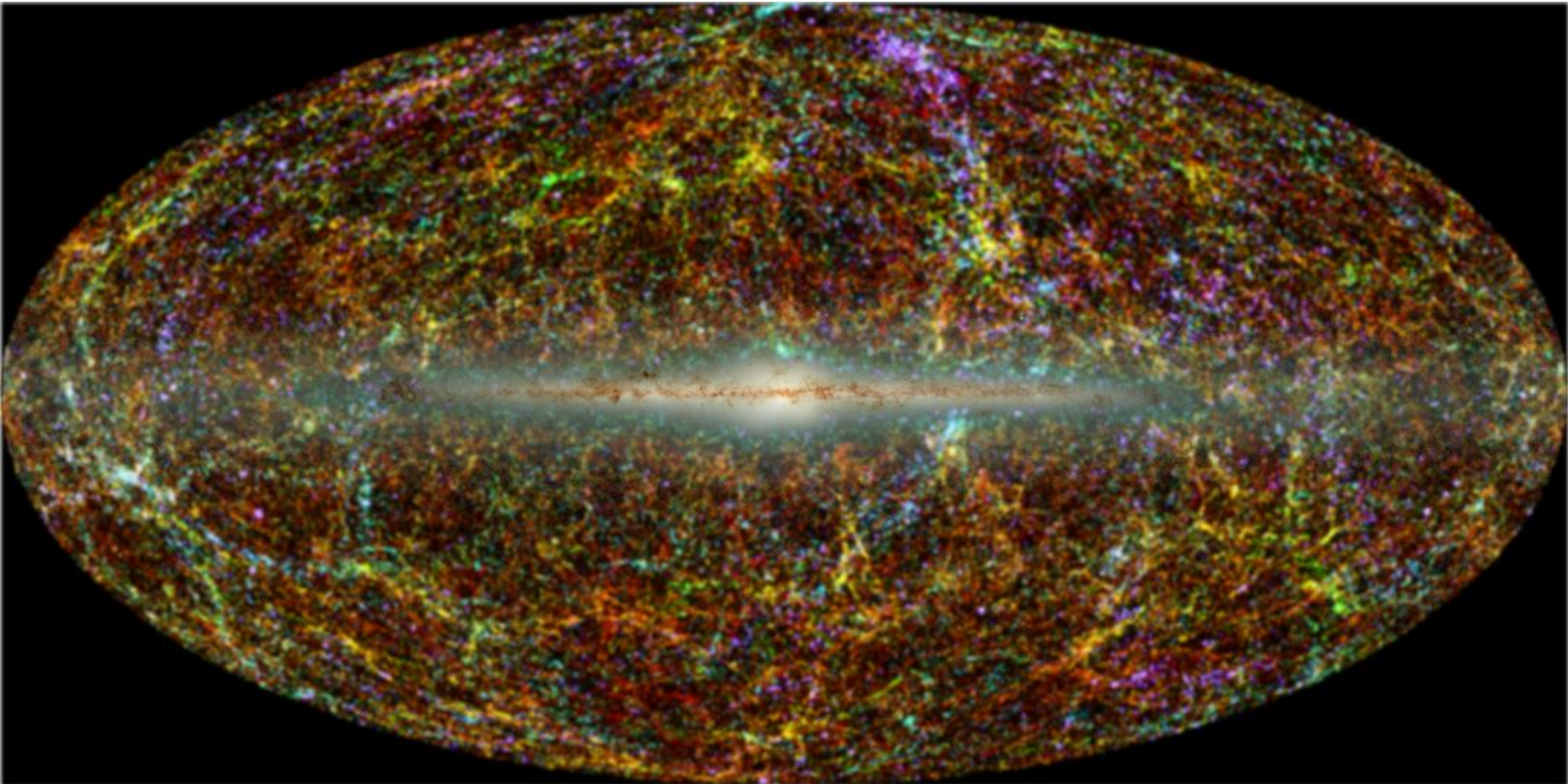
NGC  
147

NGC  
6822

IC 10







2MASS redshift survey



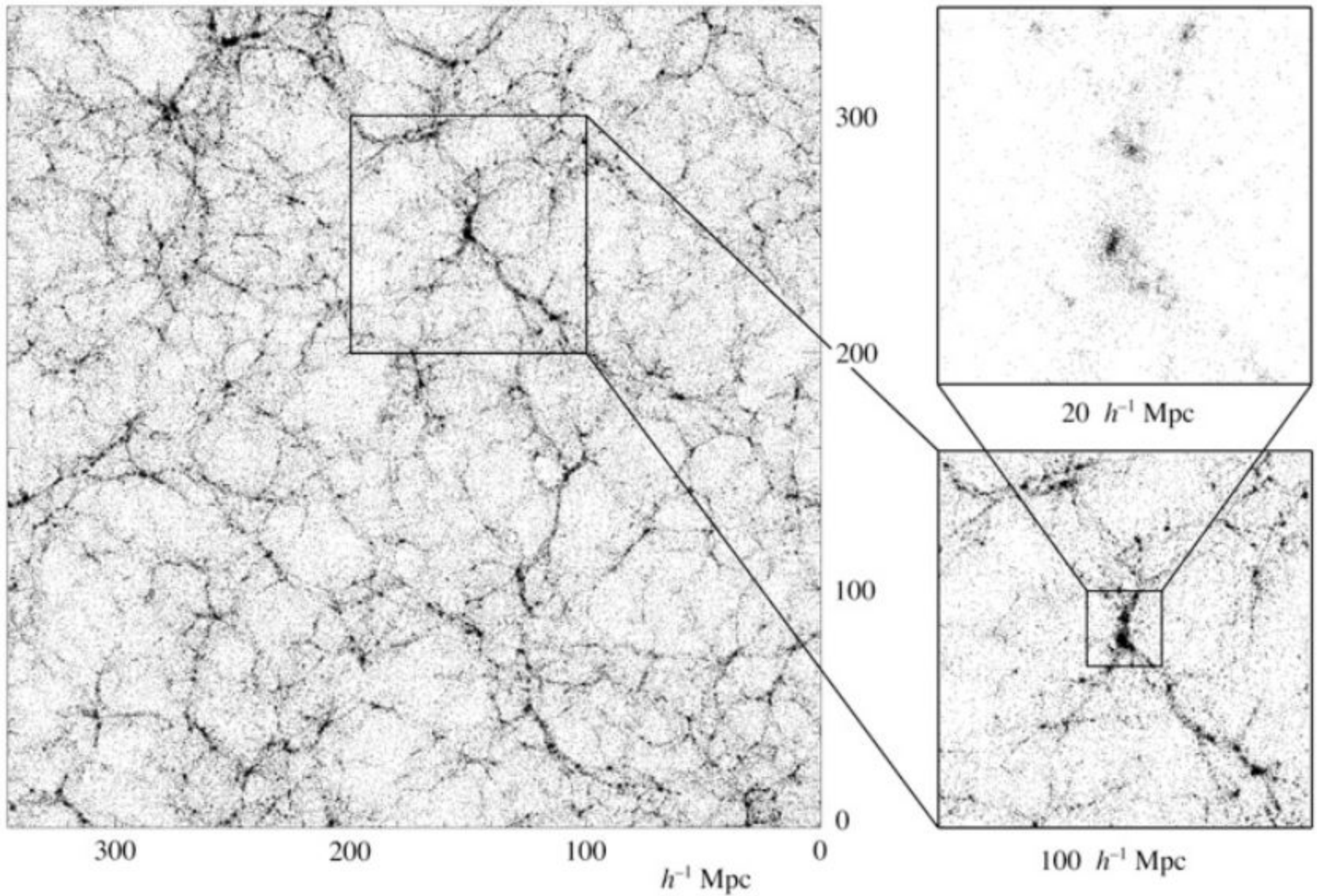


Fig 8.16 (D. Weinberg) 'Galaxies in the Universe' Sparke/Gallagher CUP 2007

The second revolution: the  
Universe is expanding !

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# Expansion

- Slipher (1915) notes that most "nebulae" are red-shifted ( $\Rightarrow$  receding from us)



## SPECTROGRAPHIC OBSERVATIONS OF NEBULAE.

BY V. M. SLIPHER.

During the last two years the spectrographic work at Flagstaff has been devoted largely to nebulae. While the observations were chiefly concerned with the spiral nebulae they also include planetary and extended nebulae and globular star clusters.

• By 1924 :

- 41 measured
- 36 receding

N.G.C.	Velocity
221	- 300 km
224 †	- 300
598	-
1023	+ 200 roughly
1068	+ 1100
7331	+ 300 roughly
3031	+ small
3115	+ 400 roughly
3627	+ 500
4565	+ 1000
4594	+ 1100
4736	+ 200 roughly
4826	+ small
5194	± small
5866	+ 600

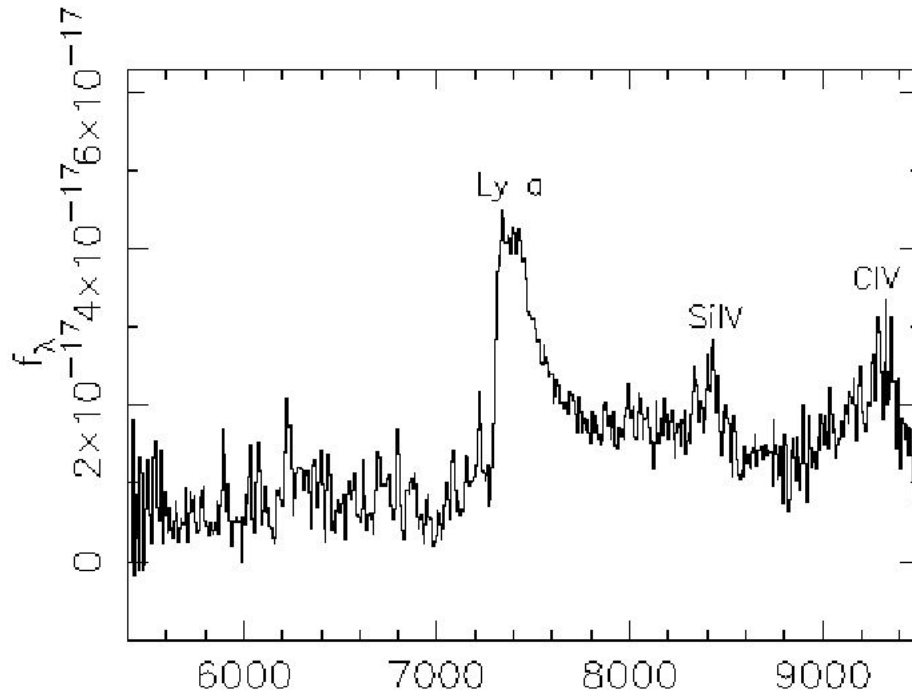
From the 1915 paper

These nebulae are on the south side of the Milky Way.

These are on the north side of the Milky Way

# Redshift

$$1 + z = \frac{\lambda_{\text{observed}}}{\lambda_{\text{emitted}}} \approx \sqrt{\frac{1 + \beta}{1 - \beta}} \approx 1 + \beta$$



- Ly- $\alpha$  :  $\lambda = 1216 \text{ \AA}$
- Ly- $\alpha$  :  $\lambda_{\text{obs}} = 7400 \text{ \AA}$
- $z = ?$

# The Universe is expanding (!)



- 49 -

UN UNIVERS HOMOGENE DE MASSE CONSTANTE ET DE RAYON CROISSANT,  
RENDANT COMPTE  
DE LA VITESSE RADIALE DES NÉBULEUSES EXTRA-GALACTIQUES

Note de M. l'Abbé G. LEMAITRE

1. GÉNÉRALITÉS.

La théorie de la relativité fait prévoir l'existence d'un univers homogène où non seulement la répartition de la matière est uniforme, mais où toutes les positions de l'espace sont équivalentes, il n'y a pas de centre de gravité. Le rayon  $R$  de l'espace est constant, l'espace est elliptique de courbure positive uniforme  $1/R^2$ , les droites issues d'un même point repassent à leur point de départ après un parcours égal à  $\pi R$ , le volume total de l'espace est fini et égal à  $\pi^2 R^3$ , les droites sont des lignes fermées parcourant tout l'espace sans rencontrer de frontière (<sup>1</sup>).

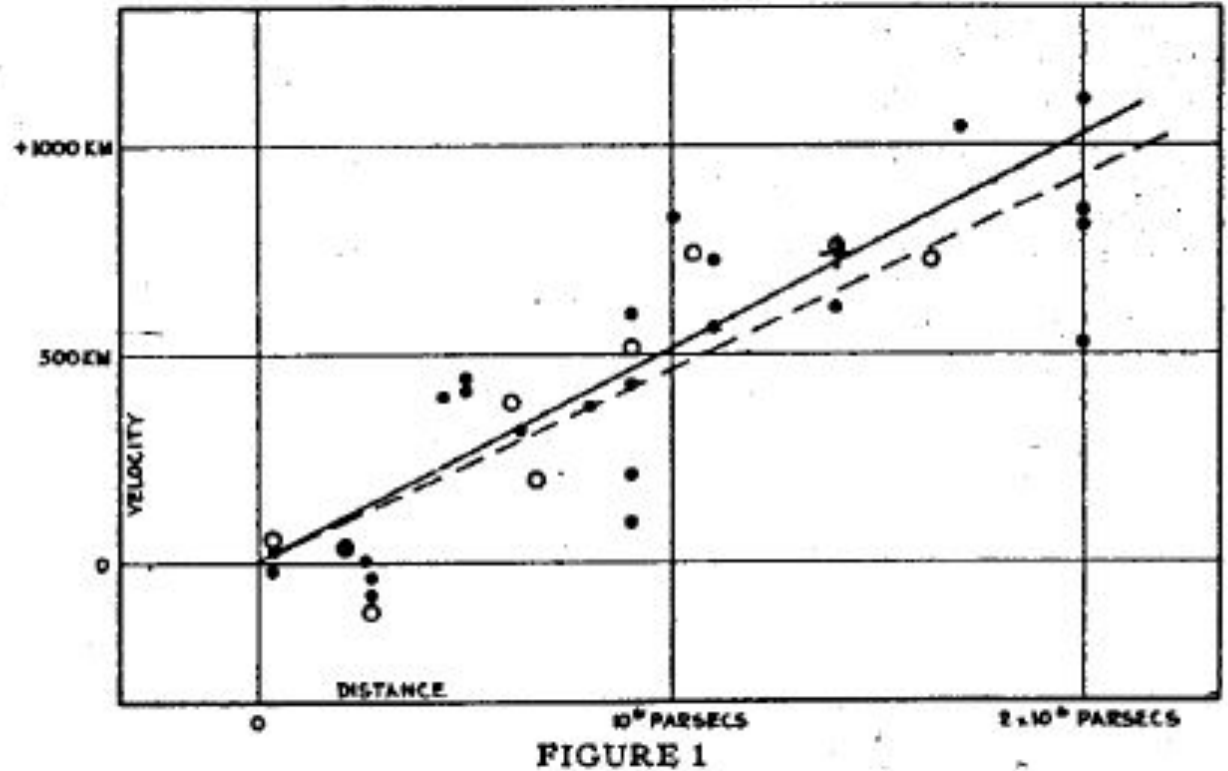
Uses Slipher's measurements

Find  $v = H \times d$  with  $H \sim 575 \text{ km/s/Mpc}$

Lemaitre, 1927

Annales de la société scientifique de Bruxelles<sub>46</sub>

# The Universe is expanding (!)

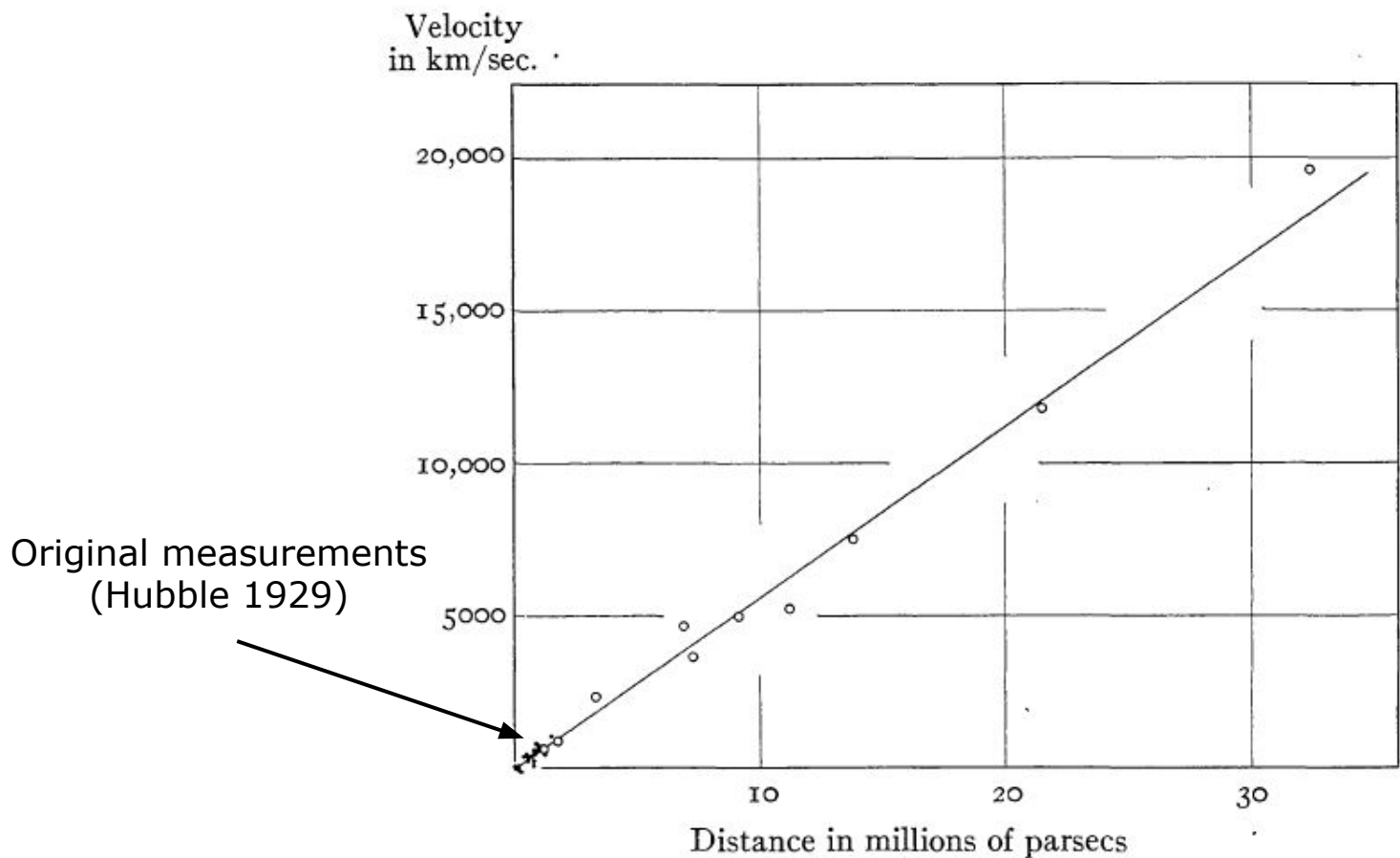


Hubble Law :

$$v = H \times d$$

"Hubble constant" [km/s/Mpc]

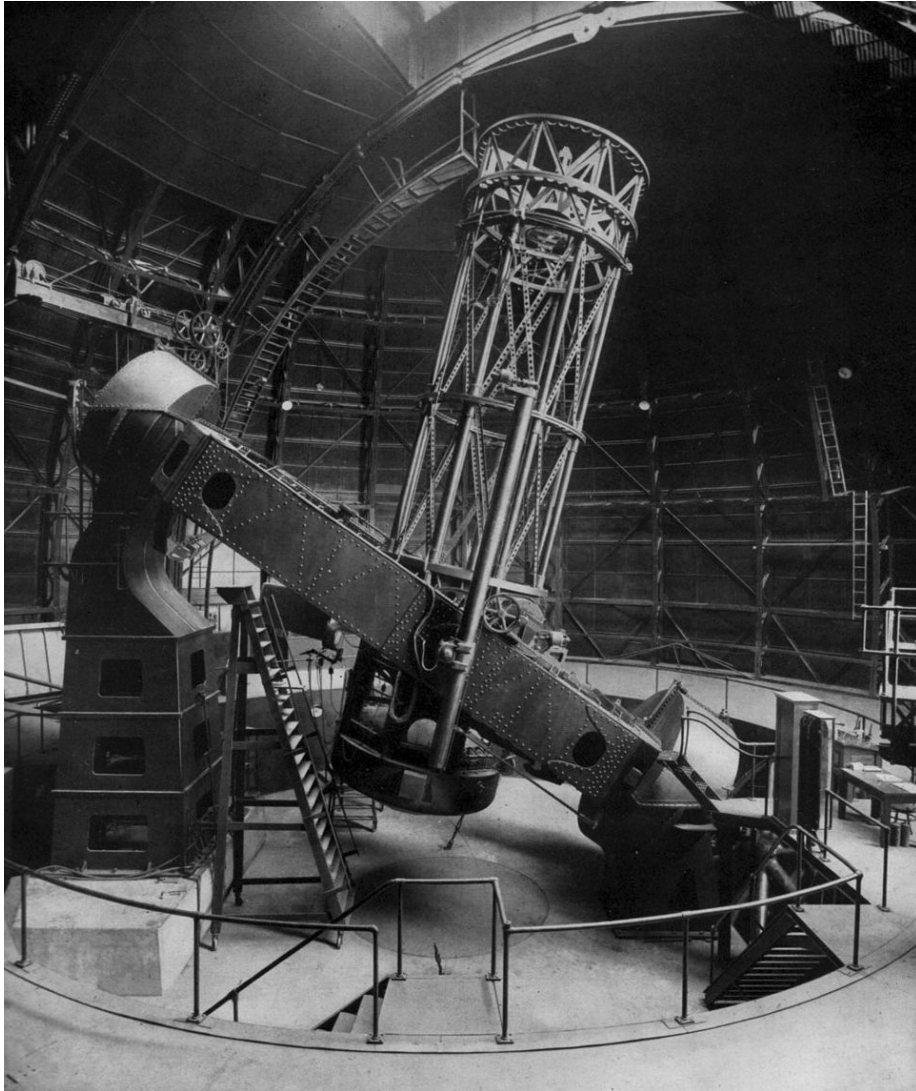
# Hubble & Humason (1931)



Mount Wilson 100 inch Hooker



# New instruments that changed the world ...

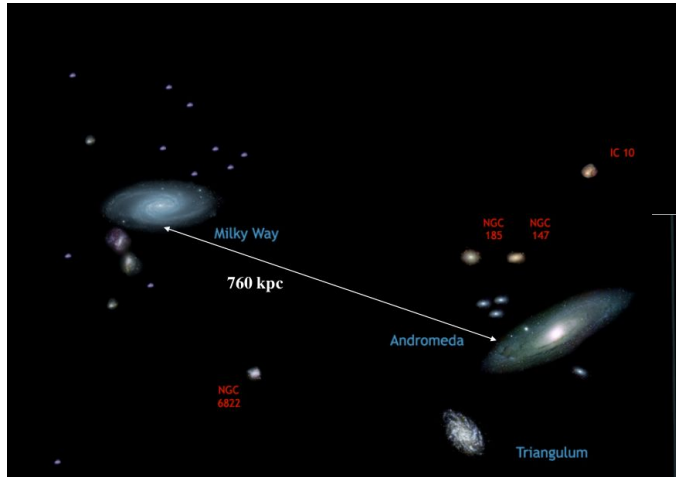


**Edwin Hubble at the  
100-inch Hooker telescope**

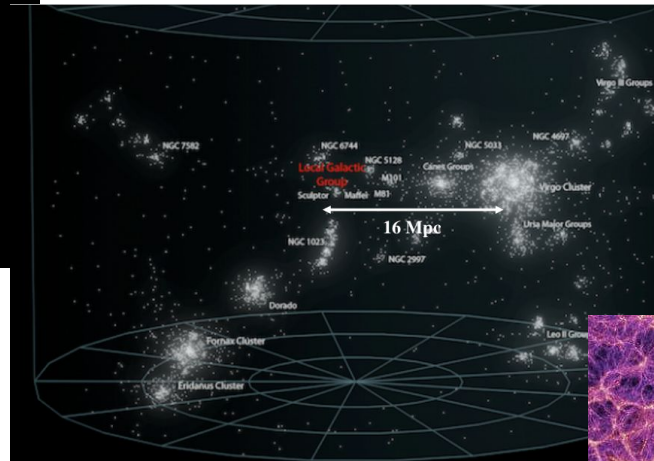
# Expansion

- The Universe is dynamic
  - In the past, the Universe was
    - Denser
    - Hotter
    - -> “initial singularity”
- *Isotropic expansion in a homogeneous Universe*
  - All observers see the same expansion

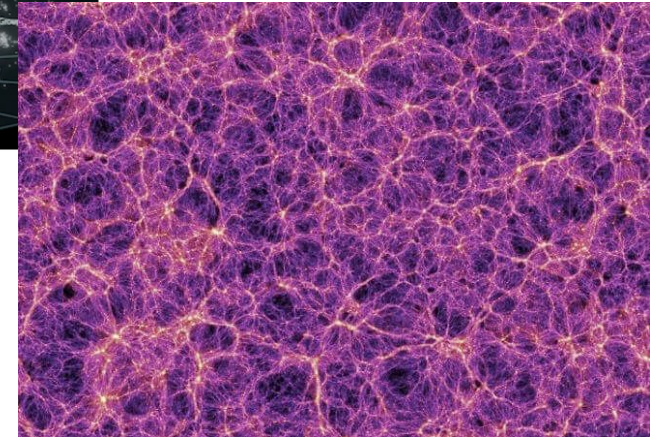
# Isotropy



1 Mpc : not isotropic



20 Mpc : not isotropic



100 Mpc : not isotropic

# Homogeneity

- Universe obviously not homogeneous on the small scales, but seems very homogeneous on the large scales (galaxy counts)
  - $\sim$  a few meters around us:  $\sim 100 \text{ kg / m}^3$ 
    - $\rightarrow 10^{28}$  orders of magnitude above Universe density
  - $\sim$  a few AUs around us:  $10^{-5} \text{ kg / m}^3$ 
    - $\rightarrow 10^{21}$  orders of magnitude above Universe density
  - $\sim$  a few Mpc around us:  $3 \cdot 10^{-26} \text{ kg / m}^3$ 
    - $\rightarrow 1$  order of magnitude above Universe density
  - Very homogeneous above 100 Mpc

# Beware that ...

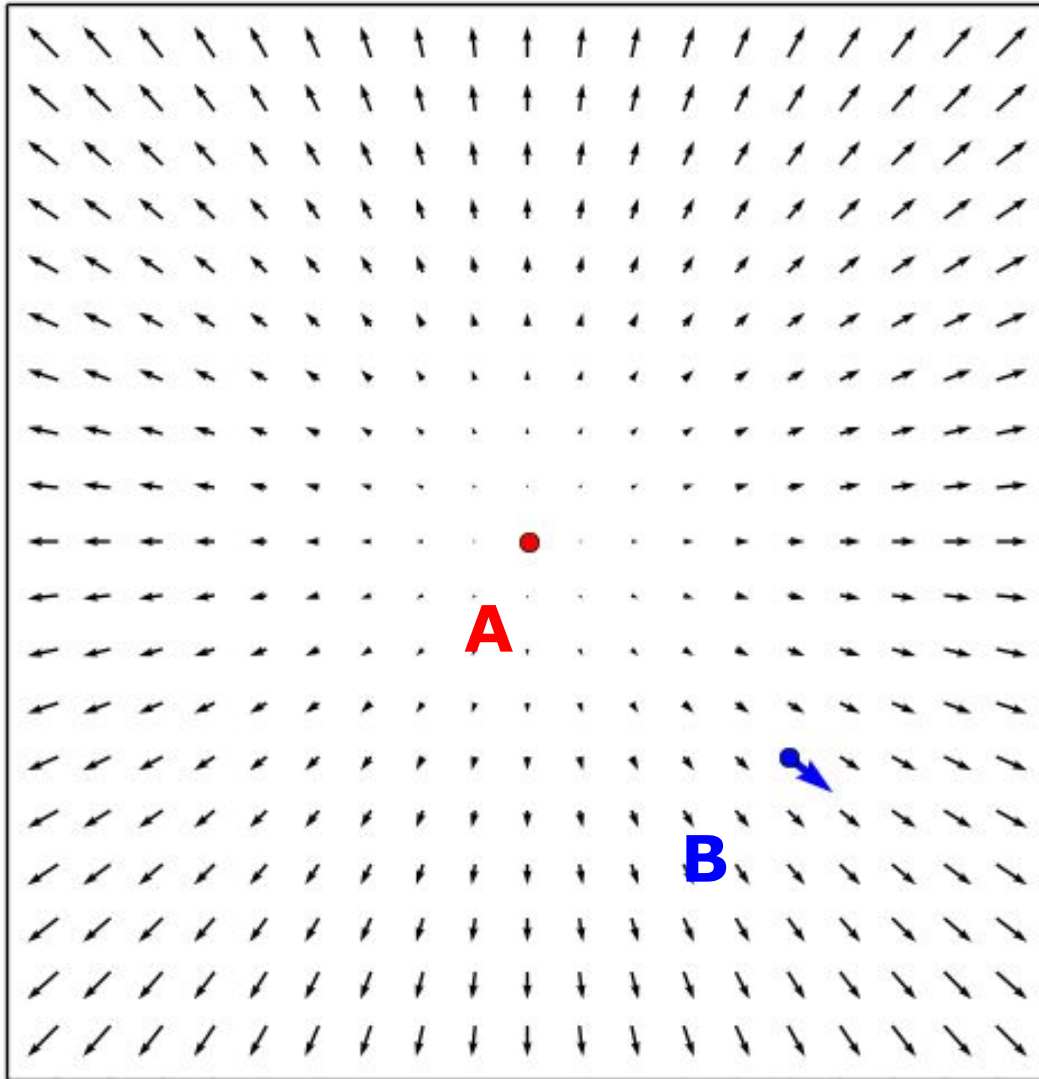
- Homogeneity does not imply isotropy !
- Isotropy does not imply homogeneity !

- Copernican Principle:

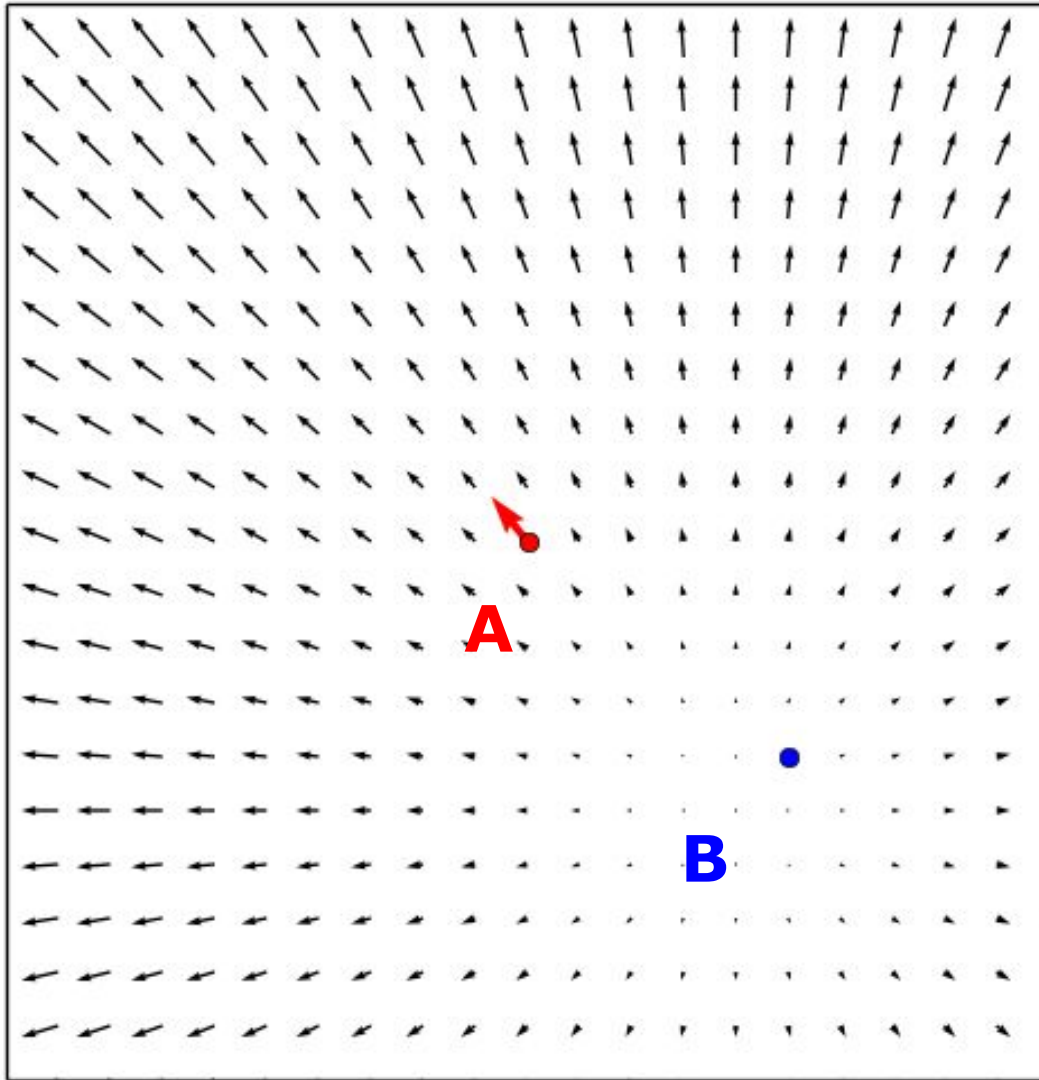
no privileged position in the Universe

Copernican Principle + Isotropy => homogeneity

Copernican Principle + isotropy -> strong constraints on the expansion law.

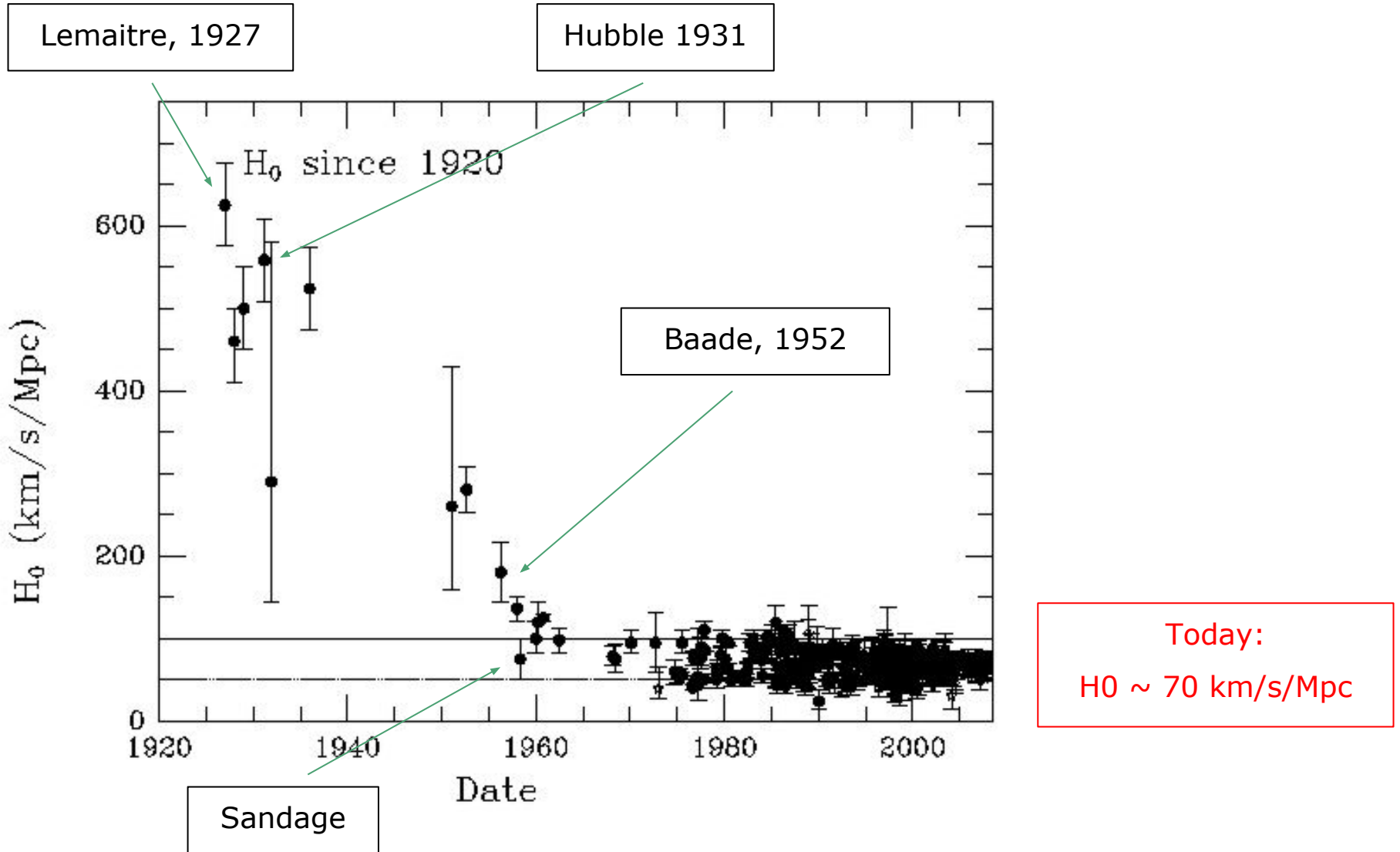


What galaxy **A** sees



What galaxy B sees

# Measuring $H_0$

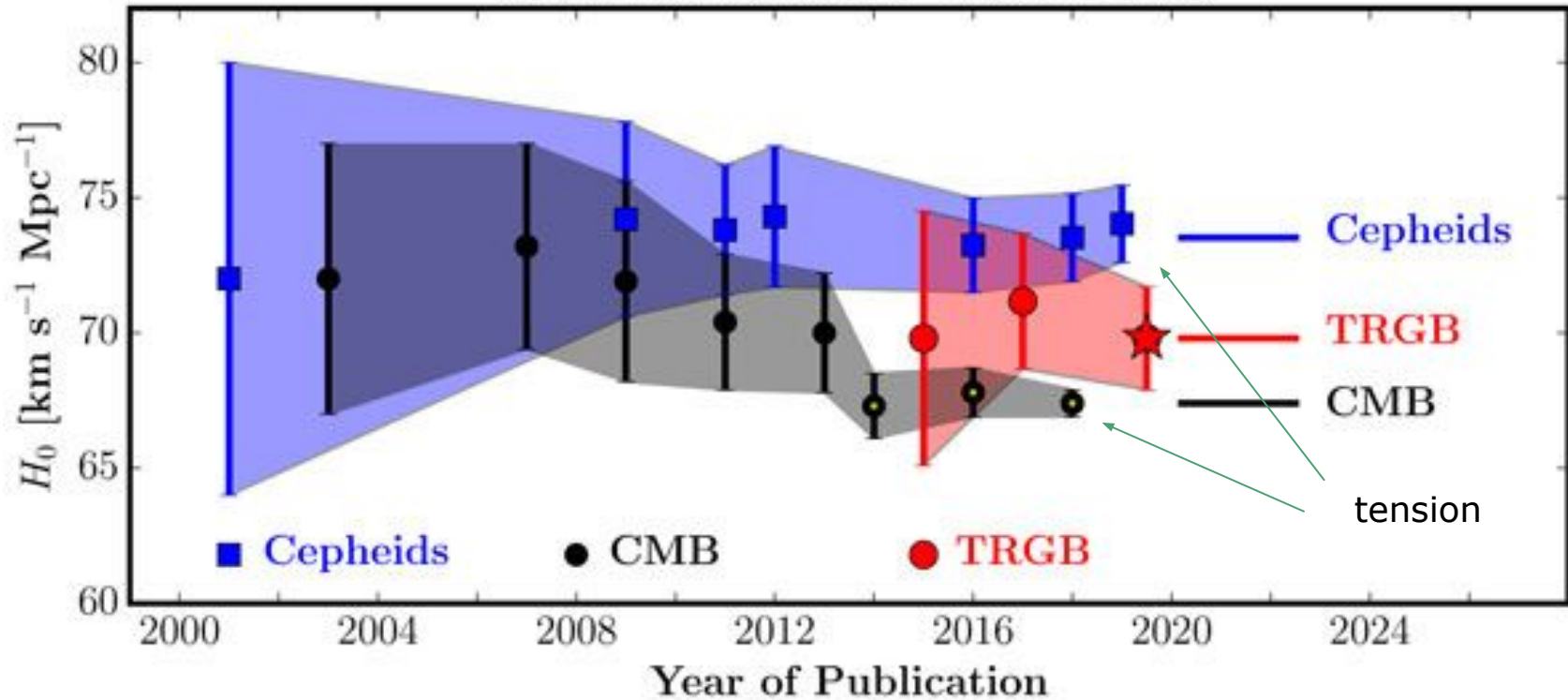


Measuring cosmological distances is very hard !



... today ...

Hubble Constant Over Time



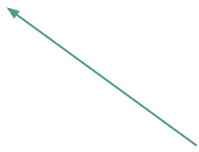
But this is another story which will be told later in this class.

# Value of the Hubble constant

$$v \approx cz = H_0 \times d$$

$$H_0 = 100 h \text{ km/s/Mpc}$$

$$H_0 = 70 h_{70} \text{ km/s/Mpc}$$



Allows to carry uncertainties on  $H_0$  in the computations

Hubble Key Project :  $H_0 = 72 \pm 8$

Local Universe

Riess et al, 2016 :  $H_0 = 73.24 \pm 1.74$

WMAP :  $H_0 = 70.5 \pm 1.3$

Early Universe (CMB)

Planck :  $H_0 = 67.8 \pm 0.9$

# Hubble time

- $H_0$  has the dimension of  $[T^{-1}]$

$$t_H = \frac{1}{H_0} = 13.97 \cdot 10^9 h_{70}^{-1} \text{ yr}$$

Hubble time

Time elapsed since so-called "singularity"

Not exactly though, just the scale, extrapolating today's measurement of H

(Remember:  $1\text{Mpc} = 3.086 \cdot 10^{22} \text{ m}$ )

# Hubble length

- Hubble length

$$d_H = \frac{c}{H_0} = 4300 h_{70}^{-1} \text{ Mpc}$$

- Typical size of observed Universe
- If  $z \ll 1$ , easy to get distances from redshift

$$d \approx z \times d_H$$

# Critical density

- With  $H_0$  [ $T^{-1}$ ] and  $G$  [ $M^{-1}L^3T^{-2}$ ], one can form a density

$$\rho_c = \frac{3H^2}{8\pi G}$$

- Called “critical density” (see later why “critical”)

$$\rho_c = 0.91 h_{70}^2 10^{-26} \text{ kg m}^{-3}$$

$$\rho_c = 1.34 h_{70}^2 10^{11} M_{\odot} \text{Mpc}^{-3}$$

$$\rho_c = 0.51 h_{70}^2 10^{10} \text{ eV m}^{-3}$$

- Densities often expressed in units of  $\rho_{c,0}$  (today)

$$\Omega_x = \frac{\rho_x}{\rho_c}$$

# Summary

- 1915 : general relativity
- 1915 - 1920's Slipher and others notice that most distant "nebulae" are redshifted
- 1922 : Alexander Friedmann finds evolving solutions to Einstein equations
- 1927 : Lemaitre's paper
- 1929 : Hubble & Humason find proportionality between distances and recession velocity



# A newtonian approach to expansion

$$\frac{\ddot{R}}{R} = -\frac{4\pi G\rho}{3}$$

Expansion should be decelerated

$$\rho \propto R^{-3}$$
$$\left(\frac{\dot{R}}{R}\right)^2 = \frac{8\pi G\rho}{3} + H_0^2(1 - \Omega_M) \left(\frac{R}{R_0}\right)^{-2}$$
$$\left(\frac{\dot{R}}{R}\right)^2 = H_0^2 \left( \Omega_M \hat{R}^{-3} + (1 - \Omega_M) \hat{R}^{-2} \right)$$



$$\left(\frac{\dot{R}}{R}\right)^2 = H_0^2 \left(\Omega_M \hat{R}^{-3} + (1 - \Omega_M) \hat{R}^{-2}\right)$$

$$\Omega_M > 1 \longrightarrow \text{Expansion stops at } R = R_0 \frac{\Omega_M}{\Omega_M - 1}$$

Then, contraction, because  $d^2R/dt^2 < 0$

$$\Omega_M = 1 \longrightarrow R(t) = R_0 \left(\frac{t}{(2/3)H_0^{-1}}\right)^{2/3}$$

“critical”

Eternal (decelerated) expansion – smaller Hubble time

$$\Omega_M < 1 \longrightarrow \text{Eternal (decelerated) expansion}$$

Special case: empty Universe:

$$R(t) = R_0 \frac{t}{H_0^{-1}}$$

Hubble time

# Outline

- What is cosmology ?
- Cosmology through the ages
- The first revolution (1925) : the Universe is Big !
- The second revolution (1927 - 1931) : the Universe is expanding !
- **The hot big-bang model**
- Observables
- The third revolution (1999-2003) : accelerated expansion &  $\Lambda$ DCM
- Our strange Universe

# The Hot Big-Band model

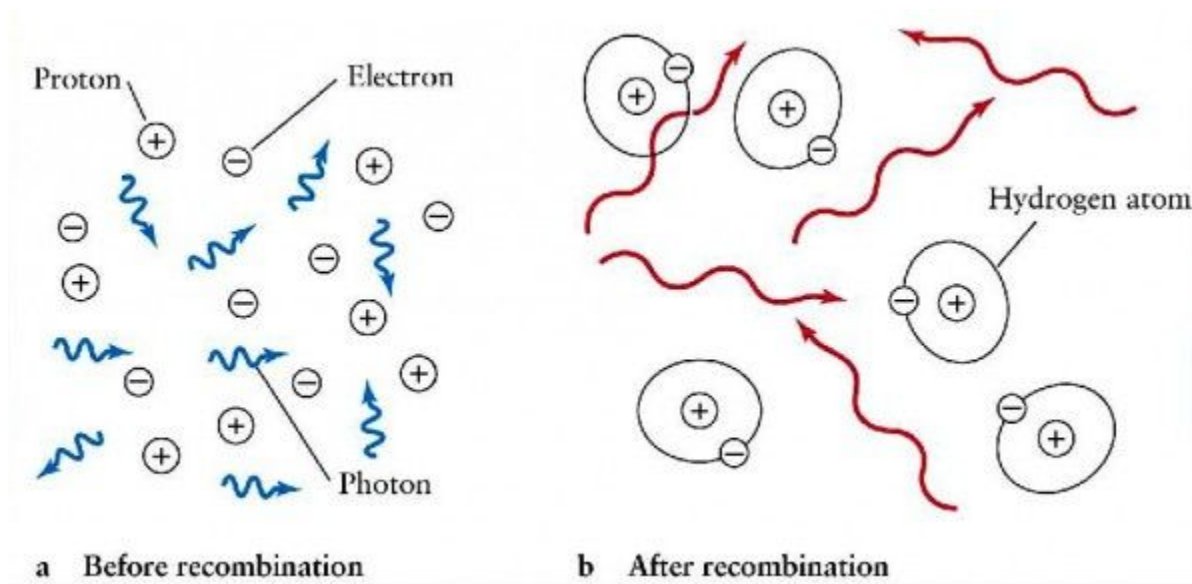
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# Modeling the Universe

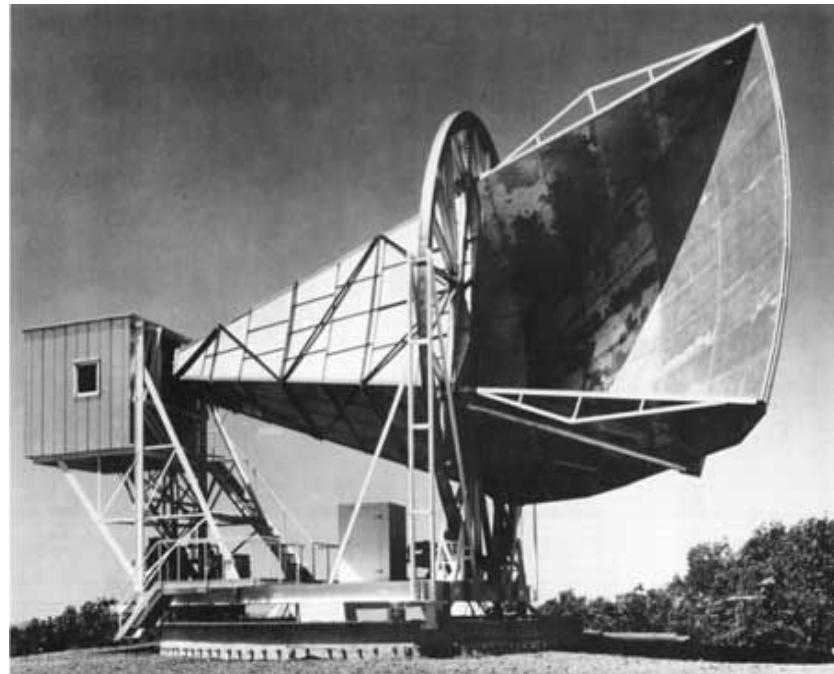
- Foundations
  - The Universe is big
  - The Universe is expanding from some kind of “initial singularity” that occurred  $\sim 1t_H = 14$  Gyr ago
  - Beyond  $\sim 100$  Mpc, the Universe is
    - Isotropic
    - Homogeneous
  - Copernican principle: no privileged position in the Universe

# Cosmological microwave background

- Predicted by Gamow (1948)
  - $\sim 300000$  yrs after BB
  - Universe was an opaque plasma
  - Expansion  $\rightarrow$  Universe getting colder  $\rightarrow$  recombination  $e/\gamma \rightarrow$  decoupling matter and photons
- We should be able to see this relic !



- Discovered by Penzias & Wilson
- In 1963
- Nobel Prize in 1978



## A MEASUREMENT OF EXCESS ANTENNA TEMPERATURE AT 4080 Mc/s

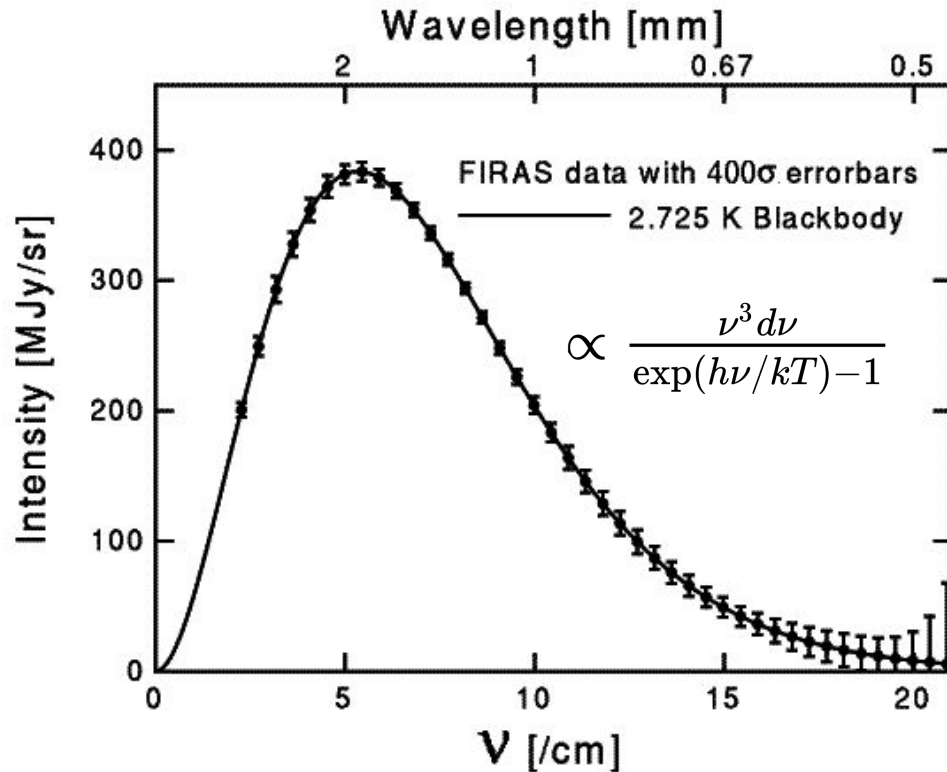
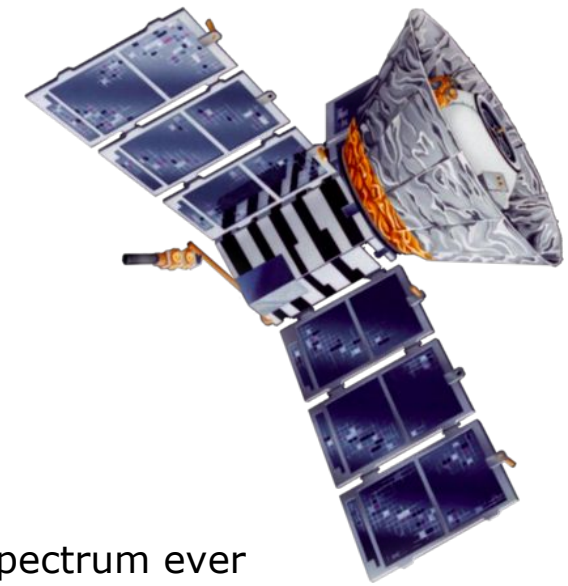
Measurements of the effective zenith noise temperature of the 20-foot horn-reflector antenna (Crawford, Hogg, and Hunt 1961) at the Crawford Hill Laboratory, Holmdel, New Jersey, at 4080 Mc/s have yielded a value about  $3.5^\circ$  K higher than expected. This excess temperature is, within the limits of our observations, isotropic, unpolarized, and

- The Dicke et al paper
- With the correct cosmological interpretation of the P&W result

### COSMIC BLACK-BODY RADIATION\*

One of the basic problems of cosmology is the singularity characteristic of the familiar cosmological solutions of Einstein's field equations. Also puzzling is the presence of matter in excess over antimatter in the universe, for baryons and leptons are thought to be conserved. Thus, in the framework of conventional theory we cannot understand the origin of matter or of the universe. We can distinguish three main attempts to deal with these problems.

# CMB spectrum



Best blackbody spectrum ever measured

$$T = 2.726 \pm 0.0012$$

(Fixen et al, 2009)

$$\epsilon_\gamma = aT^4$$

$$(a = 7.566 \cdot 10^{-16} \text{ J/m}^3/\text{K}^4)$$

$$e_\gamma \approx 2.7kT$$

$$n_\gamma \approx ?$$

$$\Omega_\gamma \approx ?$$

# BTW, how many photons from stars ?

- Number of galaxies per volume

Not very well known. Diverges at small galaxy luminosities (which do not contribute much to the total luminosity).

$$n_{gal} \sim 0.015 h_{70}^3 \text{ Mpc}^3$$


- Average luminosity of a galaxy

$$L_{gal} \sim 10^{10} L_{\odot}$$

- Time  $\sim 10$  Gyr,  $e_{\gamma} \sim 2$  eV

??? photons /  $\text{cm}^3$

$$1 \text{ Mpc} = 3.0856 \cdot 10^{24} \text{ cm}$$

$$1 L_{\odot} = 3.84 \cdot 10^{26} \text{ W}$$



# How much visible matter ?

- Typical mass-to-luminosity ratio for galaxies

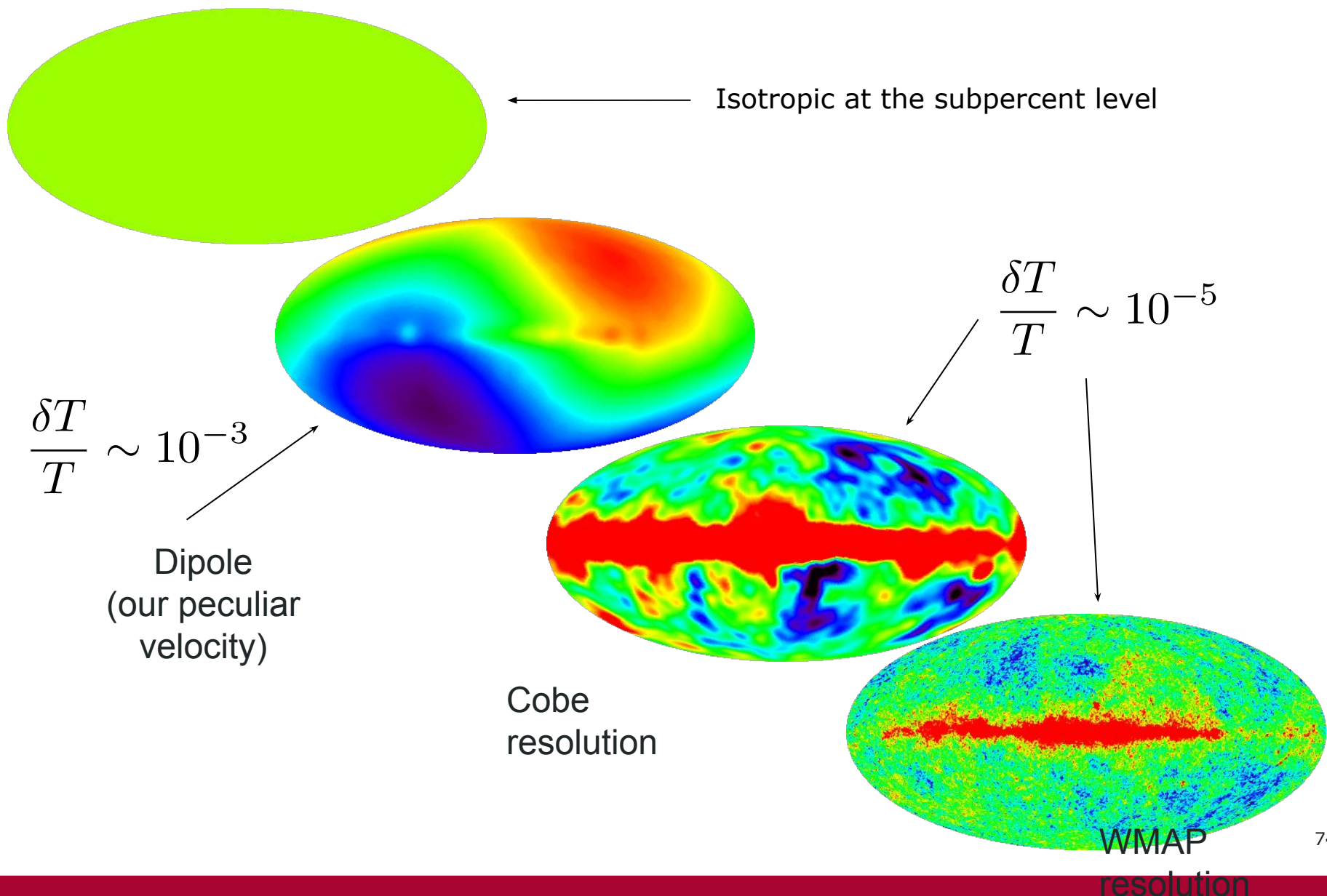
$$\left\langle \frac{M}{L} \right\rangle \sim 2.5 \frac{M_{\odot}}{L_{\odot}}$$

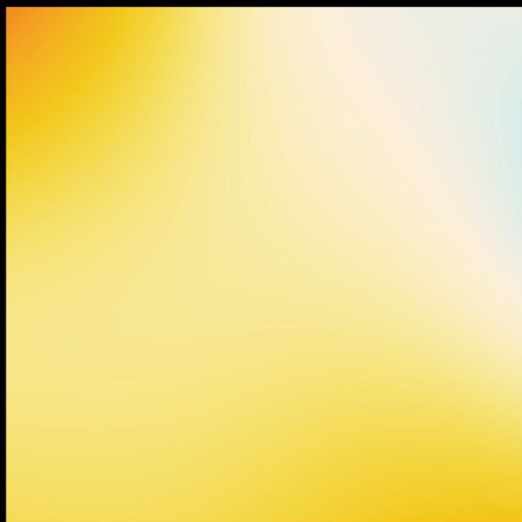
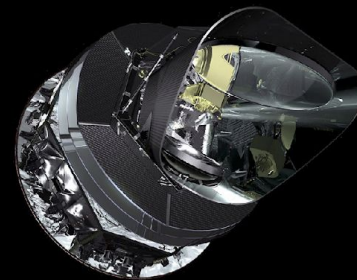
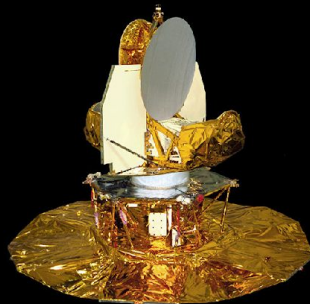
- Density of visible matter in units of the critical density ?

$$n_{\text{gal}} \sim 0.015 \text{ Mpc}^{-3}$$

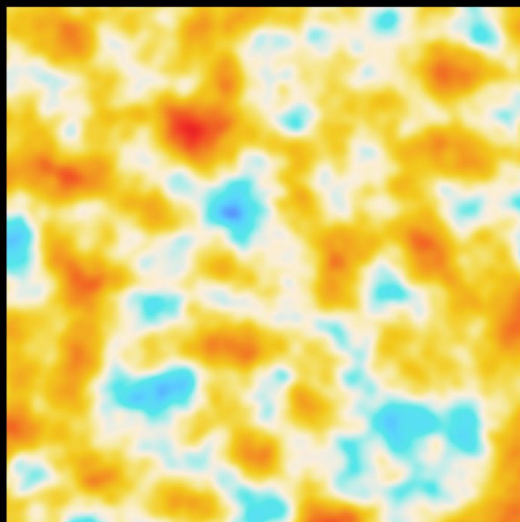
$$\rho_{\text{crit}} = 1.34 \cdot 10^{11} M_{\odot}/\text{Mpc}^3$$

# CMB anisotropies

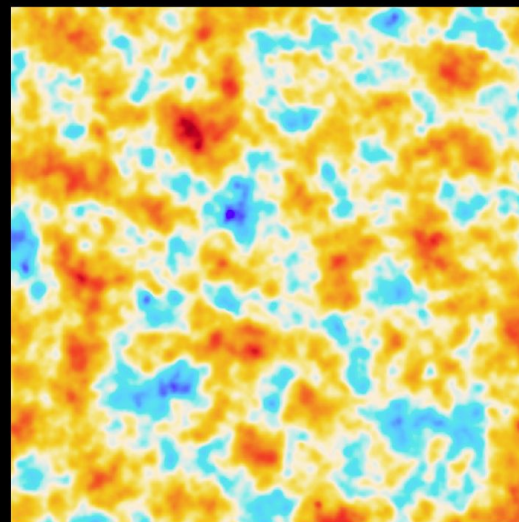




COBE

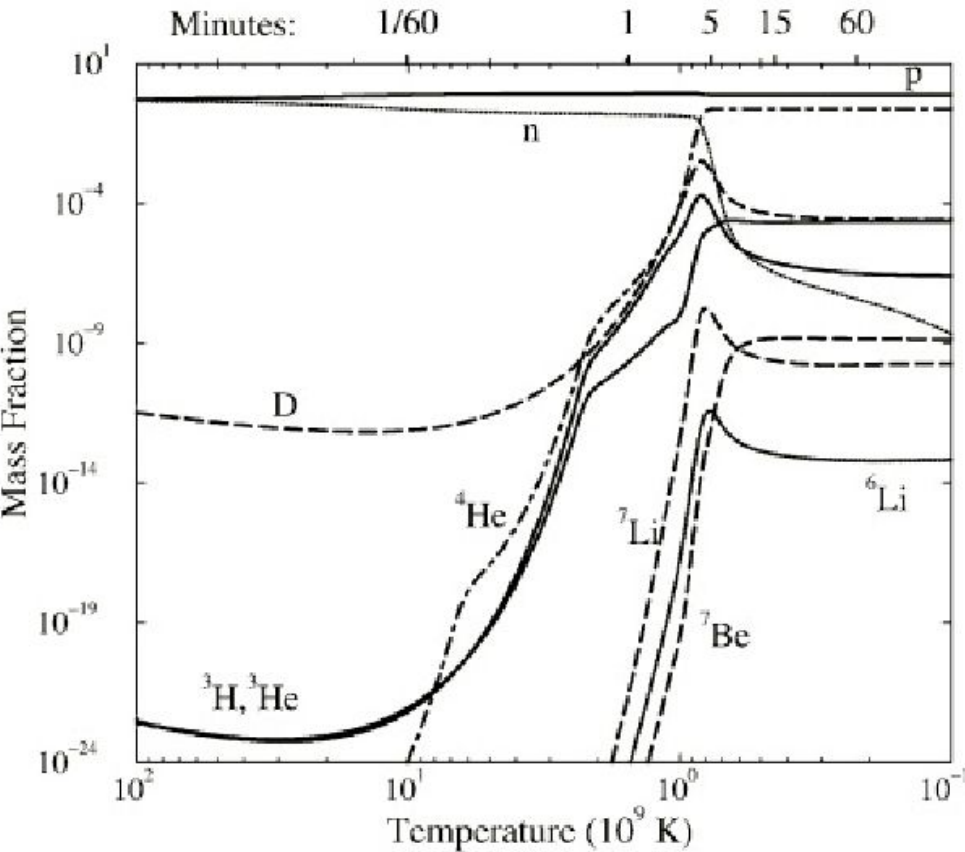


WMAP

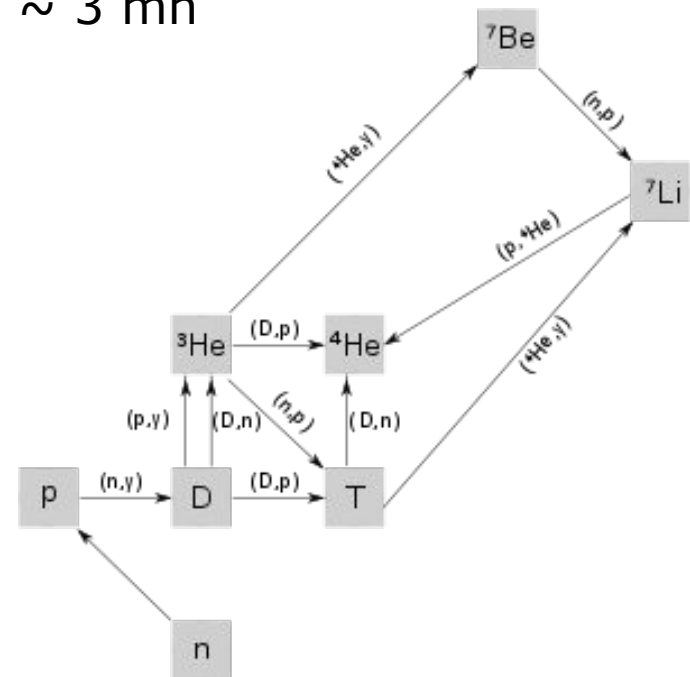


Planck

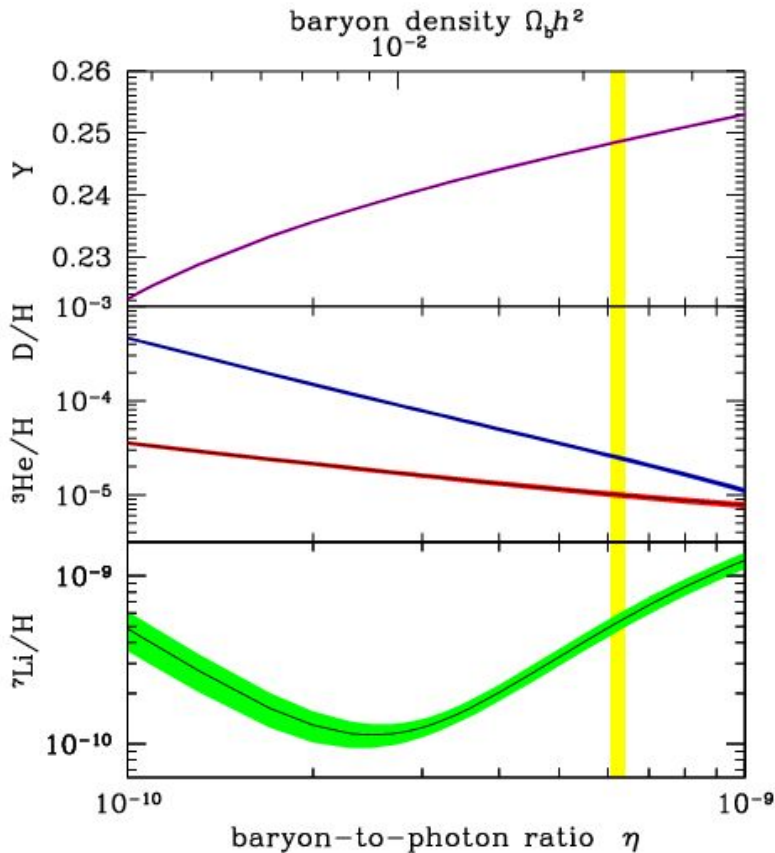
# Big-Bang nucleosynthesis



- $T \sim \text{MeV} \rightarrow \sim 60 \text{ keV}$
- Synthesis of light elements
  - D,  $\text{He}3$ ,  $\text{He}4$ ,  $\text{Li}6$ ,  $\text{Li}7$
- Stops when density gets too low
- $\sim 3 \text{ mn}$



# Big-Bang nucleosynthesis



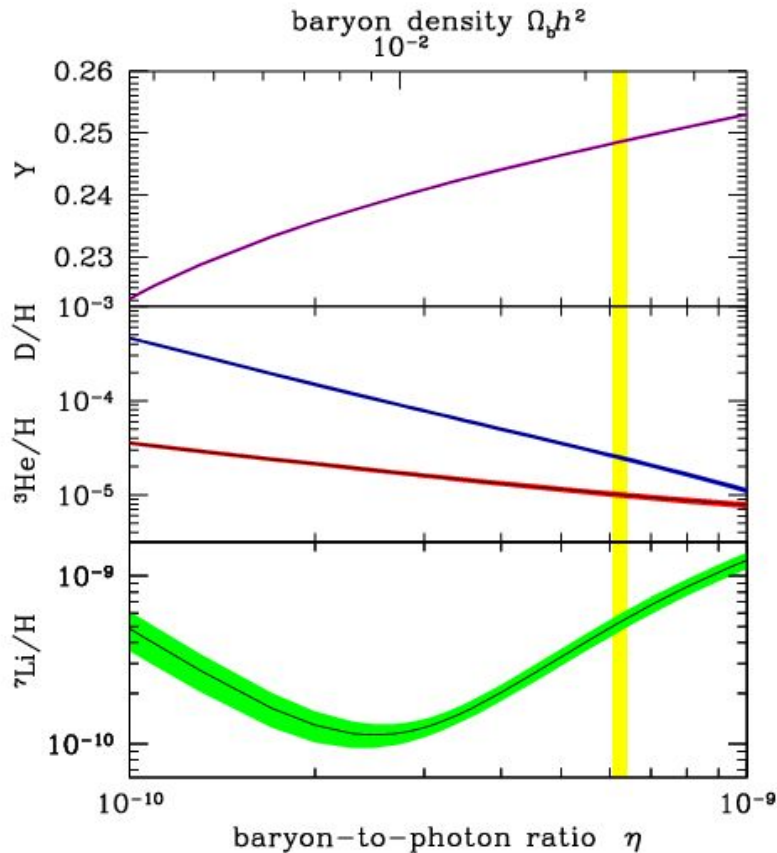
- Fundamental parameter

$$\eta = \frac{N_b}{N_\gamma}$$

- + expansion history
- Constraining abundances

- Tests of model
- Constraints on  $\Omega_b h^{-2}$
- Since  $n_\gamma$  is known

# Big-Bang nucleosynthesis



- Measurements from quasar absorption systems
- Absorption lines from primordial clouds on the line of sight

$$\eta \sim 6.10^{-10}$$



$$\Omega_b h^{-2} \approx ?$$

Conclusion ?

# M/L ratio of clusters



## ON THE MASSES OF NEBULAE AND OF CLUSTERS OF NEBULAE

F. ZWICKY

ABSTRACT

Present estimates of the masses of nebulae are based on observations of the *luminosities* and *internal rotations* of nebulae. It is shown that both these methods are unreliable; that from the observed luminosities of extragalactic systems only lower

# Virial theorem

- **Statistical theorem of classical mechanics**
  - For a system of particles in stable equilibrium bound by gravitation (e.g. a cluster of galaxies), we have

$$2 \langle T \rangle = -V_g$$

Kinetic energy of particles  
(random motions)

Gravitational potential energy  
due to mutual attraction of  
particles

Can be measured

Give access to  
total mass



For a galaxy cluster

$$V_g = -\frac{16\pi^2}{15} G \langle \rho \rangle^2 R^5 = -\frac{3}{5} \frac{GM^2}{R}$$

$$\langle T \rangle = \frac{1}{2} \sum_i M_i \langle v_i^2 \rangle \approx \frac{1}{2} M \langle \langle v^2 \rangle \rangle$$

$$M = \frac{5R \langle \langle v^2 \rangle \rangle}{3G}$$

# In the case of the Coma cluster...


- $R \sim 613$  kpc
- $v \sim 435$  km/s
- $M_{\text{sun}} = 1.99\text{E}30$  kg
- $\sim 1000$  galaxies,  $L_{\text{gal}} \sim 8.5\text{E}7$   $L_{\text{sun}}$

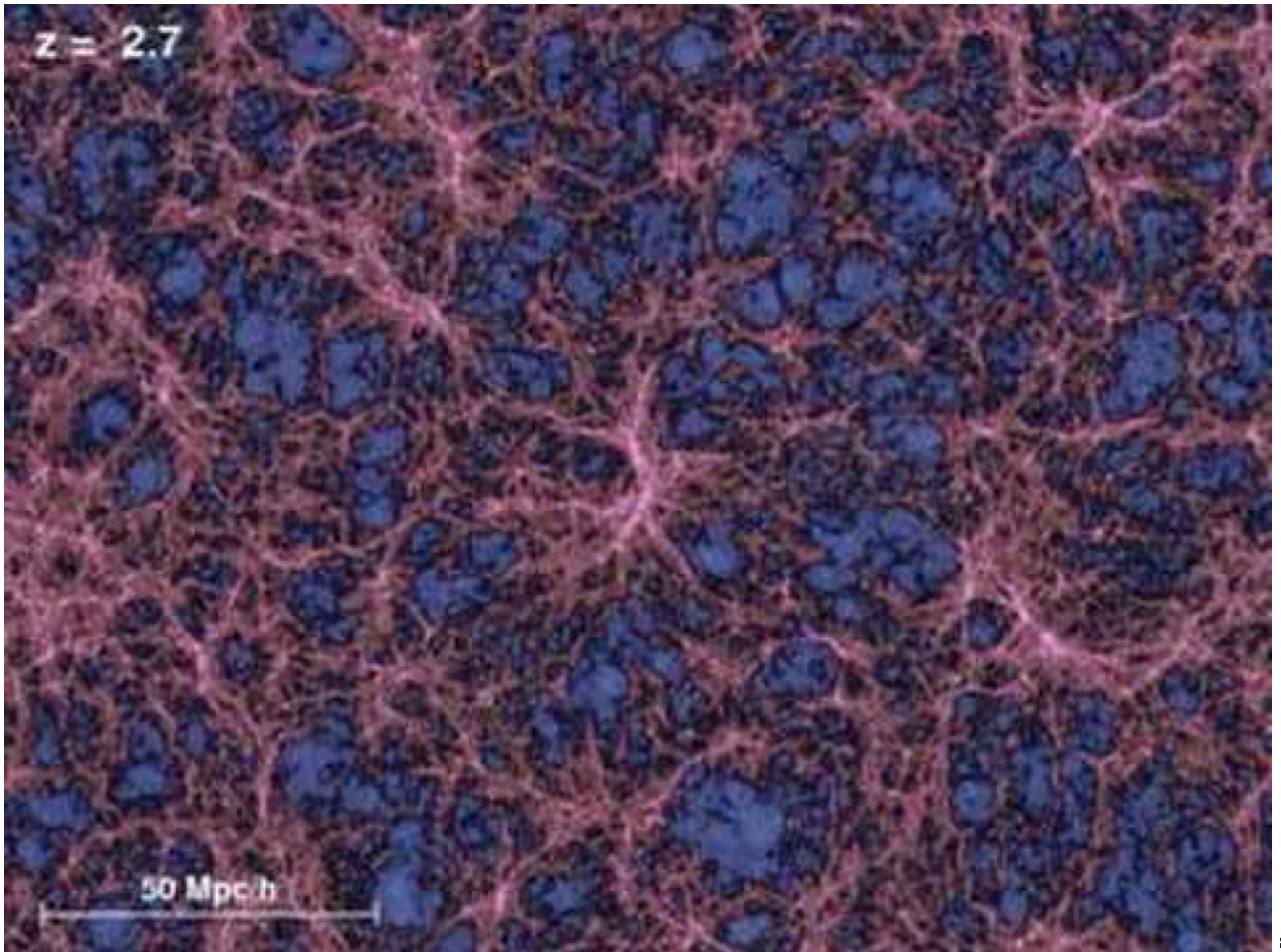
$$\frac{M}{L} = ?$$

# Summary

- **So, we live in a Universe**
  - Bathed in a CMB diffuse background (most abundant particles, weight nothing)
  - With very little visible matter
  - With very little baryons
  - And strong hints from large amounts of non-baryonic dark matter
- **What happens next ?**
  - Structure formation !
  - Filaments, haloes, first galaxies, first stars, first supernovae, re-ionization, second and third generation stars, planets, life ! (baryon physics)

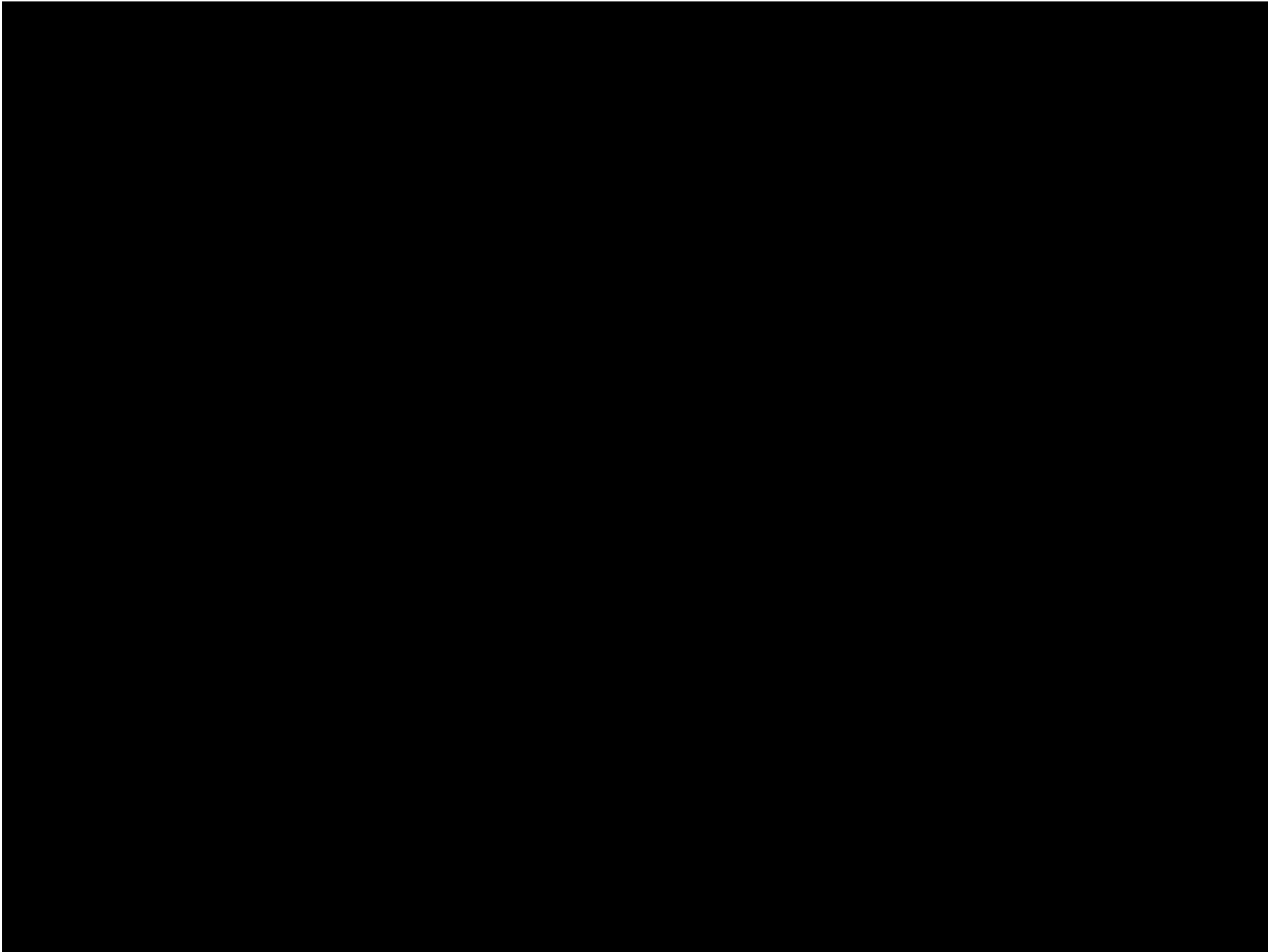
Description of the Universe  
at smaller scales





time since Big Bang  
9.5 Gyr

1 cMpc



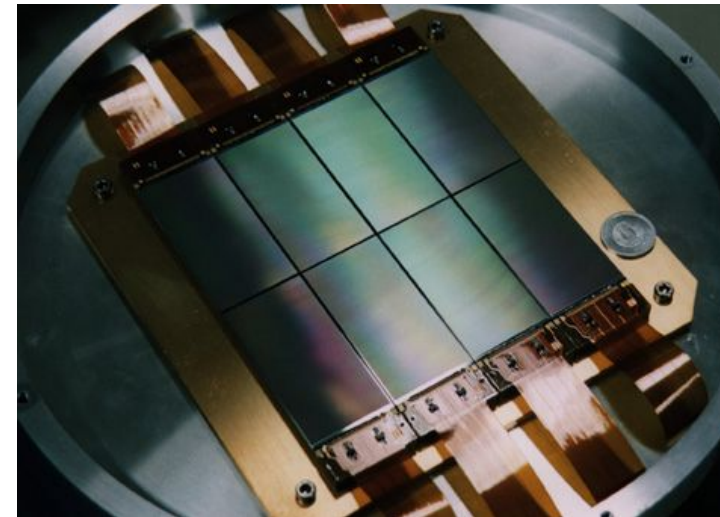
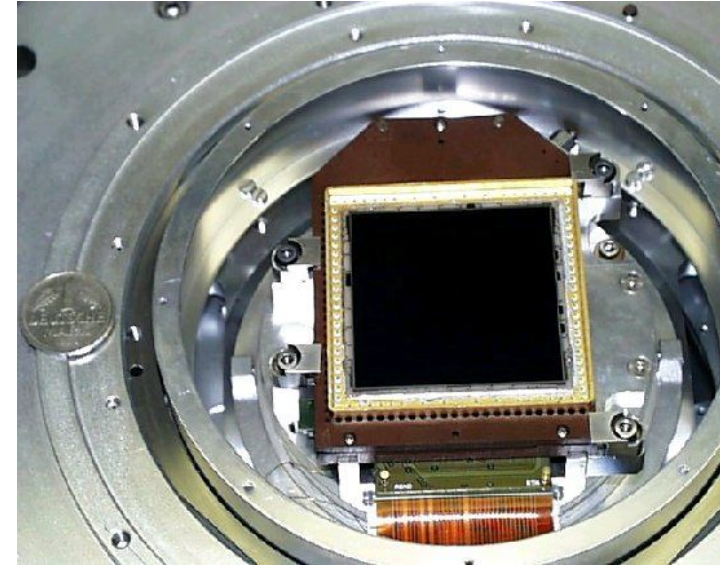
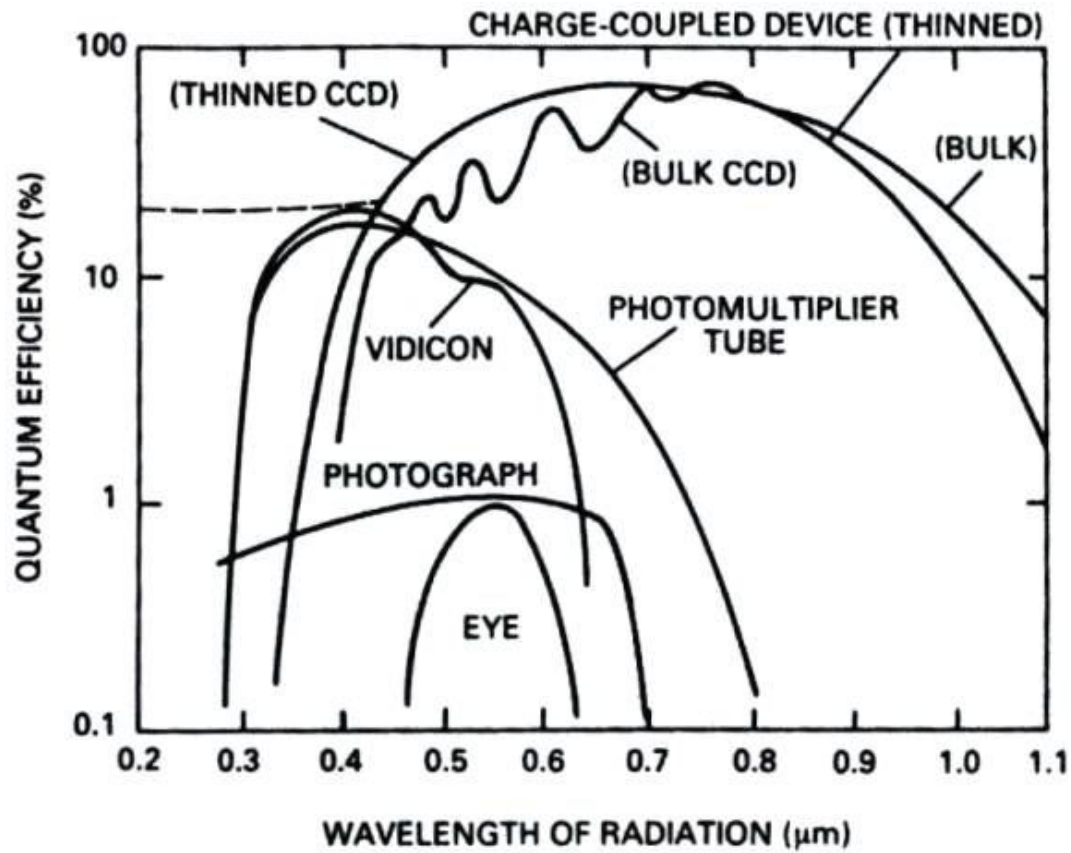
# Nothing more about the smooth Universe ?

In fact, yes, there is.

One last tiny detail ...

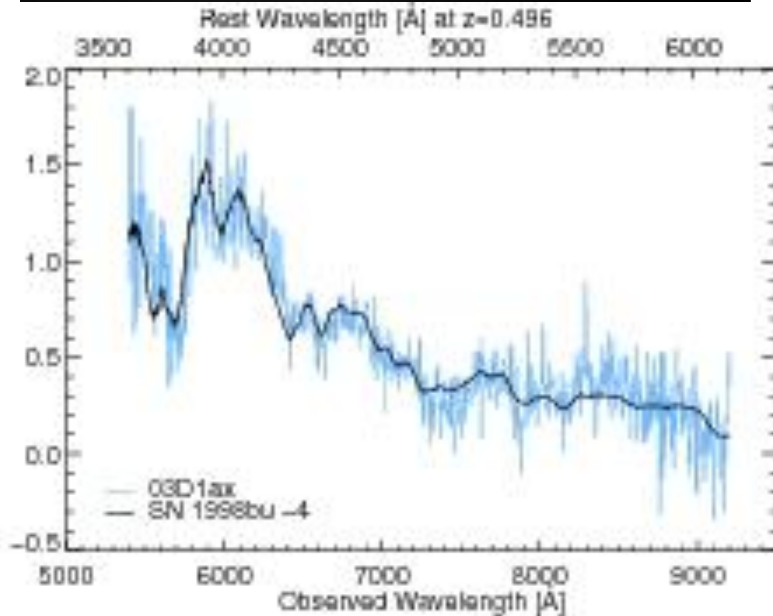
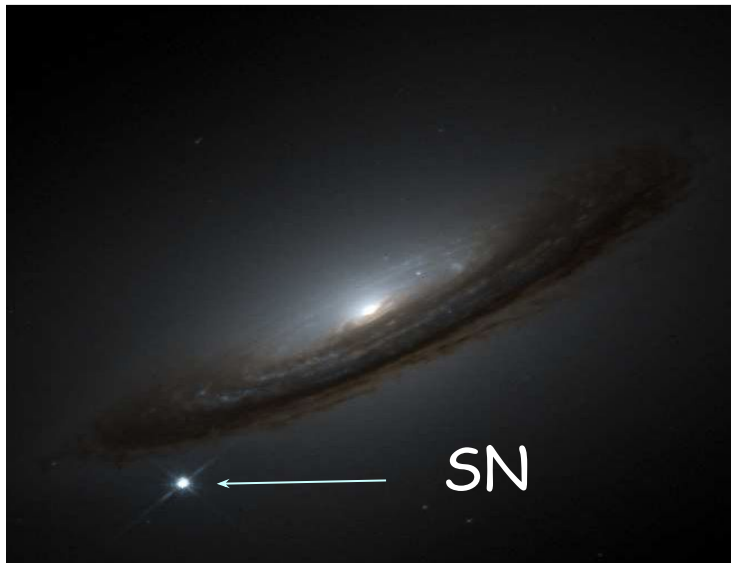
- For 50 years, astronomers have tried (unsuccessfully) to get the first measurements of expansion history
- The reason why this was so difficult:
  - Lack of reliable standard candles (galaxies are not really standard)
  - Lack of data
- then...

# Technological breakthrough : CCD's

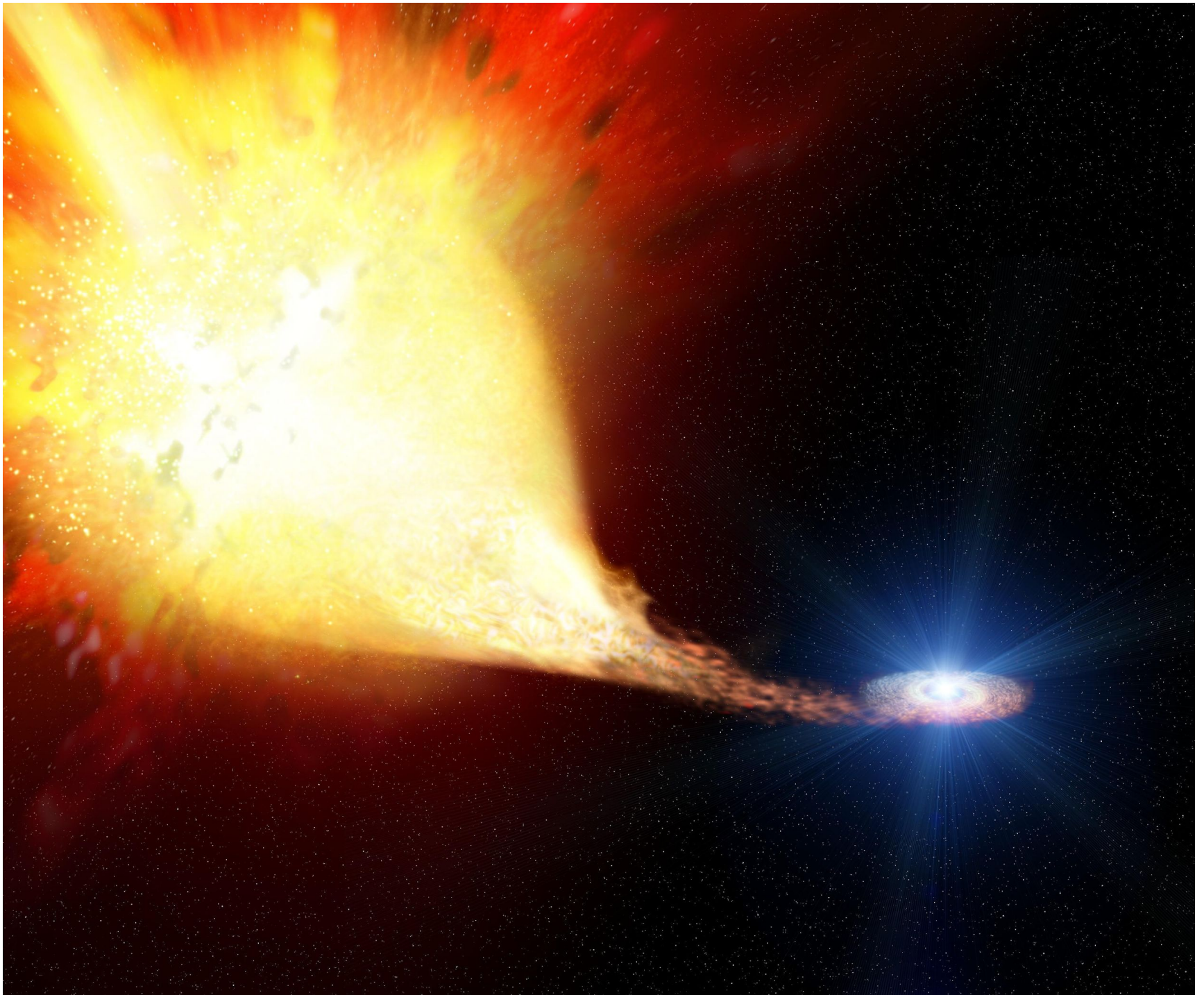


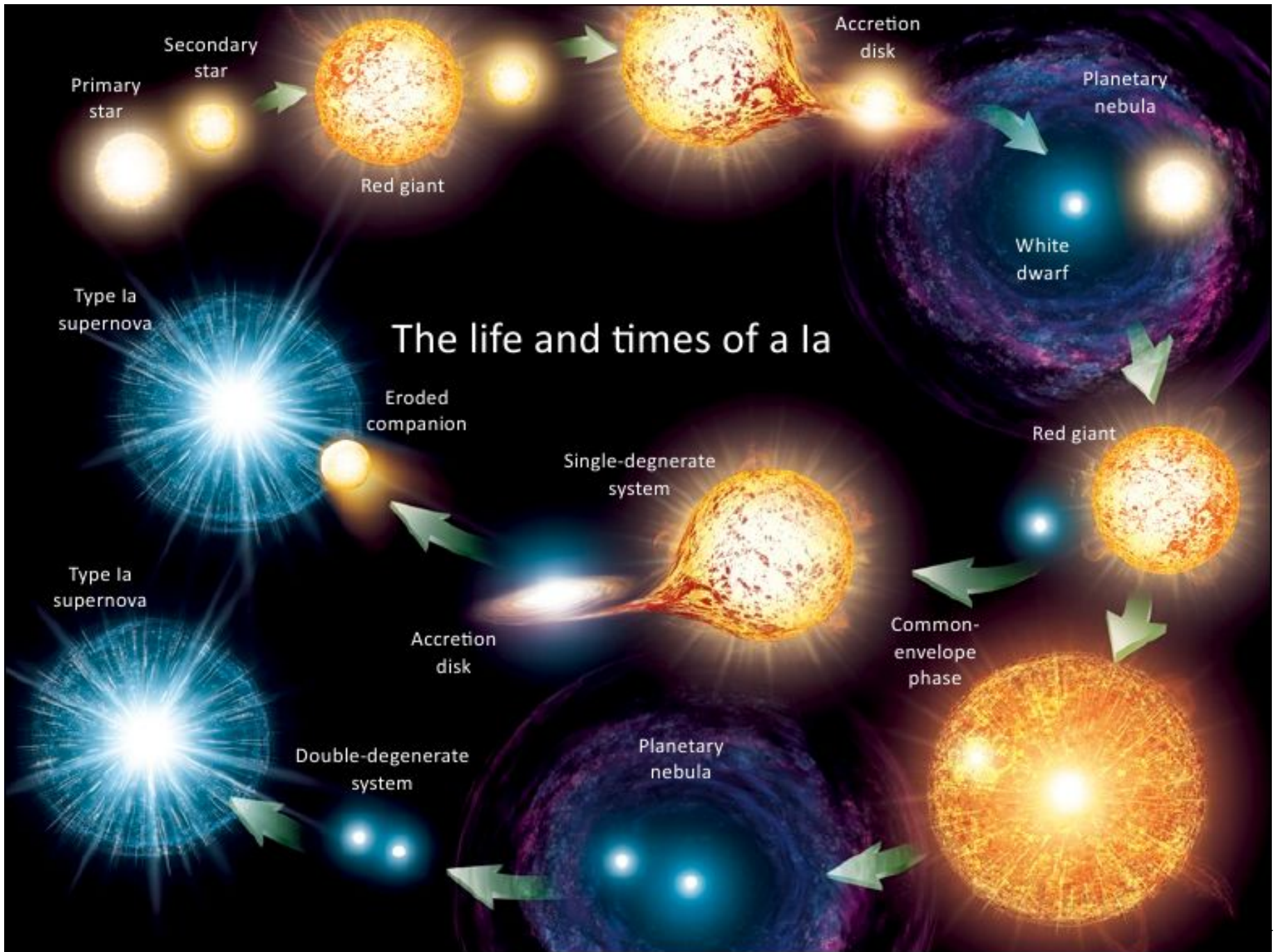


# Type Ia supernovae



- **Thermonuclear explosions of WD's**
  - Rare events
  - Very bright ( $10^{10} L_{\odot}$ )
  - Transients (1 month)
  - $\sigma(L_{\max}) \sim 40\%$
- **Standardizable**
  - $\sigma(L_{\max}) \sim 12\%$
- **Spectroscopy**
  - Identification (broad features)
  - Chemical composition & velocities
  - Redshift (better from host gal)






# Beyond the Hubble law

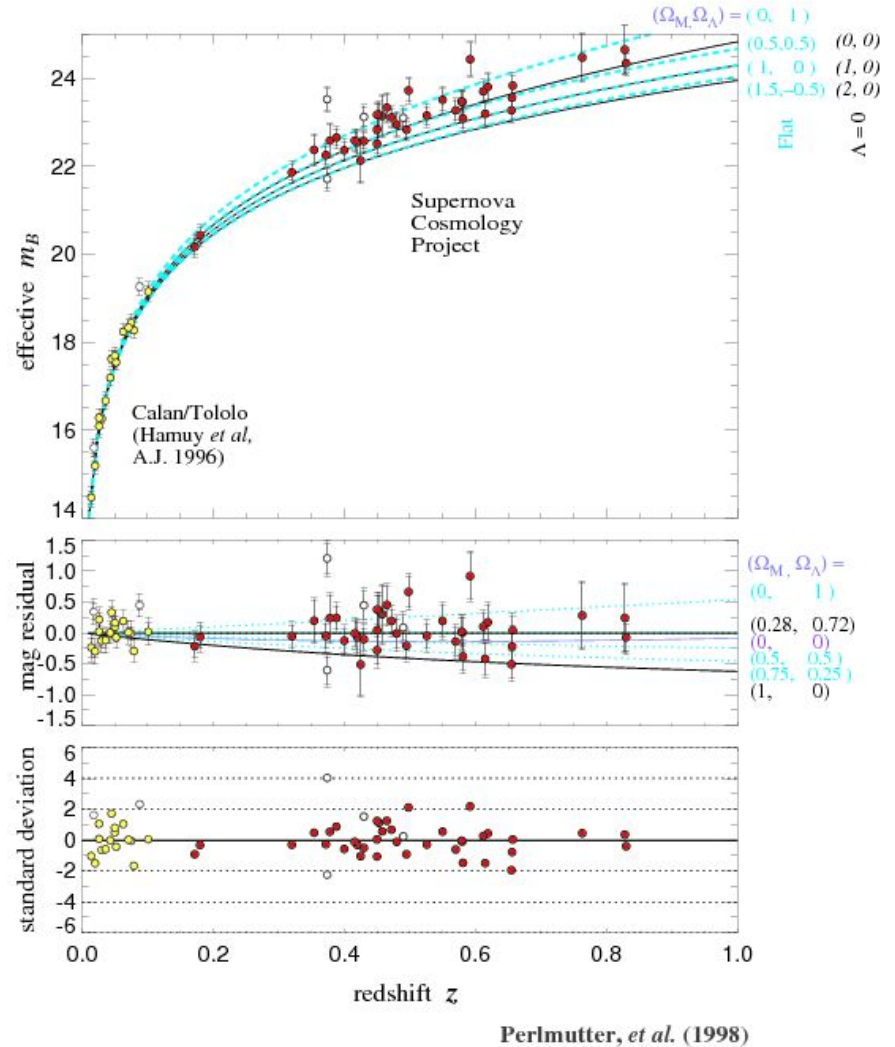
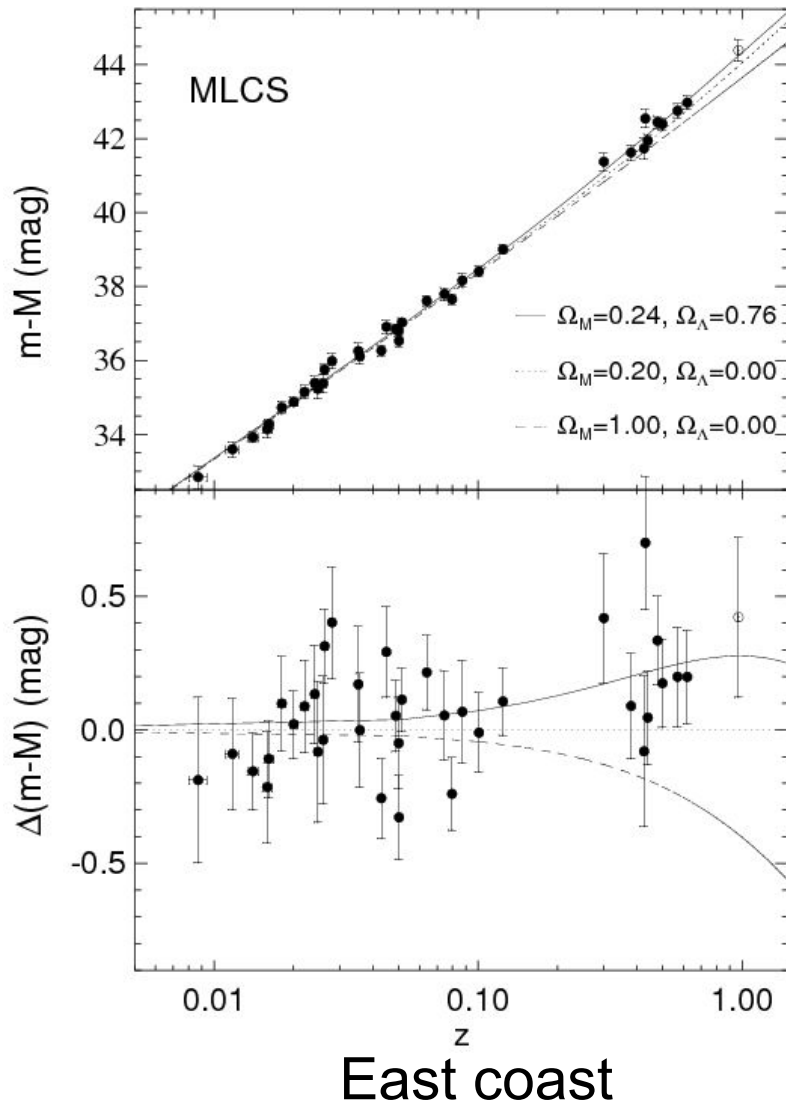
- Program

$$H_0 d_L = z + \frac{1}{2}(1 - q_0)z^2 + \dots$$

$$q_0 \approx \frac{\Omega_m}{2} \quad \text{“Deceleration parameter”}$$


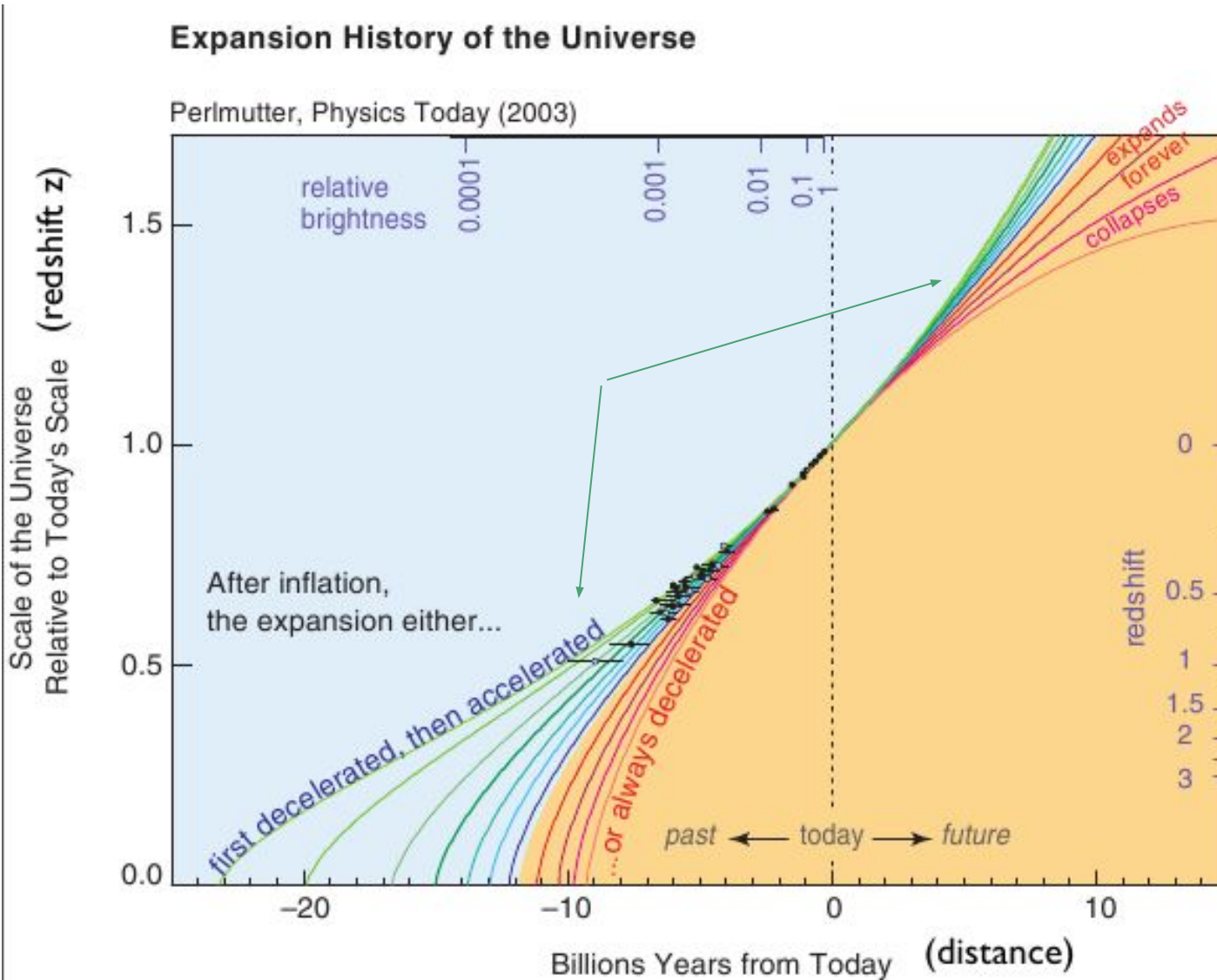
- If we measure  $q_0$ , we have access to  $\Omega_m$  !
  - SNe Ia are ideal candidates to map the Hubble flow
  - But they are rare and faint !

# First measurements @ $z \sim 0.5$



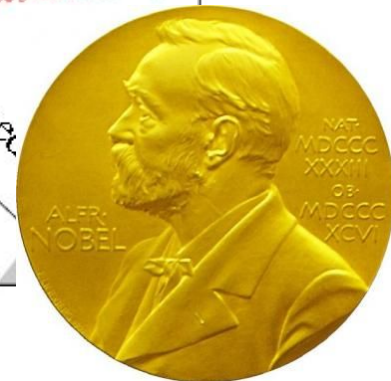
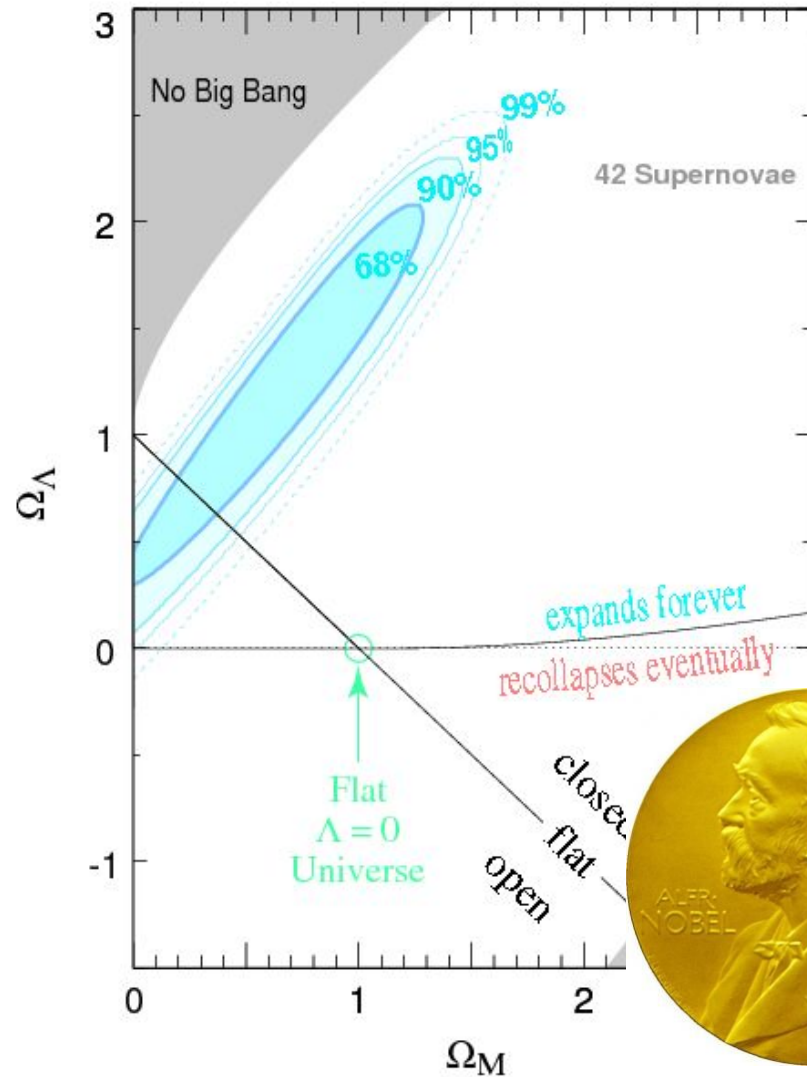
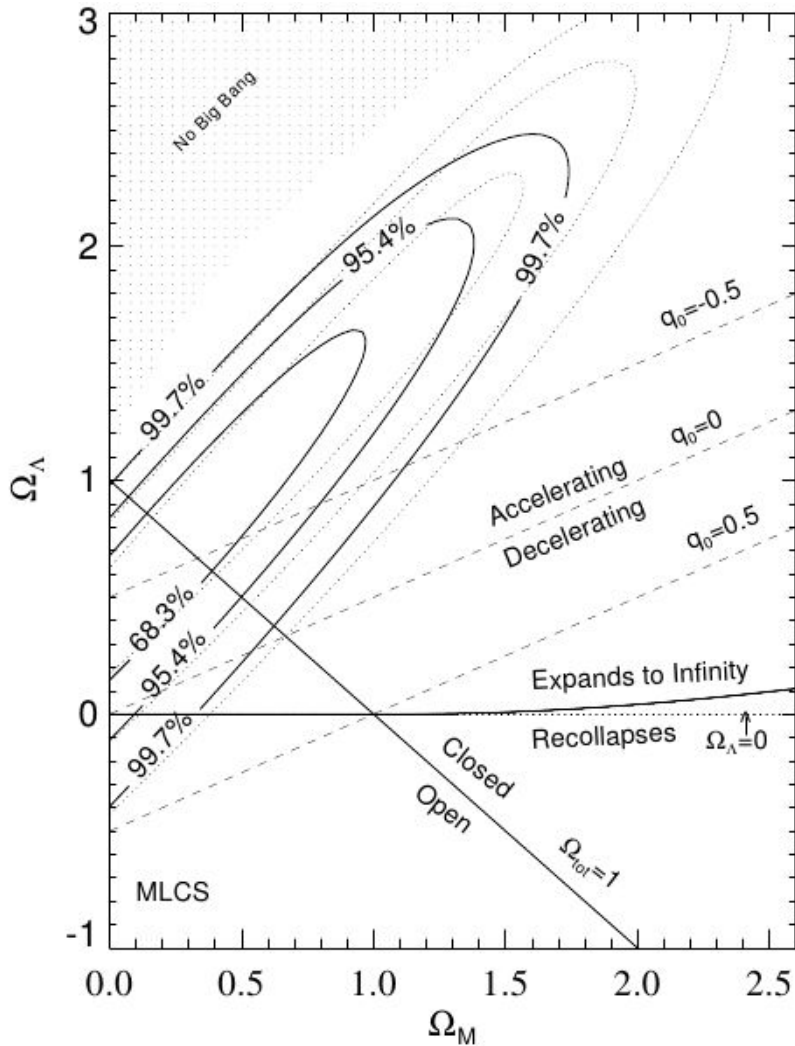
West coast

# Expansion history

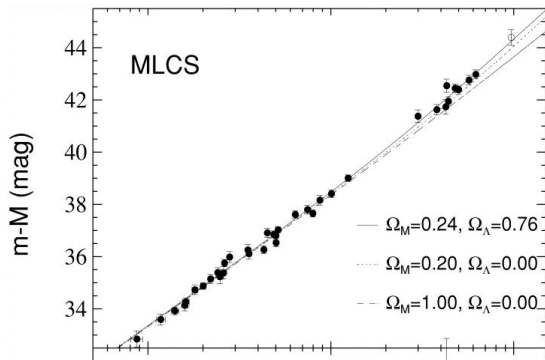


# Evidence from “repulsive stuff at large scales”

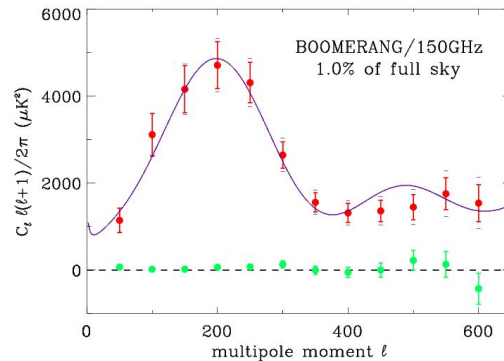
Supernova Cosmology Project  
Perlmutter *et al.* (1998)



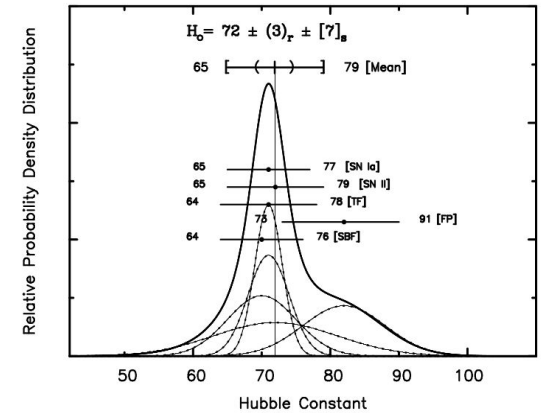
# At the turn of the century...



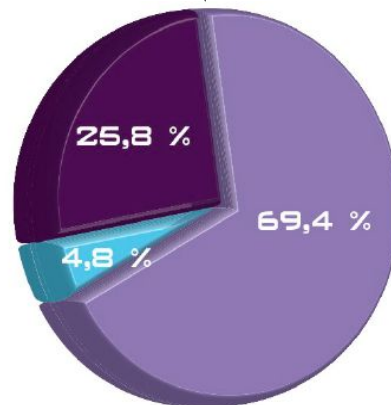
First convincing evidence for acceleration (e.g. Riess et al 1998, Perlmutter et al, 1999)



First precise measurements of CMB acoustic peak (e.g. de Bernardis et al, 2000)



First precise measurement of  $H_0$  (Freedman et al, 2000)



An accelerated Euclidian Universe, dominated by Dark Energy ( $\Lambda$ ) and by Cold Dark Matter



# Nature of Dark Energy ?

- **Cosmological constant ? Fluid of unknown nature ?**

- Measure its equation of state !  $w = \frac{p}{\rho}$
- With potentially

$$\Lambda \Rightarrow w = -1$$

$$w(a) = w_p + w_a(a_p - a)$$

- **Something wrong with GR at cosmological scales ?**

- Then expect a different phenomenology
- E.g. growth of structure should be different
- -> precision test of GR at cosmological scales

$$f \propto \Omega_m^\gamma$$

Growth rate

GR predicts  $\gamma \sim 0.55$

