From nuclei to stars

Nucleosynthesis processes in the Universe: from Big-Bang to stars

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Outline

Lecture 1: Introduction to nuclear astrophysics

Lecture 2: Nucleosynthesis processes in the Universe

- **1**. A little bit of history
- 2. Big-Bang nucleosynthesis
- **3**. Cosmic ray nucleosynthesis
- 4. Stellar nucleosynthesis
 - Hydrogen burning: p-p chains and CNO cycles
 - Helium burning
 - Advanced burning stages: C, Ne, O and Si burning
 - Explosive nucleosynthesis
 - Nucleosynthesis beyond iron: *s* and *r*-process
- 5. Back to the Hertzsprung-Russel diagram

Lecture 3: Cross-sections and thermonuclear reaction rates

Lecture 4: Experimental approaches in nuclear astrophysics

1. A little bit of history



Important dates

- 1920 Aston: mass of the helium atom is slightly less than four times the mass of the hydrogen
- 1928 Eddington: suggests that Aston's discovery would explain the energy generation in Sun
- 1928 Gamow, Condon & Gourney: 1st calculation of the quantum tunneling probability
- 1929 Atkinson & Houtermans: suggest that Gamow's results may explain energy generation
- 1932 Cockcroft & Walton: 1st induced nuclear reaction $^{7}Li(p,\alpha)\alpha \rightarrow pp$ chain
- 1934 Lauritsen & Crane: 10 min radioactivity produced ${}^{12}C(p,\gamma){}^{13}N \rightarrow CNO$ cycle
- 1936 Atkinson, Bethe & Critchfield: p+p reactions give correct energy generation in Sun
- 1936 von Weizsaker & Bethe: energy generation in stars produced via the CNO cycle
- 1957 Burbridge, Burbridge, Fowler & Hoyle Overview of nucleosynthesis processes
- 1957 Cameron
- $1968 1^{st}$ detection of neutrinos emitted by the Sun core
- 1969 1st detection of ^{26}Al $\gamma\text{-ray}$ decay in the Milky Way
- 1987 γ -ray detection of ^{56}Co and ^{57}Co decays in supernova SN 1987A
- 2013 observational evidences of heavy nuclei nucleosynthesis in the coalescence of a binary system of two neutron stars (GRB 130603B)
- 2017 Observational confirmation of heavy nuclei nucleosynthesis in a binary neutron star merger (GW 170817)

Primordial nucleosynthesis





Alpher

Bethe Gamow ("αβγ")

« All the elements were formed just after Big-Bang »

Phys. Rev. 73. (1948) 803

Almost true for D, He and a part of ^{7}Li BUT no stable isotopes with A = 5 and A = 8 (mass gap)

Stellar nucleosynthesis



Burbridge Burbridge Fowler Hoyle (B²FH)



REVIEWS OF MODERN PHYSICS

VOLUME 29, NUMBER 4

October, 1957

Synthesis of the Elements in Stars*

E. MARGARET BURBIDGE, G. R. BURBIDGE, WILLIAM A. FOWLER, AND F. HOYLE

Kellogg Radiation Laboratory, California Institute of Technology, and Mount Wilson and Palomar Observatories, Carnegie Institution of Washington, California Institute of Technology, Pasadena, California

« All elements are synthesized in stars through various processes » Rev. Mod. Phys. 29 (1957) 547

Two views....

B²FH heritage

Identified nucleosynthesis processes

- Primordial (Big-Bang) nucleosynthesis
- Hydrogen and Helium burning
- "e" process (iron peak)
- "x" process (LiBeB; "x" for unknown)
- "r" process (rapid neutron capture)
- "s" process (slow neutron capture)
- "p" process (proton rich)

Today

- "x" is identified as non-thermal nucleosynthesis (cosmic rays)
- Additional burning stages identified: C, Ne, O, Si

2. Big Bang nucleosynthesis



Observational pillars for Big-Bang model

• The expansion of the Universe

Galaxies move away from each other and from us according to Hubble's law: $V = H_0 \times D$, where $H_0 \approx 70$ km/s/pc is the Hubble "constant"

- The Cosmic Microwave Background radiation (CMB)
 Black body radiation at 2.7 K corresponding to the redshifted spectrum emitted when the Universe became transparent (Penzias & Wilson, 1965)
- Primordial nucleosynthesis (BBN) of light elements
 BBN reproduces the observed primordial abundances over a range of nine orders of magnitudes!

• For T > 10 GK, the energy density is dominated by radiation (photons and neutrinos), and all weak, strong and electromagnetic processes established a thermal equilibrium

Nucleosynthesis (1)

• $n \leftrightarrow p$ equilibrium driven by weak interactions:

(1):
$$v_e + n \leftrightarrow e^- + p$$
 (2): $\overline{v}_e + p \leftrightarrow e^+ + n$ (3): $n \leftrightarrow p + e^- + \overline{v}_e$
$$\boxed{\frac{N_n}{N_p} = e^{-Q_{np}/kT}} \qquad Q_{np} = 1.29 MeV$$

• Equilibrium as long as the weak reaction rate [(1) + (2)] are faster than the expansion rate, hence breaks out when:

$$\Gamma_{n \leftrightarrow p} \sim H(t)$$

• Decoupling and freezeout $t \approx 10$ s after Big-Bang when $T \approx 3$ GK and $N_n/N_p \approx 1/6$

• After freezeout the dominant weak interaction is the decay of free neutrons to protons

Nucleosynthesis (2)

$$n \rightarrow p + e^{-} + \overline{v}_{e}$$

• Neutrons decay until *T* is low enough so that:

 $n + p \rightarrow D + \gamma$

becomes faster than deuterium photodisintegration

 $\gamma + D \rightarrow n + p$

- This occurs at $t \approx 200$ s (3 min) when $T \approx 0.9$ GK and $N_p/N_p \approx 1/7$
- Nucleosynthesis starts to produce essentially ⁴He together with traces of D, ³He, ⁷Li, ...

 $N_n/N_p \approx 1/7 = 2/14 \rightarrow X(^4\text{He}) \approx 4 / (4 + 12) \approx 0.25$

The canonical BBN reaction network

- Standard BBN: no convection, no mixing, no diffusion, known physics
- The 12 reactions of standard BBN:

$$rac{1}{1} \quad n \leftrightarrow p \text{ and } \tau_n = 880 \text{ (4) s}$$

$$\left\{ \bullet \ p+n \rightarrow D+\gamma \right.$$

- $D + p \rightarrow {}^{3}He + \gamma$
- $D + D \rightarrow {}^{3}He + n$
- $D + D \rightarrow T + p$
- $T + D \rightarrow {}^{4}He + n$
- $T + {}^{4}He \rightarrow {}^{7}Li + \gamma$
- $^{3}He + n \rightarrow p + T$
- ${}^{3}\text{He} + D \rightarrow p + {}^{4}\text{He}$
- ${}^{3}He + {}^{4}He \rightarrow {}^{7}Be + \gamma$
- $^{7}Li + p \rightarrow {}^{4}He + {}^{4}He$
- $^{7}Be + n \rightarrow ^{7}Li + p$

Number of baryons per photon: $\eta \equiv n_{b}/n_{\gamma}$

Baryonic density of the Universe: $\Omega_{h}h^{2} = 3.65 \times 10^{7} \eta$



experiments

Predictions vs observations

Observations from a set of primitive objects when the Universe was young

- D observations: in remote cosmological clouds (i.e. at high redshift) on the line of sight of quasars $D/H = (2.527 \pm 0.030) \times 10^{-5}$
- ⁴He observations: in H II (ionized H) regions of blue compact galaxies
 ⁴He/H = 0.2449 ± 0.0040
- ³He observations: in HII regions of *our* Galaxy ³He/H = $(1.1 \pm 0.2)x10^{-5}$
- ⁷Li observations: at the surface of low metallicity stars in the halo of our Galaxy

 $^{7}\text{Li/H} = 1.58^{+0.35}_{-0.28} \text{ x10}^{-10}$



Solutions to the ⁷Li problem?

Several possibilities are considered

- Astrophysical solution
- Nuclear physics solution
- Physics beyond the standard model

Primordial ⁷Li abundance measured in old metal poor halo dwarf stars

⁷Li abundances

Spite plateau (Spite & Spite, 1982)

- Li/H ≈ 1.12 x 10⁻¹⁰
- Very low dispersion

Spite plateau indicates that the bulk of the lithium is unrelated to galactic nucleosynthesis processes and thus is primordial



[Fe/H]

How reliable is Li abundance determination?

Li/H

 \rightarrow Systematic errors in the extraction of Li abundances due to the used atmosphere models?

 \rightarrow **unlikely** Asplund and Lind 2010

⁷Li stellar destruction?

Could atmospheric ⁷Li be depleted by rotationally induced mixing and/or diffusion?

- Lithium easily burned in stars (low binding energy)
 - → 7 Li(p, α) α for *T* > 2.5 MK
- Convection brings surface material to deeper layers
 - → lithium burning



Not enough and not uniform ⁷Li destruction

- Metal poor halo stars have shallower convective zones than in solar metallicity stars
- Stars of different masses have different convective zone size
 - → larger scatter around ⁷Li plateau should be observed

Nuclear solution to 7Li problem?

• ⁷Li produced by ⁷Be decay (EC) at high $\Omega_b h^2$

Any additional ⁷Be destruction would alleviate the ⁷Li problem

10

⁴He

ЗH

6

9

8

5

³Не

 ^{2}H

n

4

3

2

1

 ^{1}H

⁷Be

11

12

⁷Li

- Main ⁷Be production mechanism: ${}^{3}He({}^{4}He,\gamma){}^{7}Be$
 - → Various measurements of the cross-section 10% uncertainty
- Main ⁷Be destruction mechanism: ⁷Be(n,p)⁷Li(p, α) α
 - → ⁷Be(n,p)⁷Li well known cross-section 1% uncertainty
 - → $^{7}Li(p,\alpha)\alpha$ 6% uncertainty on cross-section
- Secondary destruction mechanisms
 ⁷Be+d, ⁷Be+³He, ⁷Be+⁴He....
 → all experimentally studied, and

 \rightarrow all experimentally studied, and none can alleviate the ⁷Li problem

Nuclear physics is very unlikely to solve the ⁷Li problem



Physics beyond the standard model?

Idea: late time neutron injection

- enhance ⁷Be destruction by ⁷Be(n,p)⁷Li(p, α) α reactions
- Alleviate the Li problem at the expense (harmless) Deuterium overproduction

Two examples among many....

 Decays of heavier meta-stable (100 – 1000 s) particles that inject additional neutrons

(Jedamzik (2004, 2006), Kawasaki+ (2005), Ellis+ (2005))

- Existence of a mirror universe in which neutrons can oscillate to our world (Coc+ 2013)
 - \rightarrow effective late time neutron injection



Summary

- Big-Bang Nucleosynthesis (BBN) produces, between 3 min and 20 min, H, D, He and part of Li
- Heavier elements nucleosynthesis is prevented because:
 - Larger Coulomb barriers for elements with higher atomic numbers (see next Lecture)
 - Lack of isotope of mass number A = 5 and A = 8
 - Decreasing matter density as the Universe expands

Further reading...

- C. Pitrou, A. Coc, P. Uzan & E. Vangioni, *Physics Reports* (2018)
- NPAC, cosmology course

3. Cosmic rays nucleosynthesis



Hess (center) lands after his balloon flight in 1912



Ionization as a funtion of altitude (Hess)



What is the origin of LiBeB isotopes?

What are the processes producing ^{6,7}Li, ⁹Be and ^{10,11}B?

- Big-Bang Nucleosynthesis
 - significant amount of ⁷Li
 - ⁶Li, ⁹Be and ^{10,11}B abundances predicted from BBN are at least 3 orders of magnitude below the abundances measured in metal-poor stars
- Stellar nucleosynthesis
 - Light elements are fragile enough (relatively low binding energy per nucleon) to be destroyed in stars during quiescent burning
 - ⁷Li in classical novae (explosive), AGB (?)
 - 7 Li, 11 B by v-induced spallation reactions
- Galactic Cosmic Rays (GCR)
 - Similar abundances than solar system with notable exception for LiBeB!!



20/76

Cosmic rays properties

Composition: H (90 %), He (9 %), C, N, O, e- (1 %)

Cosmic rays are not in thermodynamic equilibrium \rightarrow power law spectrum



Data from *Voyager 1* probe (red circles), AMS-02 experiment (blue stars) and HEAO-3-C2 (green squares)

Spallogenic nucleosynthesis

Non thermal nucleosynthesis induced by cosmic rays

Spallation: "heavy" nucleus (C, N, O, ...) emits lighter fragments (Li, Be, B, ...) as a result of a collision with a high-energy particle (H, He)



Inverse spallation: heavy nucleus impinges light nucleus



LiBeB emitted at about same energy per nucleon as incident C, N, O, … → must slow down to rest (small survival probability)

Spallation cross-sections



- The decreasing sequence of B, Li and Be matches the B, Li and Be GCR abundances
- $\alpha + \alpha$ reactions important for production of ^{6,7}Li isotopes

Summary

Galactic Cosmic Rays play a major role in the production of the LiBeB elements

| | BBN | GCR | v in core- collapse supernovae | Low-mass stars |
|-----------------|------|-------|--------------------------------------|-------------------|
| ⁶ Li | | 100 % | | |
| ⁷ Li | 12 % | 18 % | < 20 % | 50 – 70 % |
| ⁰Be | | 100 % | | |
| ¹⁰ B | | 100 % | | |
| ¹¹ B | | 70 % | 30 % | |

Further reading...

- V. Tatischeff & S. Gabici, Annual Reviews (2018)
- N. Prantzos, Astronomy & Astrophysics 542, A67 (2012)

4. Stellar nucleosynthesis

Quiescent (hydrostatic) stellar burning



Sun, Solar Dynamics Observatory

Explosive stellar burning



Classical nova, Nova Cygni 1992, HST

4.1 Quiescent hydrogen burning

- Where does it take place?
 - Core of main-sequence stars (8 55 MK)
 - Core of the Sun (15.6 MK)
 - Burning shell in AGB stars (45 100 MK)
- How does it work?

•
$$4p \rightarrow {}^{4}\text{He} + 2e^{+} + 2\nu_{e}$$
 $(Q = 26.73 \text{ MeV})$
 \downarrow
ashes
 \downarrow
energy source

- Probability for the simultaneous interaction of 4 protons far too small → reactions sequence
- Who & when?
 - Bethe & Critchfield (1938)
 - von Weizsaecker (1938)
 - Bethe (1939)

pp chain

CNO cycle



Hans Bethe (1906 - 2005)

Hydrogen burning

The proton – proton (pp) chains



Note: neutrinos provide direct evidence that nuclear reactions occur (see later)

Hydrogen burning

The pp1 chain (1)

- Succession of 3 reactions producing almost 90 % of Sun's energy
- First reaction: $p + p \rightarrow d + e^+ + v$ (Q = 1.44 MeV)
 - → strong + weak interactions
 - \rightarrow cross-section is about 20 orders of magnitude smaller than for nuclear (strong) interaction!!
 - \rightarrow cannot be measured
 - \rightarrow can be calculated



- All subsequent reactions involve nuclear and electromagnetic interactions
 → much faster
- Second reaction: $p + d \rightarrow {}^{3}He + \gamma$ (Q = 5.49 MeV)

 \rightarrow many measurements since 1962, including one at LUNA in 2002 (see lecture 4)

The pp1 chain (2)

- Deuterium abundance in the core of the Sun
 - Temporal evolution of deuterium = $production [p(p,e^+v)d]$
 - destruction [d(p, γ)³He]

$$\frac{dN_d}{dt} = \frac{N_H^2}{2} \left\langle \sigma v \right\rangle_{p(p,e^+\nu)} - N_H N_d \left\langle \sigma v \right\rangle_{d(p,\gamma)}$$

• At equilibium:

$$\left(\frac{N_d}{N_H}\right)_e = \frac{\langle \sigma v \rangle_{p(p,e^+\nu)}}{2 \langle \sigma v \rangle_{d(p,\gamma)}}$$

For
$$T = 15.6$$
 MK (Sun)
 $\langle \sigma v \rangle_{p(p,e^+\nu)} = 1.5 \times 10^{-43} \text{cm}^3 \text{s}^{-1}$
 $\langle \sigma v \rangle_{d(p,\gamma)} = 2.0 \times 10^{-26} \text{cm}^3 \text{s}^{-1}$
 $\left(\frac{N_d}{N_H} \right)_e = 7.5 \times 10^{-18}$
Solar D/H $\approx 2 \times 10^{-5}$
 \rightarrow D from BBN

• Lifetime of a proton and a deuterium in the core of the Sun we consider $\rho_c = 150 \text{ g cm}^{-3}$ and $X_H \sim X_{He} \sim 0.5 \rightarrow N_H = 4.5 \ 10^{25} \text{ cm}^{-3}$ $\tau_H = \frac{1}{N_H \langle \sigma v \rangle_{p(p,e^+\nu)}} = 4.7 \times 10^9 \text{ yr}$ $\tau_d = \frac{1}{N_H \langle \sigma v \rangle_{d(p,\gamma)}} = 1.1 \text{ s}$

Hydrogen burning

The pp1 chain (3)

Possible reactions for ³He burning pp1 chain ⁸B p(p,e⁺v)d S(0) Reaction Q (MeV) (keV b) $d(p,\gamma)^{3}He$ ³He(³He,2p)⁴He ⁷Be ⁸Be 16.39 ~0.3 ³He(d,γ)⁵Li(p)⁴He 6240 ³He(d,p)⁴He 18.35 ⁶Li ⁷Li ~0.8 3 He(3 He, γ) 6 Be(2p) 4 He 11.50 ³He ⁴He 5320 (80) ³He(³He,2p)⁴He 12.86 ³He(⁴He,γ)⁷Be 1.59 0.57 (4) ЗН ^{1}H

- ${}^{3}\text{He} + p \rightarrow {}^{4}\text{Li} \rightarrow {}^{3}\text{He} + p$ ($\tau = 10^{-22} \text{ s}$)
- ³He + d negligible given the low deuterium abundance
- ${}^{3}\text{He} + {}^{3}\text{He} \rightarrow 2p + {}^{4}\text{He} (Q = 12.86 \text{ MeV}) \rightarrow \text{Third reaction of the pp1 chain}$
 - \rightarrow has been measured in LUNA (see lecture 4)
- If N(⁴He) >> N(³He) [factor > 10⁴] then ³He(⁴He, γ)⁷Be is activated
 - \rightarrow pp2 & pp3 chains

Hydrogen burning

The pp2 and pp3 chains

⁷Be destruction: competition between electronic capture (EC) and proton capture





- ⁷Be decays by EC and its lifetime depends on its charge state
- In stars, ⁷Be fully ionized and then capture free electrons, so τ depends on n_e and T. In the Sun's core $\tau_s = 1.6 \tau_{lab} = 120$ days



• The ⁷Be(p, γ)⁸B reaction is faster than ⁷Be EC for *T* > 25 MK \rightarrow pp3 chain

Relative contribution of the 3 pp chains



The pp chains in the Sun



The effective energy given to the Sun is smaller than Q = 26.73 MeV because of the escape of the neutrinos

$$pp2 \quad Q_{eff} = Q - \overline{E}_{\nu}(p+p) - \overline{E}_{\nu}(^{7}Be) = 25.61 \text{ MeV}$$

$$pp1 \quad Q_{eff} = Q - 2\overline{E}_{\nu}(p+p) = 26.20 \text{ MeV} \quad pp3 \quad Q_{eff} = Q - \overline{E}_{\nu}(p+p) - \overline{E}_{\nu}(^{8}B) = 19.67 \text{ MeV}$$

Hydrogen burning

The CNO cycle (1)

 In population I stars (second, third... generation of stars), the elements C, N and O serve as catalysts of the transformation:

 $4p \to {}^{4}\text{He} + 2e^{+} + 2\nu_{e} \quad (Q = 26.73 \text{ MeV})$

 There are four sets of reactions converting H to He → 4 CNO cycles
 → we will focus on the CNO-1 cycle





 $T_{1/2}(^{13}N) = 9.965 \text{ min}$ $T_{1/2}(^{15}O) = 122.24 \text{ s}$ $T_{1/2}(^{17}F) = 64.49 \text{ s}$ $T_{1/2}(^{18}F) = 109.77 \text{ min}$

The CNO cycle (2)

- The slowest reaction ¹⁴N(p,γ)¹⁵O of the CNO cycle fixes:
 - the energy production rate $\epsilon \propto Q_{CNO}/\tau_{CNO}$
 - the cycle duration
 - $\tau_{CNO} = \tau_p(^{12}C) + \tau_p(^{13}C) + \tau_p(^{14}N) + \tau_p(^{15}N)$ $\cong \tau_p(^{14}N)$
 - For $\rho_c = 100 \text{ g.cm}^{-3}$, $X_H = 0.5 \text{ and } T_c = 60 \text{ MK}$ $\rightarrow \tau(^{12}\text{C}) = 6.1 \times 10^9 \text{ yr}$, $\tau(^{13}\text{C}) = 1.1 \times 10^9 \text{ yr}$, $\tau(^{14}\text{N}) = 2.1 \times 10^{12} \text{ yr}$, $\tau(^{15}\text{N}) = 1.0 \times 10^8 \text{ yr}$



- The ${}^{14}N(p,\gamma){}^{15}O$ reaction has been measured directly by the LUNA collaboration (see lecture 4)
 - \rightarrow impact on the age of Globular Clusters (turn-off age; see lecture 1)

(Imbriani+, A&A, 2013)

• CNO cycle in AGB stars is the main source of ¹³C and ¹⁴N in the Universe

Hydrogen burning

The CNO cycle (3)



- CNO cycle has a steeper temperature dependence than pp chain (see lecture 3)
- pp1 chain dominates in low mass stars (~ M_{\odot}), while CNO cycles dominates for higher mass stars (few M_{\odot})
- Above T = 20 MK, CNO1 faster than pp1

→ change in stellar structure at 1.15 M_{\odot} , e.g. different radiative / convective zones


The solar neutrino spectrum



The detection of solar neutrinos (1)

The pioneering experiment (1964-2001) of R. Davis (Nobel price in 2002) and J. Bahcall

- 680 tons of perchloroethylene (C₂Cl₄) in the Homestake gold mine (1.5 km deep)
- v_e + ³⁷Cl \rightarrow ³⁷Ar ($T_{1/2}$ = 35 days) + e⁻
- Production of ³⁷Ar: ~0.5 atom per day
- Radiochemical separation: extraction of the ³⁷Ar nuclei every 100 days, counting (EC → Auger electrons) in a gas detector
- Result: 2.56 ± 0.16 (stat) ± 0.16 (sys) SNU
 → 30 % of the expected signal
- Solar model (Bahcall 2004): 8.5 ± 0.18 SNU



1 SNU (Solor Neutrino Unit) = 10⁻³⁶ capture per second and target atom

The detection of solar neutrinos (2)

- Radiochemical experiments with gallium: SAGE and GALLEX
 - Reaction: $v_e + {^{71}Ga} \rightarrow {^{71}Ge} (T_{1/2} = 11.4 \text{ d}) + e^- (\text{threshold } E_v = 0.23 \text{ MeV})$
 - \rightarrow sensitive to pp neutrinos
 - Results: 40 % of the expected signal
- Real-time detection of (mostly) e- neutrinos: Kamiokande (700 tons of water, 1983 – 1996), Super-Kamiokande (50 kt, 1996 –)
 - Reaction: $v_e + e^- \rightarrow v_e + e^-$ (emission of Cherenkov light)
 - Results: 40 % of the expected signal





Solution to the solar neutrino problem

Possible origin of the deficit

- Problem with the standard solar model? (3% of error on $T_c \rightarrow a$ factor of 2 in N_v)
- Problem with the nuclear data? $^{7}Be(p,\gamma)^{8}B$ cross-section
- New physics of neutrino \rightarrow oscillation $\nu_e \rightarrow \nu_{\mu}, \nu_{\tau}$?

SNO: Sudbury Neutrino Observatory

- 1100 tons of D₂O (99.9%)
- Sensitive to the three neutrino flavors

 $\rightarrow v_x + d \rightarrow p + n + v_x$ (neutral current)

(Bellerive+, NPB, 2016)



• Results: $\phi_{NC} = 5.21 \pm 0.27$ (stat) ± 0.39 (sys) SNU in agreement with $\phi_{SSM} = 5.05^{+1.01}_{-0.81}$ SNU



4.2 Quiescent helium burning

- Where does it take place?
 - Core of horizontal branch stars (100 400 MK)
 - Burning shell in AGB stars (45 100 MK)
- Main nucleosynthesis products

 ^4He transformed in ^{12}C and ^{16}O for stars of more than $\sim 0.5~\text{M}_\odot$

• How does it work?

Mainly three reactions:

- $\alpha + \alpha + \alpha \rightarrow {}^{12}C \qquad Q = 7.3 \text{ MeV}$
- ${}^{12}C(\alpha,\gamma){}^{16}O$ Q = 7.2 MeV
- ${}^{16}O(\alpha,\gamma){}^{20}Ne$ Q = 4.7 MeV



Fred Hoyle (1915 - 2001)

- Who & when?
 - Triple alpha process: Öpik (1951), Salpeter (1952)
 - The "Hoyle" state in ¹²C: Hoyle (1953)

The triple alpha process

How are synthesized elements heavier than ⁴He, given that there are no stable isotopes for mass A = 5 (p+ α) and A = 8 (α + α)?



• Experimental verification in 1953 and 1957

Helium burning

Slow and crucial reaction \rightarrow Holy Grail in nuclear astrophysics

The ${}^{12}C(\alpha,\gamma){}^{16}O$ reaction

- The rate of this reaction determines the ¹²C/¹⁶O ratio at the end of the helium burning phase, and thus the subsequent burning stages in massive stars
- ¹²C/¹⁶O influences the nature of the remnant (neutron star? Black hole?) left after a core-collapse supernova
- A difficult case: contribution from a broad state, two sub-threshold resonances and the direct capture process.
- Cross-section at 300 keV

→ $\sigma \approx 10^{-17}$ b! (can't be measured, less than 1 event per year)



The ¹⁶O(α,γ)²⁰Ne reaction



Helium burning

M2 NPAC 2022-2023 (Lecture 2)

How insignificant we are!



Helium burning

M2 NPAC 2022-2023 (Lecture 2)

Other reactions

 ¹⁴N is the main "ash" from the CNO cycle, and accounts for 1-2% of the mass of the fusion core at the end of H burning (pop I stars)

 \rightarrow ¹⁴N(α , γ)¹⁸F(β ⁺ ν)¹⁸O(α , γ)²²Ne

followed by

→ $^{22}Ne(\alpha,\mathbf{n})^{25}Mg$ [= main source of neutrons of the weak s-process ("slow" neutron capture)]

⁴He





4.3 Advanced nuclear burning phases



Schematic diagram of the "onion-skin" structure of a pre-supernova



Chandra X-ray observatory image of the SN remnant Cassiopeia A

Carbon burning

- When?
 - He exhausted in the stellar core \rightarrow mainly ^{12}C and ^{16}O ashes \rightarrow gravitational contraction \rightarrow increase of temperature
 - $T_c \sim (5-9) \times 10^8$ K and $\rho > 2 \times 10^5$ g cm⁻³ for M ≥ 8 M_{\odot}
- Major reaction sequences

| $^{12}C + ^{12}C \rightarrow ^{20}Ne + \alpha$ | (Q = 4.62 MeV) | dominates by far | |
|--|-----------------|------------------|--|
| → ²³ Na + p | (Q = 2.24 MeV) | | |
| → ²³ Mg + n | (Q = -2.62 MeV) | | |
| + several seconday reactions. | | | |

- Composition at the end of core carbon burning
 - Mainly ²⁰Ne with some ^{21,22}Ne, ²³Na, ^{24,25,26}Mg and ^{26,27}Al
 - ¹⁶O not burning yet.... \rightarrow amount comparable with ²⁰Ne

Advanced burning phases

M2 NPAC 2022-2023 (Lecture 2)

Neon burning

- When?
 - After carbon burning \rightarrow mainly ²⁰Ne ashes \rightarrow the core further contracts \rightarrow increase of temperature
 - $T_c \sim (1-2) \times 10^9$ K and $\rho \sim 10^6$ g cm⁻³ for M ≥ 11 M_{\odot}
- Major reaction sequences

Temperatures are high enough to initiate photodisintegration processes

 $\begin{array}{ccc} \gamma + {}^{20}\text{Ne} \rightarrow {}^{16}\text{O} + \alpha & (Q = -4.73 \text{ MeV}) \\ {}^{16}\text{O} + \alpha \rightarrow {}^{20}\text{Ne} + \gamma & \end{array} \begin{array}{c} \text{Equilibrium establishes} \end{array}$

followed by e.g. the ²⁰Ne(α,γ)²⁴Mg(α,γ)²⁸Si sequence

- Composition at the end of core neon burning
 - Mainly ¹⁶O with some ²⁴Mg and ²⁸Si

Oxygen burning

- When?
 - After neon burning the core further contracts
 - $T_c \sim (2-3) \times 10^9$ K and $\rho \sim 3 \ 10^6$ g cm⁻³ for M ≥ 11 M_{\odot}
- Major reaction sequences

$$\begin{array}{rl} {}^{16}\text{O} + {}^{16}\text{O} & \rightarrow \; {}^{32}\text{S}^{\star} \to \; {}^{31}\text{S} + n & (Q = 1.45 \; \text{MeV}) \\ & \rightarrow \; {}^{31}\text{P} + p & (Q = 7.68 \; \text{MeV}) \\ & \rightarrow \; {}^{30}\text{P} + d & (Q = -2.41 \; \text{MeV}) \\ & \rightarrow \; {}^{28}\text{Si} + \alpha & (Q = -2.41 \; \text{MeV}) \end{array}$$

+ recapture of n, p, d and α -particles

- Composition at the end of oxygen burning
 - The most abundant nuclides are $^{\rm 28}{\rm Si}$ and $^{\rm 32}{\rm S}$

Silicon burning

- When?
 - After oxygen burning the core further contracts and the temperature incresases
 - $T_c \sim (2.8 4.1) \times 10^9$ K and $\rho \sim 3 \ 10^7$ g cm⁻³ for M ≥ 11 M_{\odot}
- Photodisintegration
 - Starts with ²⁸Si: ²⁸Si(γ, α)²⁴Mg(γ, α)²⁰Ne(γ, α)...
 - Photodisintegration rearrangement: destruction of less tightly bound species and capture of released n, p, α -particles to synthesize more tightly bound species
- Nuclear Statistical Equilibrium (NSE) is achieved for many reactions
 - NSE = both photodisintegration and capture rates are fast

 $\gamma + (Z, N) \rightleftharpoons p + (Z - 1, N) \quad \gamma + (Z, N) \rightleftharpoons n + (Z, N - 1) \quad \gamma + (Z, N) \rightleftharpoons \alpha + (Z - 2, N - 2)$

- Equilibrium drives towards $A = 56 \rightarrow \text{most}$ stable nuclide (higher binding energy)
- Synthesis of nuclei from Si to Zn ("iron peak" elements Ti to Zn)
- Composition at the end of silicon burning: ${}^{56}Fe \rightarrow$ formation of an iron core

Advanced burning phases

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Summary

| Stellar mass (M.) | Stage reached | |
|-------------------|-------------------------|--|
| < 0.08 | no thermonuclear fusion | |
| 0.1 -0.5 | H burning | |
| 0.5 - 8 | He burning | |
| 8 - 11 | C burning | |
| > 11 | all stages | |

Evolution stages of a 25 $\rm M_{\odot}$ star

| Stage reached | Timescale | T _{core} (10 ⁹ K) | Density (g cm ⁻³) |
|-------------------|---------------------|---------------------------------------|-------------------------------|
| H burning | 7x10 ⁶ y | 0.06 | 5 |
| He burning | 5x10 ⁵ y | 0.23 | 7x10 ² |
| C/O burning | 600 y / 6 months | 0.93 - 2.3 | $2x10^{5} - 1x10^{7}$ |
| Si melting | 1 d | 4.1 | 3x10 ⁷ |
| Explosive burning | 0.1 – 1 s | 1.2 - 7 | varies |

Advanced burning phases

4.4 Explosive nucleosynthesis

Massive stars





Hubble Space Telescope Wide Field Planetary Camera 2

Binary systems



Type la supernova G299 (Chandra Xray observatory)



Classical nova

Nova Cygni 1992 (HST)

Core collapse supernova (1)

"Onion shell" structure of massive stars



Explosion:

- Core in NSE, grows in mass until ~ 1.4 M_{\odot} , electron degeneracy pressure unable to counteract gravity...
- Collapse starts, enhanced by photodisintegration (e.g. γ + ⁵⁶Fe \rightarrow 13 ⁴He + 4n) and electron capture (e⁻ + (Z,N) $\rightarrow v_e$ + (Z-1,N+1))
- When $\rho \sim 10^{14}$ g/cm³ nuclei feel short-range nuclear force \rightarrow inner part of core rebounds \rightarrow outward moving shock

Explosive nucleosynthesis: induced by neutrinos and outward moving shock (mainly in Si, O and Ne/C layers) cc Supernovae M2 NPAC 2022-2023 (Lecture 2) 54/76

Core collapse supernova (2)

Light curve powered by radioactive decay

⁴⁴Ti observations from SN remants



cc Supernovae

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Sudden increase in star's luminosity ($L \sim 10^4 - 10^6 L_i$, and $t \sim 1h - 1d$)

Classical novae (1)

Final evolution of a close binary system



| | novae | ccSN |
|--|---|--------------------|
| $M_{ej}(M_{\odot})$ | ~ 10 -5 | ~ 10 |
| f (yr ⁻¹ galaxy ⁻¹) | ~ 30 | ~ 10 ⁻² |
| L (L _o) | ~ 10⁵ | ~ 1011 |
| Nucleosynthesis | ¹³ C, ¹⁵ N, ¹⁷ O | ~ all |

- H-rich material transfer from normal star to white dwarf (WD)
- ${\it T}$ and ρ increase at surface of WD
- Start and thermonuclear runaway ($T \approx 50 300$ MK)
 - \rightarrow cataclysmic explosion
- Ejection of part of the accreted material



Shell ejection

The energy release from the β^+ -decays (¹³N, ¹⁴O, ¹⁵O, ¹⁷F) throughout the envelope helps to eject the material from the WD

Classical novae (2)



 $T_{1/2}(^{13}N) = 9.965 \text{ min}$ $T_{1/2}(^{15}O) = 122.24 \text{ s}$ $T_{1/2}(^{17}F) = 64.49 \text{ s}$ $T_{1/2}(^{18}F) = 109.77 \text{ min}$

End-point of nucleosynthesis: A ~ 40 (Ca)

- *T_{peak}* ~ 300 400 MK
- (p,γ) reactions on the proton-rich side
- Coulomb barrier too high to overcome for $A \ge 40$

Nucleosynthesis of γ -ray emitters

- ¹⁸F (T_{1/2}=110 min); 511 keV
- ²²Na (T_{1/2}=2.6 yr); 1275 keV
- ²⁶Al (T_{1/2}=0.7 Myr); 1809 keV

4.5 Nucleosynthesis beyond iron



Elements heavier than iron can't be synthesized by fusion reactions

Neutron capture reactions

- Radiative neutron captures [(n, γ) reactions] in competition with β^{-} decay
- Processus starts with Fe seeds



- Mean lifetime for neutron capture $\tau_n = \frac{1}{N_n \langle \sigma v \rangle}$ to be lifetime τ_{β} (from seconds to years)
 - $\frac{1}{V_n \langle \sigma v \rangle}$ to be compared to β -decay
- If $\tau_n > \tau_\beta \rightarrow$ unstable nuclide decays if $\tau_n < \tau_\beta \rightarrow$ neutron capture

s-process: "slow" *r*-process: "rapid"

s-process

- Slow neutron capture process
 - Unstable nucleus decays before capturing another neutron
 - $\tau_n >> \tau_\beta \quad \Leftrightarrow \quad N_n \sim 10^8 \text{ n/cm}^3$



- Nucleosynthesis: path along the valley of $\beta^{\text{-}}$ stability up to ^{209}Bi (long time scale $\sim 10^4$ yr)
- Neutron source: ${}^{13}C(\alpha,n){}^{16}O$ and/or ${}^{22}Ne(\alpha,n){}^{25}Mg$
- Quiescent scenarios: AGB stars; main s-process; "Ba/Pb" peaks
 - Massive stars; weak s-process; "Sr-Y" peak

r-process

- Rapid neutron capture process
 - Unstable nucleus captures neutron before decaying



- Nucleosynthesis: path far from the valley of β⁻ stability (short time scale ~ seconds)
- Explosive scenarios: but where?

Astrophysical site for *r*-process?

Core-collapse Supernovae?



Supernova SN1987A

- Dynamical ejecta of prompt explosions (of O-Ne-Mg cores)
- Neutrino-driven wind from proto-neutron stars

Neutron star merger?



- Mergers are expected to eject ~ 0.01 $\rm \ M_{\odot}$ of very neutron-rich material
- Sources of gravitational waves
- Electromagnetic emission from radioactive decay of *r*-process nuclei → kilonova

Neutron star merger GW170817

Gravitational waves from neutron star merger detected by LIGO/VIRGO



Two neutron stars of 0.86 $\rm M_{\odot}and$ 2.26 $\rm M_{\odot}$

• Optical transient source counterpart SSS17a (Swope Supernova Survey)



Counterpart in galaxy NGC4993 at ~ 40 Mpc

- First day
 - \rightarrow blue and bright
- Four days later
 → red and fainter

Near-infrared emission

Comparison of the measured near-infrared spectrum counterpart of the binary neutron star merger GW170817 with a "red" kilonova model



- The two bumps in the near infrared spectrum is a signature of very heavy elements
- Effect of opacity induced by lanthanide elements
- Lanthanides (~ 1%)
 - → *r*-process

5. Back to the HR diagram



Globular cluster M10

Red giant stars (1)

- Stars of mass $0.5 10 M_{\odot}$ (if $M \ge 10 M_{\odot} \rightarrow red$ supergiants)
- Inert He core (no energy source) surrounded by a H burning shell
- From the Virial theorem $E = K + \Omega = \Omega/2 = -K$ If E ~ cst, Ω and K also

→ contraction of the core must be accompagnied by expansion of the envelope $(\Omega \sim \text{cte})$ up to 50 R_o (~ Mercury)

→ core heating must result in cooling of the envelope $(K \sim \text{cte}) \rightarrow T_{eff}$ decreases

$$\rightarrow L = 4\pi R^2 \sigma_s T_{eff}^4$$
 increases



Sun's Post-Main Sequence Evolutionary Track

Red giant stars (2)



- Decrease of $T_{eff} \rightarrow$ recombination in stellar atmosphere \rightarrow increase of opacity \rightarrow radiative transport less efficient \rightarrow convection settles in envelope
- Ashes of H-shell burning ¹³C, ¹⁴N are transported to the surface
 - → first "dredge-up"

 \rightarrow high $^{13}C/^{12}C$ and $^{14}N/^{12}C$ isotopic ratios observed in absorption spectra of red giant stars

Stars of the horizontal branch (1)

Ignition of the He core at $T_c \sim 100 \text{ MK} \rightarrow \text{core contraction stops}$

In low-mass stars (0.7 – 2 M_☉) the electron gas in the core is partially degenerated → helium flash

→ release during a few seconds of $10^{10} L_{\odot}$ in L_{nuc} ! but invisible from the surface

→ expansion and cooling of the core result in the contraction and heating of the envelope



Sun's Post-Main Sequence Evolutionary Track

Stars of the horizontal branch (2)

Ignition of the He core at $T_c \sim 100 \text{ MK} \rightarrow \text{core contraction stops}$

- Quiet ignition of the He core (convective) for intermediate-mass stars (2 – 10 $\rm M_{\odot})$



AGB stars

- Asymptotic Giant Branch (AGB); E-AGB = early AGB
 - Inert C/O core (no energy source) left after He core burning
 - He burning shell + H burning shell
 - Convective envelope → second "dredge-up" (H-burning ashes are brought to the surface by convection)
- As for red giant phase, radius is increasing..... up to 200 $\rm R_{\odot}$ (~ Earth)!



TP-AGB stars (Thermal Pulses)



Evolution of a solar-type star

| Time until the next stage (year) | <i>Т_с</i> (МК) | T _{eff} (K) | ρ _c (g cm ⁻³) | Radius (R _⊙) | Stellar stage |
|-------------------------------------|------------------------------|-------------------------|---|-----------------------------|--|
| 1010 | 15 | 6000 | 10 ² | 1 | Main sequence |
| 108 | 50 | 4000 | 104 | 3 | Subgiant |
| 105 | 100 | 4000 | 105 | 50 | Helium flash |
| 5×10 ⁷ | 200 | 5000 | 104 | 10 | Horizontal branch |
| 104 | 250 | 4000 | 105 | 200 | AGB |
| 105 | 300 | 100 000 | 107 | 0.01 | Compact star enriched in C, O (planetary nebula) |
| _ | 100 | 50 000 | 107 | 0.01 | White dwarf |
Summary

Abundance curve and processes



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Nuclear landscape and astrophysical processes



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Bibliography

- Nuclear Physics of Stars Christian Iliadis, Wiley-VCH Verlag GmbH & Co. KGaA, 2015 ISBN 978-3-527-33648-7
- An Introduction to the Theory of Stellar Structure and Evolution (Virial theorem, p26, p32, p126)
 Dina Prialnik, Cambridge University Press
 ISBN 978-0-521-65065-6