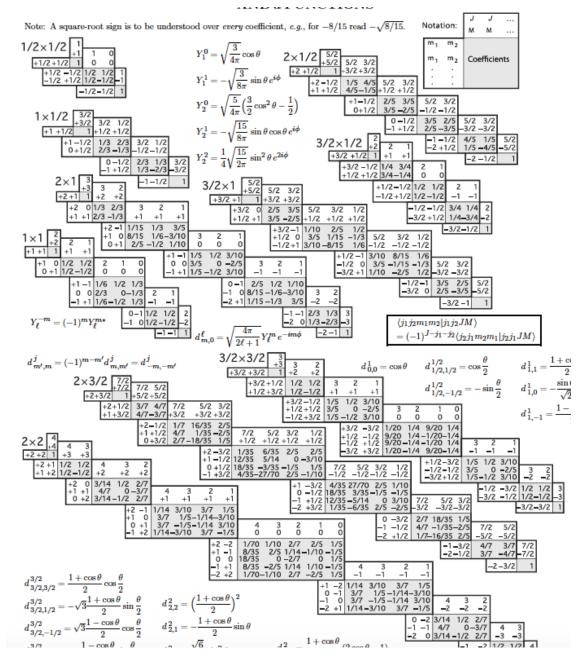
NPAC Particle Physics Course 2 – Symmetries

Eli Ben-Haïm Fabrice Couderc

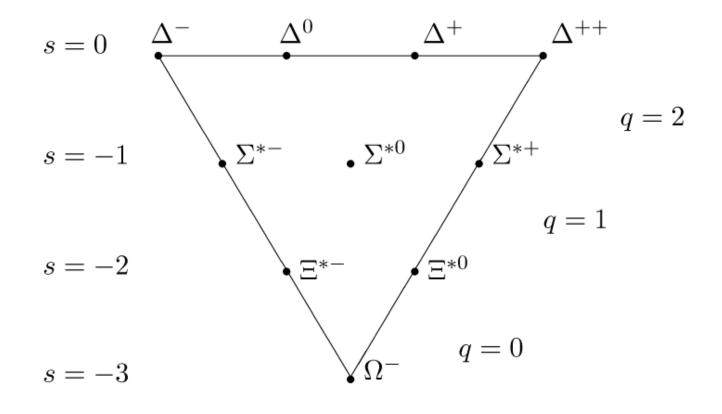
Program

- 1. Conservation laws
- 2. Spin and angular momenta
 - 2.1 Composition of angular momenta
 - 2.2 Clebsch-Gordan coefficients
 - 2.3 Helicity
- 3. Flavour symmetries
 - 3.1 Flavour SU(2) Isospin
 - 3.2 Other flavour symmetries
- 4. Discrete symmetries
 - 4.1 Parity
 - 4.2 Charge conjugation
 - 4.3 G-Parity
 - 4.4 *CP*: K⁰ mixing and *CP* violation
 - 4.5 T and CPT

Clebsch-Gordon coefficients



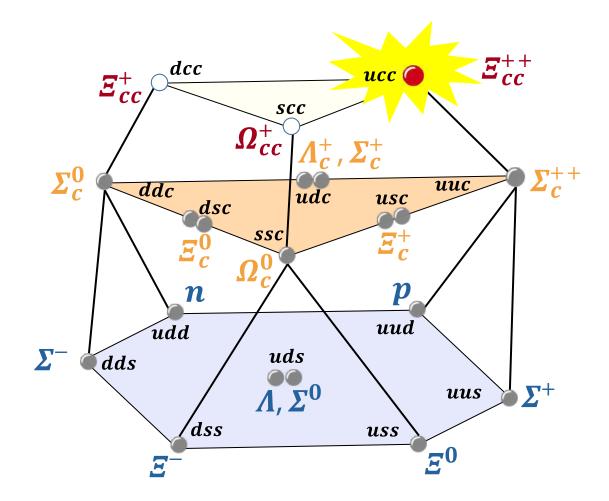
Baryon decuplet



q = -1

SU(4) 20-plet

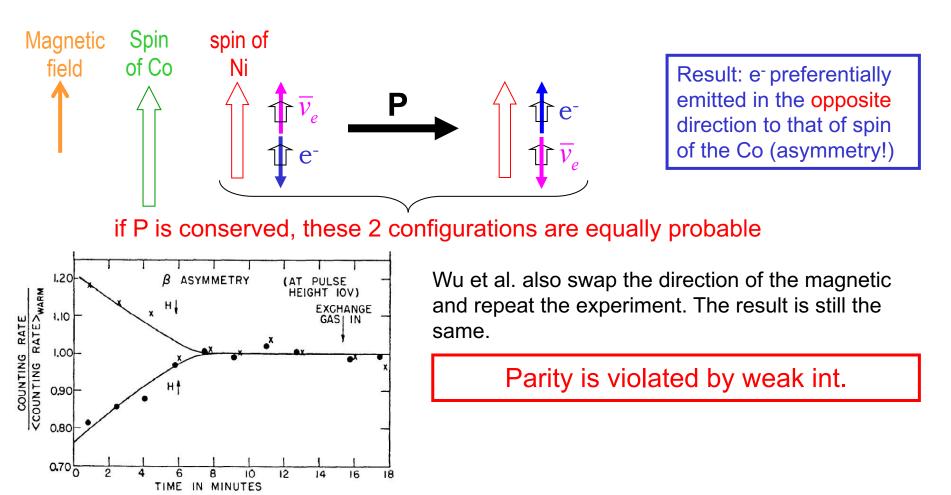
 Ξ_{cc}^{++} discovered in 2017 (LHCb at CERN), Ξ_{cc}^{++} and Ω_{cc}^{+++} still missing.



The Wu et al. experiment

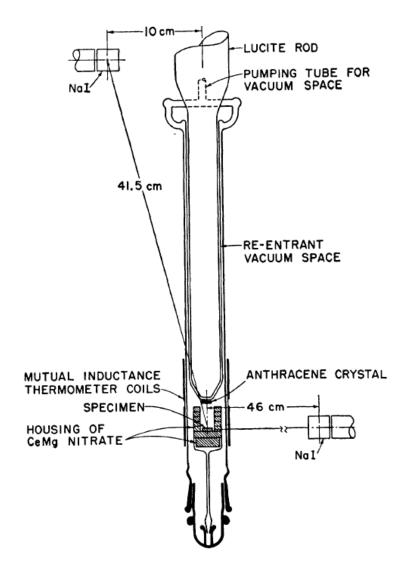
• Decay:
$$\operatorname{Co}^{60}(J=5) \to \operatorname{Ni}^{60^*}(J=4)e^-\overline{v_e}$$

- The experiment:
 - The spins of cold Co⁶⁰ atoms are aligned in a magnetic field
 - Detection of the e⁻ (knowledge of the direction of its momentum)



 $n \rightarrow p e V_{o}$

The Wu et al. experiment: scheme of apparatus



4.3 G-Parity

- It is a generalization of charge conjugation, applicable to isospin multiplets and systems of particles.
- The operator G is defined as:

$$G = C \exp(i\pi I_2)$$

charge conjugation op. 2nd isospin component

(180° rotation about the 2nd isospin axis followed by a charge conjugation).

• The G-parity (eigenvalue) of particles belonging to isospin singlets and triplets is: $\eta_G = \eta_C (-1)^I$

Eigenvalue of the charge conjugation of Isospin of the multiplet (0 or 1) the (single!) C-eigenstate of the multiplet

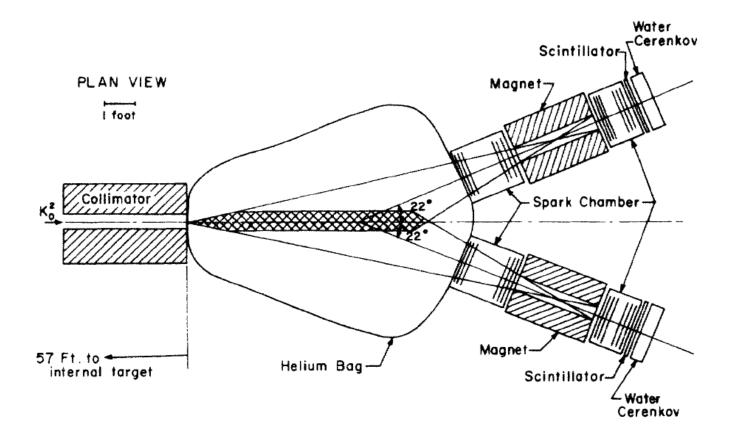
Example:
$$\eta_G(\pi^+) = \eta_C(\pi^0)(-1)^1 = (+1)(-1) = -1$$

(confirm with the PDG)

- G-parity is a multiplicative quantum number.
- Strong interaction conserves both C and the isospin.
 → If a process is forbidden by charge conjugation, other processes obtained by isospin rotation are also forbidden.
 Note that this is valid even though the charge conjugation is not defined for certain particles in the "isospin-rotated" process.
 - \Rightarrow G-Parity is conserved by the strong interaction
- This is an illustration of the fact that the SU(2) symmetry does not consist only in an exchange between two states. It is a symmetry with respect to rotation in the space of the two states.
- Some "non-observations" of processes are easily explainable by G-parity violation (and not in other ways).

Example: non observation of $\rho \rightarrow \pi \pi \pi$ by strong interaction.

Cronin and Fitch experiment: scheme of apparatus



Cronin and Fitch experiment: results

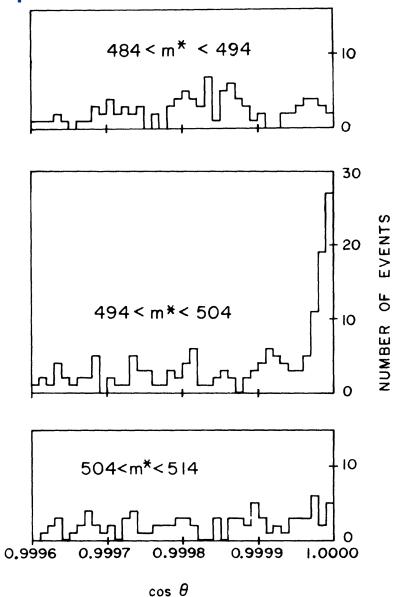


FIG. 3. Angular distribution in three mass ranges for events with $\cos\theta > 0.9995$.

