

From nuclei to stars

Nucleosynthesis processes in the Universe: from Big-Bang to stars

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Outline

Lecture 1: Introduction to nuclear astrophysics

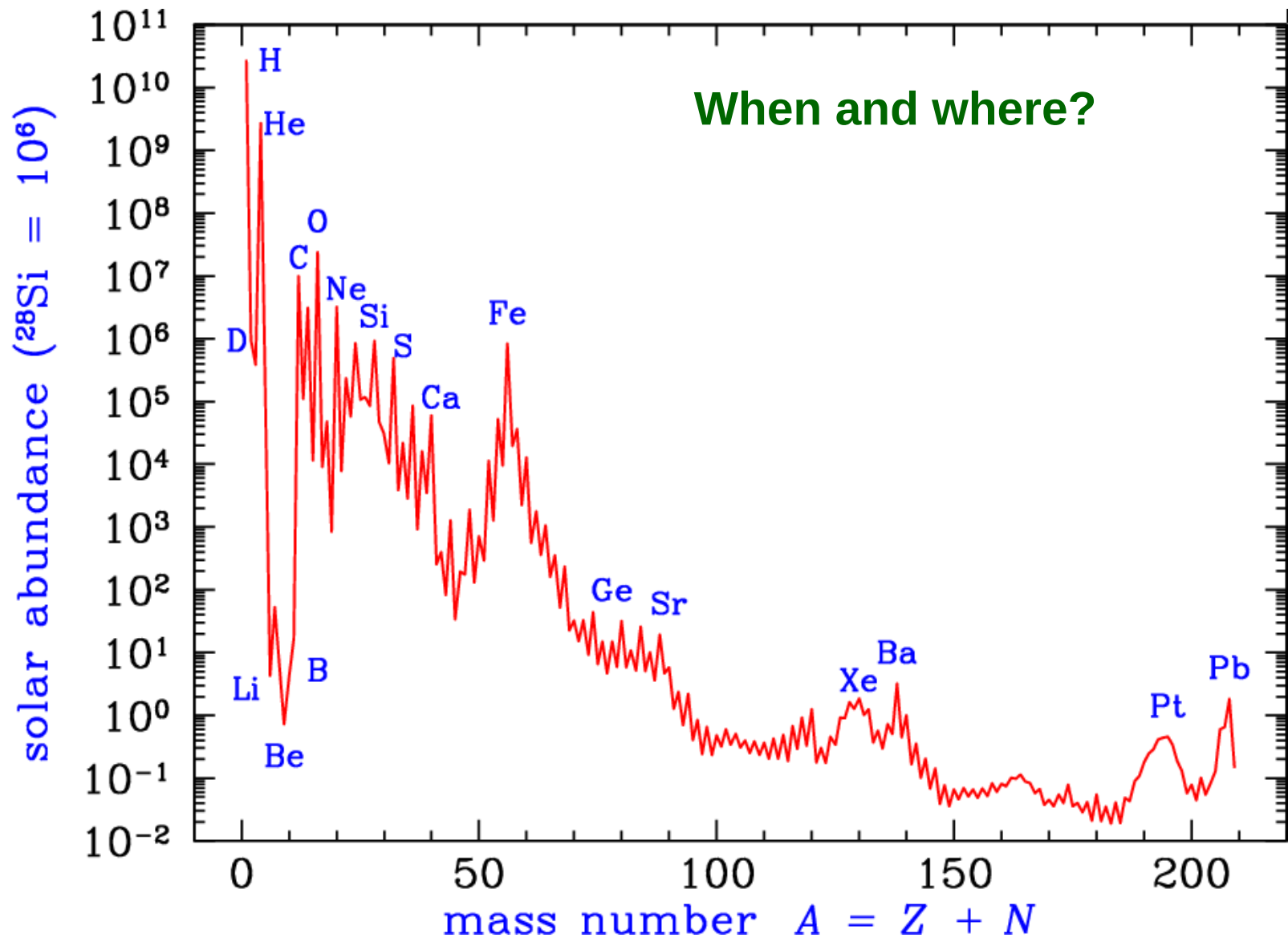
Lecture 2: Nucleosynthesis processes in the Universe

1. A little bit of history
2. Big-Bang nucleosynthesis
3. Cosmic ray nucleosynthesis
4. Stellar nucleosynthesis
 - Hydrogen burning: p-p chains and CNO cycles
 - Helium burning
 - Advanced burning stages: C, Ne, O and Si burning
 - Explosive nucleosynthesis
 - Nucleosynthesis beyond iron: s- and *r*-process
5. Back to the Hertzsprung-Russel diagram

Lecture 3: Cross-sections and thermonuclear reaction rates

Lecture 4: Experimental approaches in nuclear astrophysics

1. A little bit of history



Important dates

- 1920 – **Aston**: mass of the helium atom is slightly less than four times the mass of the hydrogen
- 1928 – **Eddington**: suggests that Aston's discovery would explain the energy generation in Sun
- 1928 – **Gamow, Condon & Gourney**: 1st calculation of the quantum tunneling probability
- 1929 – **Atkinson & Houtermans**: suggest that Gamow's results may explain energy generation

- 1932 – **Cockcroft & Walton**: 1st induced nuclear reaction ${}^7\text{Li}(p,\alpha)\alpha \rightarrow$ pp chain
- 1934 – **Lauritsen & Crane**: 10 min radioactivity produced ${}^{12}\text{C}(p,\gamma){}^{13}\text{N} \rightarrow$ CNO cycle

- 1936 – **Atkinson, Bethe & Critchfield**: p+p reactions give correct energy generation in Sun
- 1936 – **von Weizsaker & Bethe**: energy generation in stars produced via the CNO cycle

- 1957 – **Burbridge, Burbridge, Fowler & Hoyle** } **Overview of nucleosynthesis processes**
- 1957 – **Cameron** }

- 1968 – 1st detection of neutrinos emitted by the Sun core
- 1969 – 1st detection of ${}^{26}\text{Al}$ γ -ray decay in the Milky Way
- 1987 – γ -ray detection of ${}^{56}\text{Co}$ and ${}^{57}\text{Co}$ decays in supernova SN 1987A
- 2013 – observational evidences of heavy nuclei nucleosynthesis in the coalescence of a binary system of two neutron stars (GRB 130603B)
- 2017 – Observational confirmation of heavy nuclei nucleosynthesis in a binary neutron star merger (GW 170817)

Two views....

Primordial nucleosynthesis



Alpher



Bethe
("α β γ")



Gamow

« All the elements were formed
just after Big-Bang »

Phys. Rev. 73. (1948) 803

Almost true for D, He and a part of ${}^7\text{Li}$
BUT no stable isotopes with $A = 5$ and $A = 8$
(mass gap)

Stellar nucleosynthesis



Burbidge
Burbidge Fowler
(B²FH)



Hoyle



REVIEWS OF MODERN PHYSICS

VOLUME 29, NUMBER 4

OCTOBER, 1957

Synthesis of the Elements in Stars*

E. MARGARET BURBIDGE, G. R. BURBIDGE, WILLIAM A. FOWLER, AND F. HOYLE

*Kellogg Radiation Laboratory, California Institute of Technology, and
Mount Wilson and Palomar Observatories, Carnegie Institution of Washington,
California Institute of Technology, Pasadena, California*

« All elements are synthesized in stars
through various processes »

Rev. Mod. Phys. 29 (1957) 547

B²FH heritage

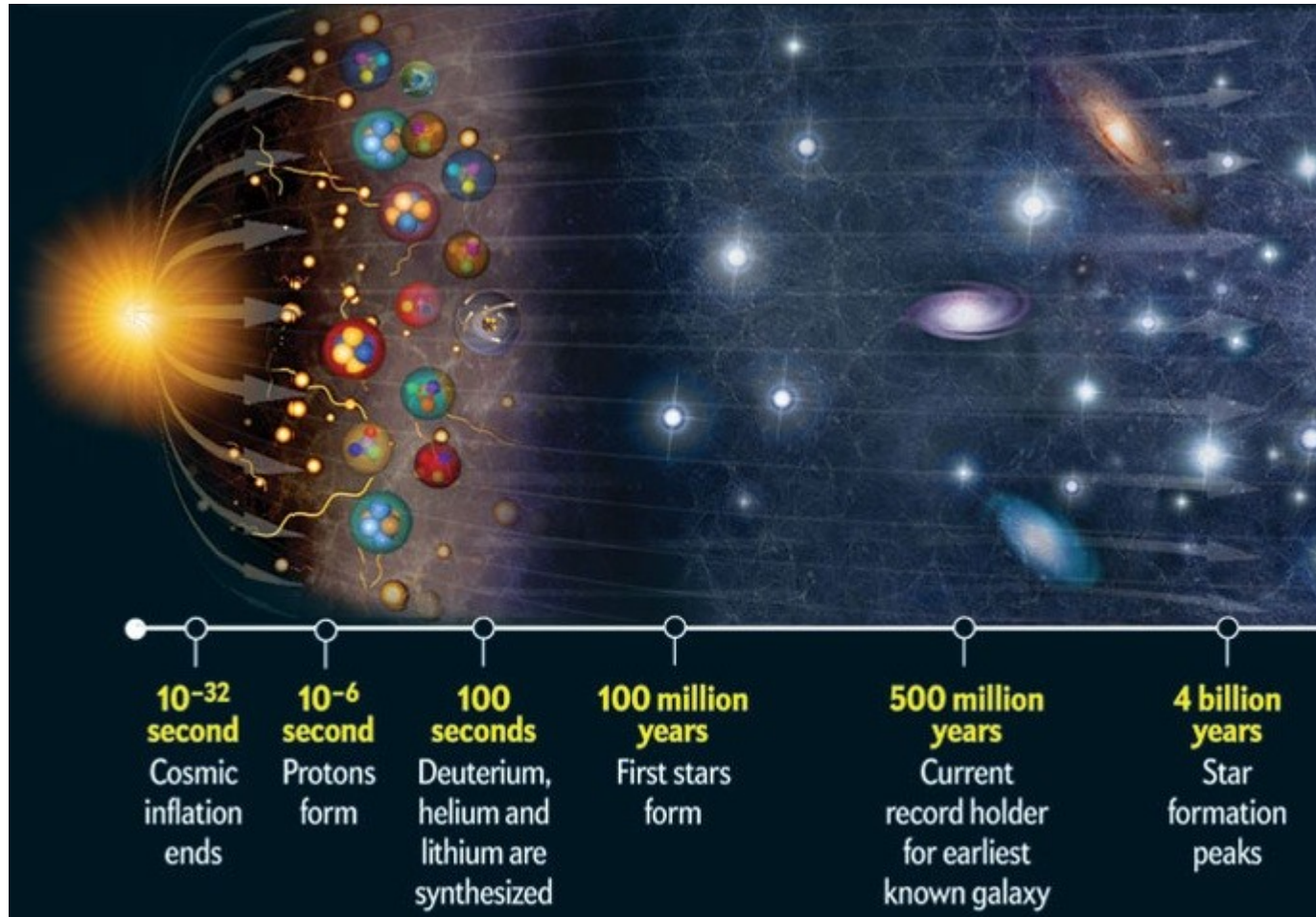
Identified nucleosynthesis processes

- Primordial (Big-Bang) nucleosynthesis
- Hydrogen and Helium burning
- “e” process (iron peak)
- “x” process (LiBeB; “x” for unknown)
- “r” process (rapid neutron capture)
- “s” process (slow neutron capture)
- “p” process (proton rich)

Today

- “x” is identified as non-thermal nucleosynthesis (cosmic rays)
- Additional burning stages identified: C, Ne, O, Si

2. Big Bang nucleosynthesis



Observational pillars for Big-Bang model

- The expansion of the Universe

Galaxies move away from each other and from us according to Hubble's law: $V = H_0 \times D$, where $H_0 \approx 70 \text{ km/s/Mpc}$ is the Hubble "constant"

- The Cosmic Microwave Background radiation (CMB)

Black body radiation at 2.7 K corresponding to the redshifted spectrum emitted when the Universe became transparent (Penzias & Wilson, 1965)

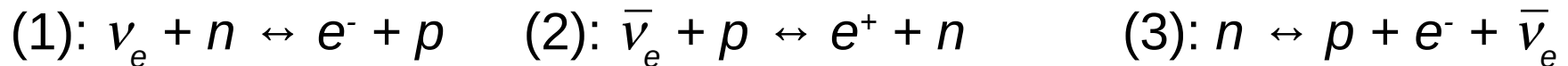
- Primordial nucleosynthesis (BBN) of light elements

BBN reproduces the observed primordial abundances over a range of nine orders of magnitudes!

Nucleosynthesis (1)

- For $T > 10$ GK, the energy density is dominated by radiation (photons and neutrinos), and all weak, strong and electromagnetic processes established a **thermal equilibrium**

- $n \leftrightarrow p$ equilibrium driven by weak interactions:



$$\frac{N_n}{N_p} = e^{-Q_{np}/kT}$$

$$Q_{np} = 1.29 \text{ MeV}$$

- **Equilibrium** as long as the weak reaction rate [(1) + (2)] are faster than the expansion rate, hence **breaks out when**:

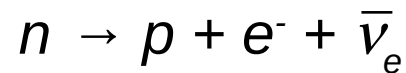
$$\Gamma_{n \leftrightarrow p} \sim H(t)$$

Γ : reaction rates

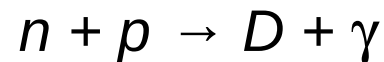
- Decoupling and freezeout $t \approx 10$ s after Big-Bang when $T \approx 3$ GK and $N_n/N_p \approx 1/6$

Nucleosynthesis (2)

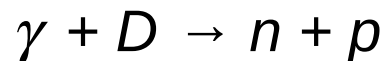
- After freezeout the dominant weak interaction is the **decay of free neutrons to protons**



- Neutrons decay until T is low enough so that:



becomes faster than deuterium photodisintegration



- This occurs at $t \approx 200$ s (3 min) when $T \approx 0.9$ GK and $N_n/N_p \approx 1/7$
- Nucleosynthesis starts to produce essentially ${}^4\text{He}$ together with traces of D, ${}^3\text{He}$, ${}^7\text{Li}$, ...

$$N_n/N_p \approx 1/7 = 2/14 \quad \rightarrow \quad X({}^4\text{He}) \approx 4 / (4 + 12) \approx 0.25$$

The canonical BBN reaction network

- Standard BBN: no convection, no mixing, no diffusion, known physics
- The 12 reactions of standard BBN:

theory

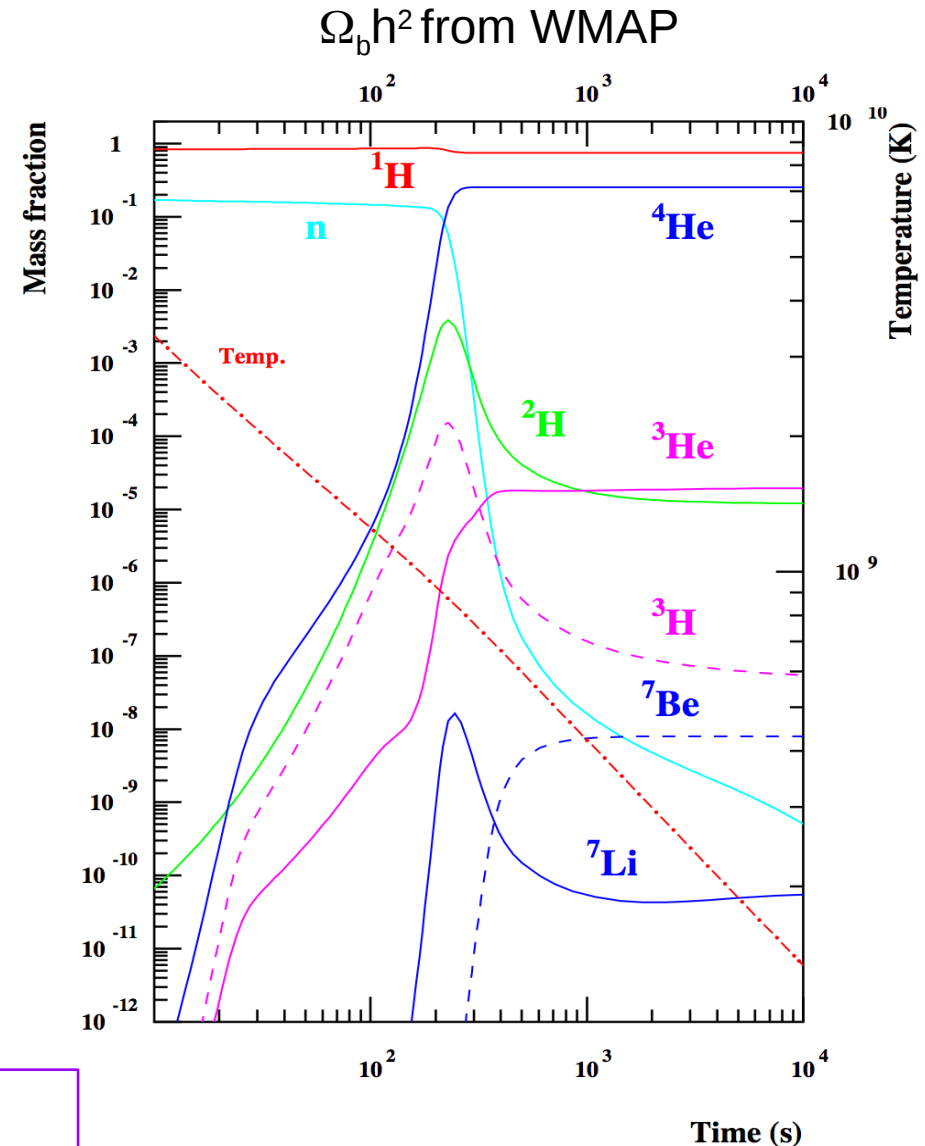
- $n \leftrightarrow p$ and $\tau_n = 880$ (4) s
- $p + n \rightarrow D + \gamma$

experiments

- $D + p \rightarrow {}^3\text{He} + \gamma$
- $D + D \rightarrow {}^3\text{He} + n$
- $D + D \rightarrow T + p$
- $T + D \rightarrow {}^4\text{He} + n$
- $T + {}^4\text{He} \rightarrow {}^7\text{Li} + \gamma$
- ${}^3\text{He} + n \rightarrow p + T$
- ${}^3\text{He} + D \rightarrow p + {}^4\text{He}$
- ${}^3\text{He} + {}^4\text{He} \rightarrow {}^7\text{Be} + \gamma$
- ${}^7\text{Li} + p \rightarrow {}^4\text{He} + {}^4\text{He}$
- ${}^7\text{Be} + n \rightarrow {}^7\text{Li} + p$

Number of baryons per photon: $\eta \equiv n_b/n_\gamma$

Baryonic density of the Universe: $\Omega_b h^2 = 3.65 \times 10^7 \eta$



Predictions vs observations

Observations from a set of primitive objects when the Universe was young

- **D observations:** in remote **cosmological clouds** (i.e. at high redshift) on the line of sight of quasars

$$D/H = (2.527 \pm 0.030) \times 10^{-5}$$

- **^4He observations:** in H II (ionized H) regions of blue compact galaxies

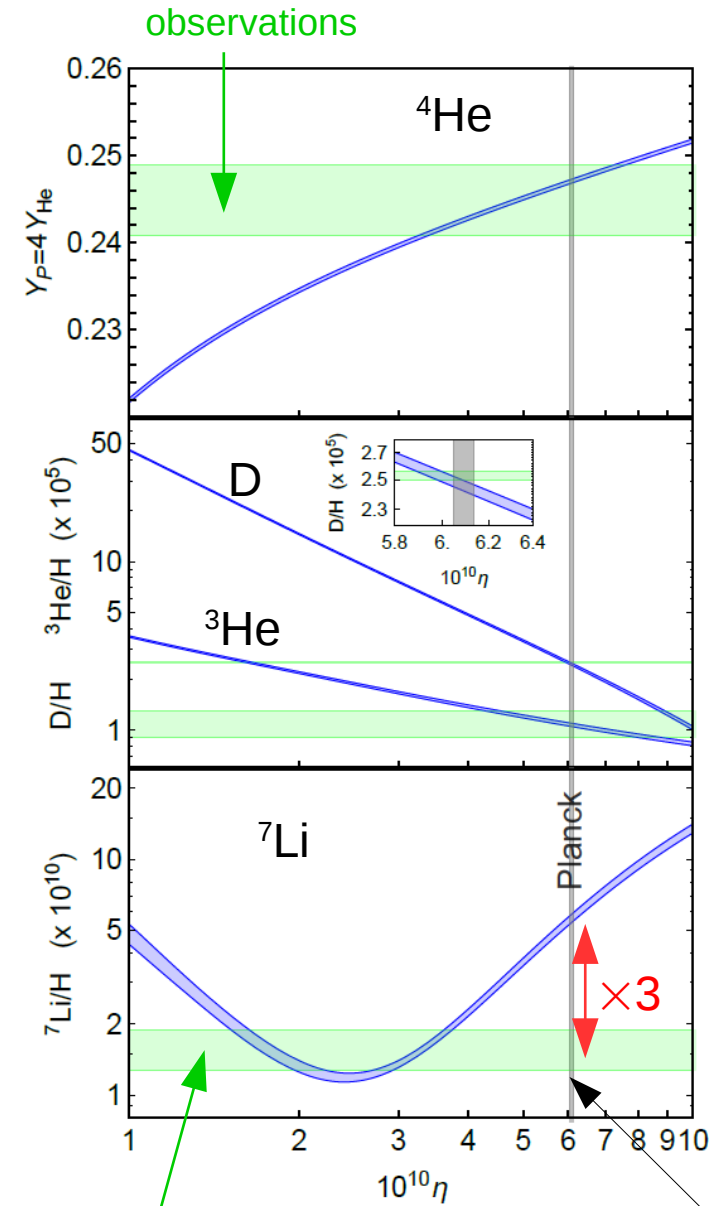
$$^4\text{He}/\text{H} = 0.2449 \pm 0.0040$$

- **^3He observations:** in HII regions of *our* Galaxy

$$^3\text{He}/\text{H} = (1.1 \pm 0.2) \times 10^{-5}$$

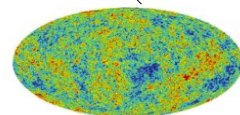
- **^7Li observations:** at the surface of low metallicity stars in the halo of our Galaxy

$$^7\text{Li}/\text{H} = 1.58^{+0.35}_{-0.28} \times 10^{-10}$$



Pitrou+ 2018

Metal poor Halo dwarf stars



Solutions to the ${}^7\text{Li}$ problem?

Several possibilities are considered

- **Astrophysical** solution
- **Nuclear physics** solution
- **Physics beyond** the standard model

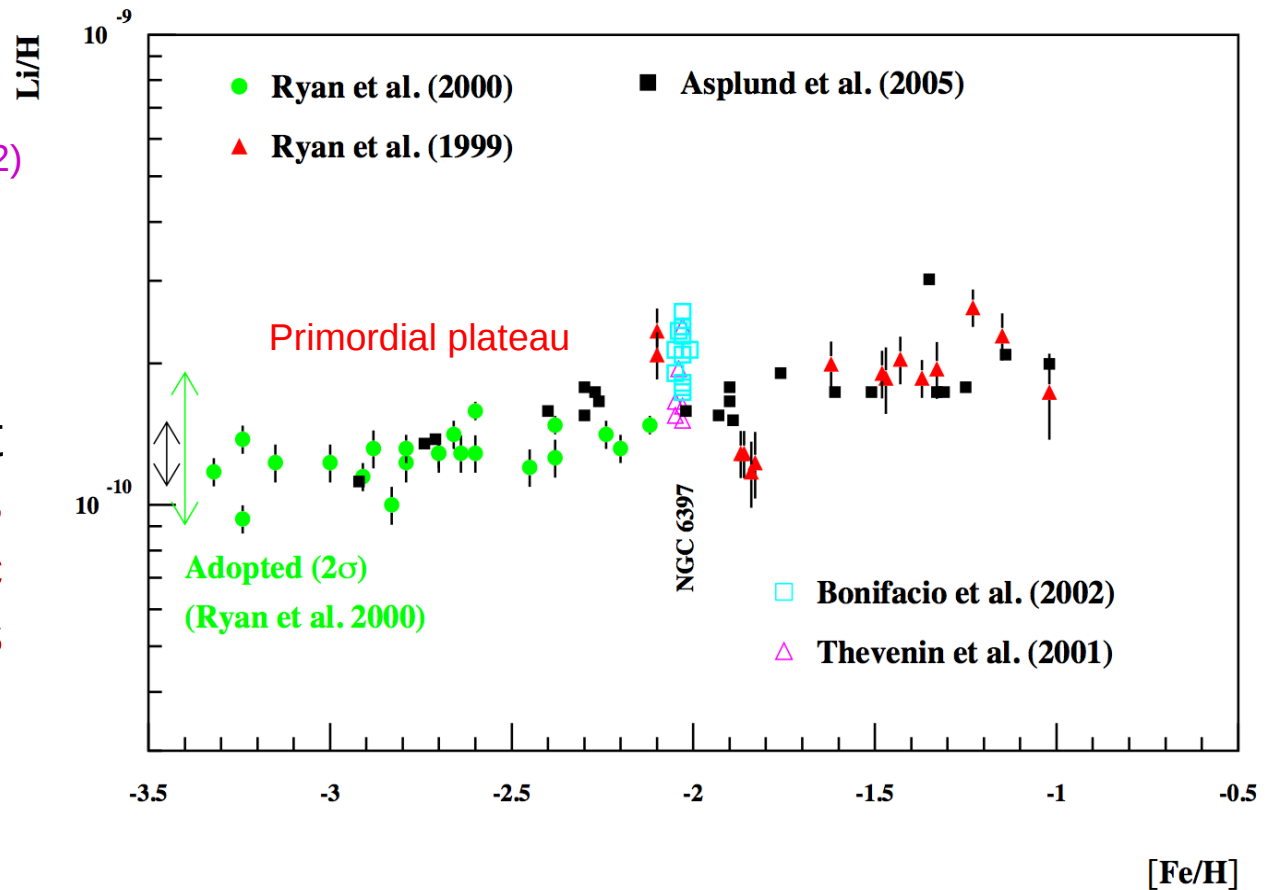
${}^7\text{Li}$ abundances

Primordial ${}^7\text{Li}$ abundance measured in old metal poor halo dwarf stars

Spite plateau (Spite & Spite, 1982)

- $\text{Li}/\text{H} \approx 1.12 \times 10^{-10}$
- Very low dispersion

Spite plateau indicates that the bulk of the lithium is unrelated to galactic nucleosynthesis processes and thus is primordial



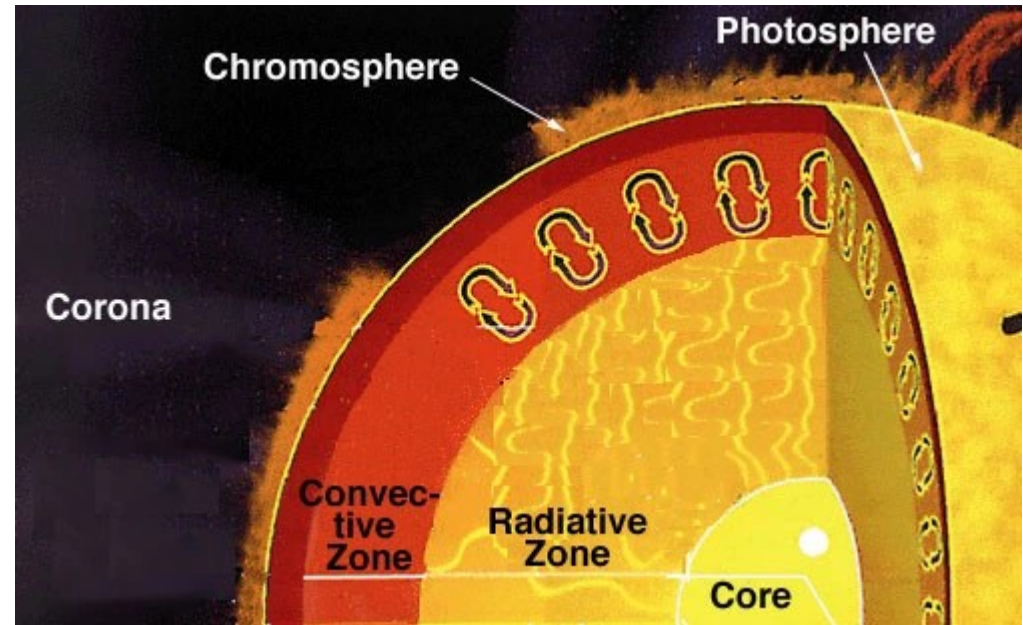
How reliable is Li abundance determination?

- Systematic errors in the extraction of Li abundances due to the used atmosphere models?
- unlikely Asplund and Lind 2010

${}^7\text{Li}$ stellar destruction?

Could atmospheric ${}^7\text{Li}$ be depleted by rotationally induced **mixing and/or diffusion**?

- Lithium easily burned in stars (**low binding energy**)
→ ${}^7\text{Li}(p,\alpha)\alpha$ for $T > 2.5$ MK
- **Convection brings surface material to deeper layers**
→ lithium burning



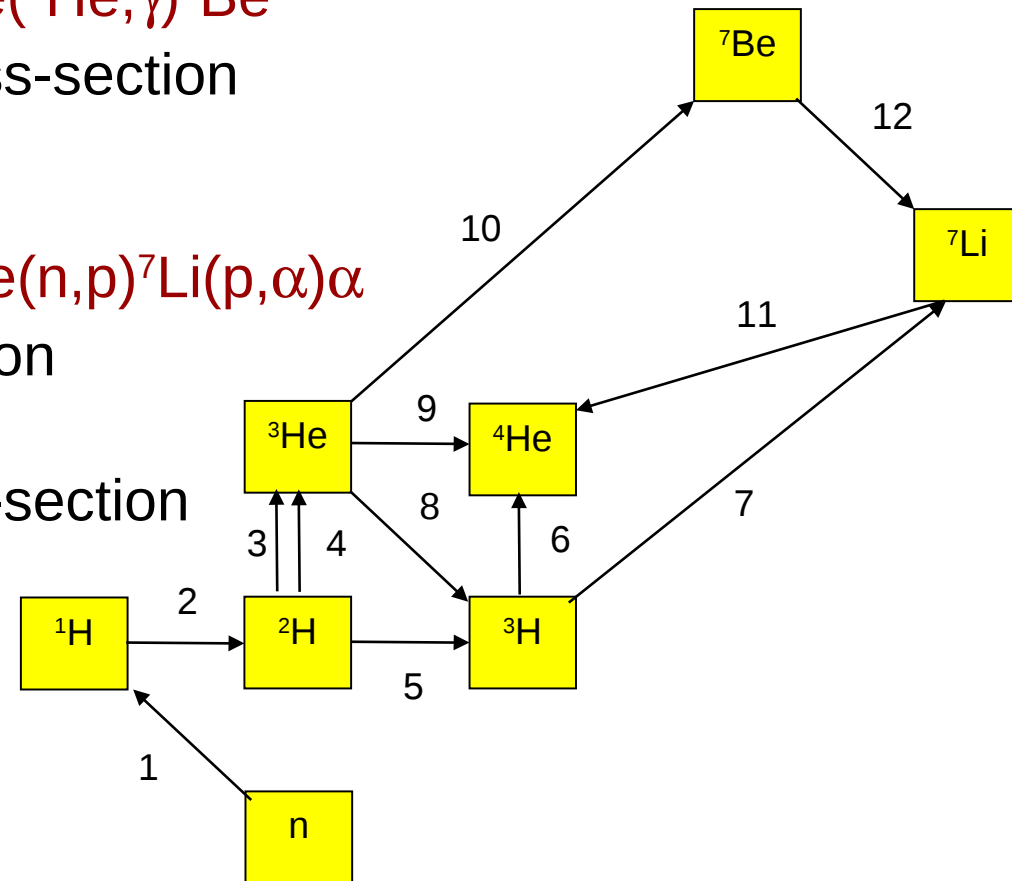
Not enough and not uniform ${}^7\text{Li}$ destruction

- Metal poor halo stars have **shallower convective zones** than in solar metallicity stars
- Stars of different masses have different convective zone size
→ **larger scatter** around ${}^7\text{Li}$ plateau **should be observed**

Nuclear solution to ${}^7\text{Li}$ problem?

- ${}^7\text{Li}$ produced by ${}^7\text{Be}$ decay (EC) at high $\Omega_b h^2$
- Main ${}^7\text{Be}$ production mechanism: ${}^3\text{He}({}^4\text{He}, \gamma){}^7\text{Be}$
 - Various measurements of the cross-section
10% uncertainty
- Main ${}^7\text{Be}$ destruction mechanism: ${}^7\text{Be}(n, p){}^7\text{Li}(p, \alpha)\alpha$
 - ${}^7\text{Be}(n, p){}^7\text{Li}$ well known cross-section
1% uncertainty
 - ${}^7\text{Li}(p, \alpha)\alpha$ 6% uncertainty on cross-section
- Secondary destruction mechanisms ${}^7\text{Be}+d, {}^7\text{Be}+{}^3\text{He}, {}^7\text{Be}+{}^4\text{He}\dots$
 - all experimentally studied, and none can alleviate the ${}^7\text{Li}$ problem

Any additional ${}^7\text{Be}$ destruction would alleviate the ${}^7\text{Li}$ problem



Nuclear physics is very unlikely to solve the ${}^7\text{Li}$ problem

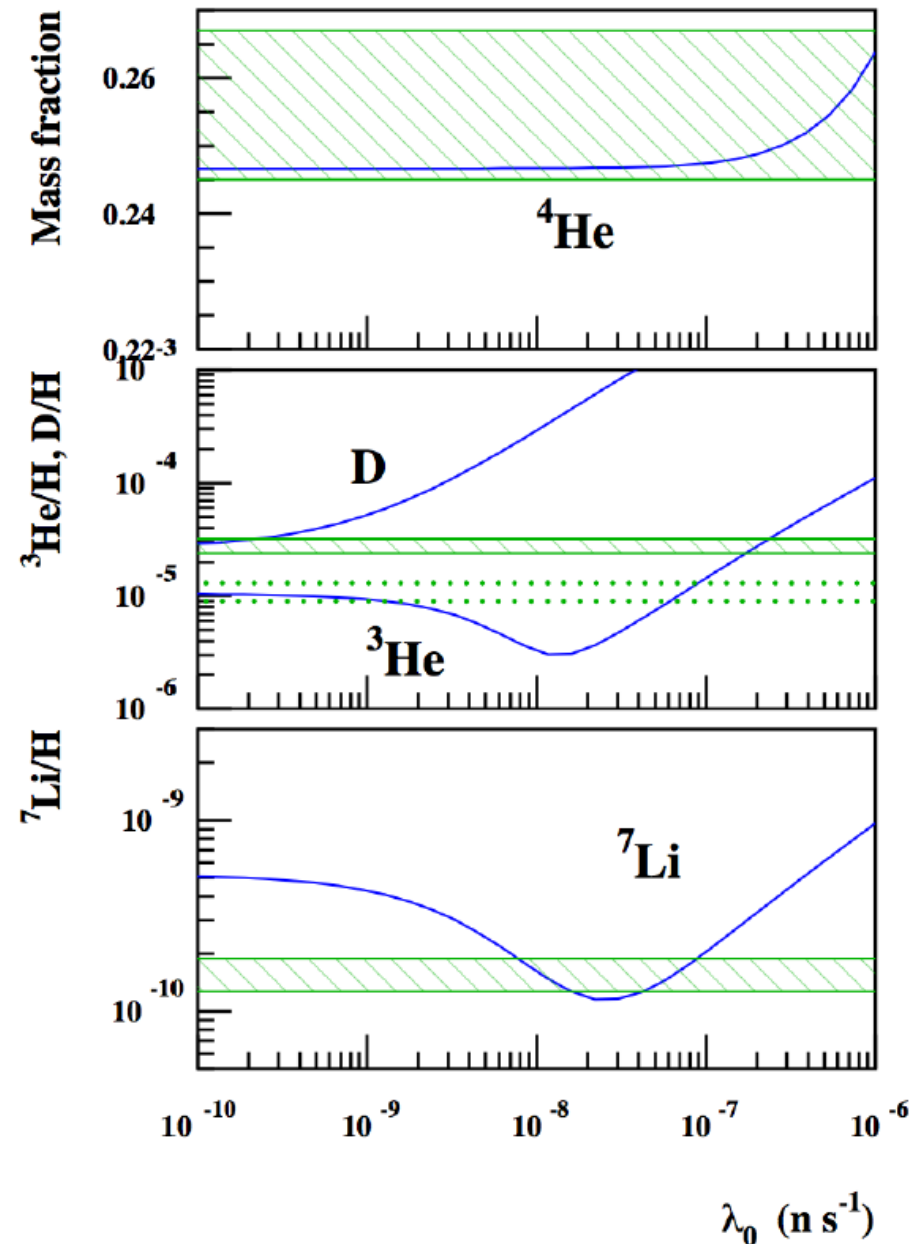
Physics beyond the standard model?

Idea: late time neutron injection

- enhance ${}^7\text{Be}$ destruction by ${}^7\text{Be}(n,p){}^7\text{Li}(p,\alpha)\alpha$ reactions
- Alleviate the Li problem at the expense of deuterium overproduction

Two examples among many....

- Decays of heavier meta-stable (100 – 1000 s) particles that inject additional neutrons
(Jedamzik (2004, 2006), Kawasaki+ (2005), Ellis+ (2005))
- Existence of a mirror universe in which neutrons can oscillate to our world (Coc+ 2013)
→ effective late time neutron injection



Summary

- Big-Bang Nucleosynthesis (BBN) produces, between 3 min and 20 min, **H**, **D**, **He** and part of **Li**
- Heavier elements nucleosynthesis is prevented because:
 - Larger Coulomb barriers for elements with higher atomic numbers (see next Lecture)
 - Lack of isotope of mass number $A = 5$ and $A = 8$
 - Decreasing matter density as the Universe expands

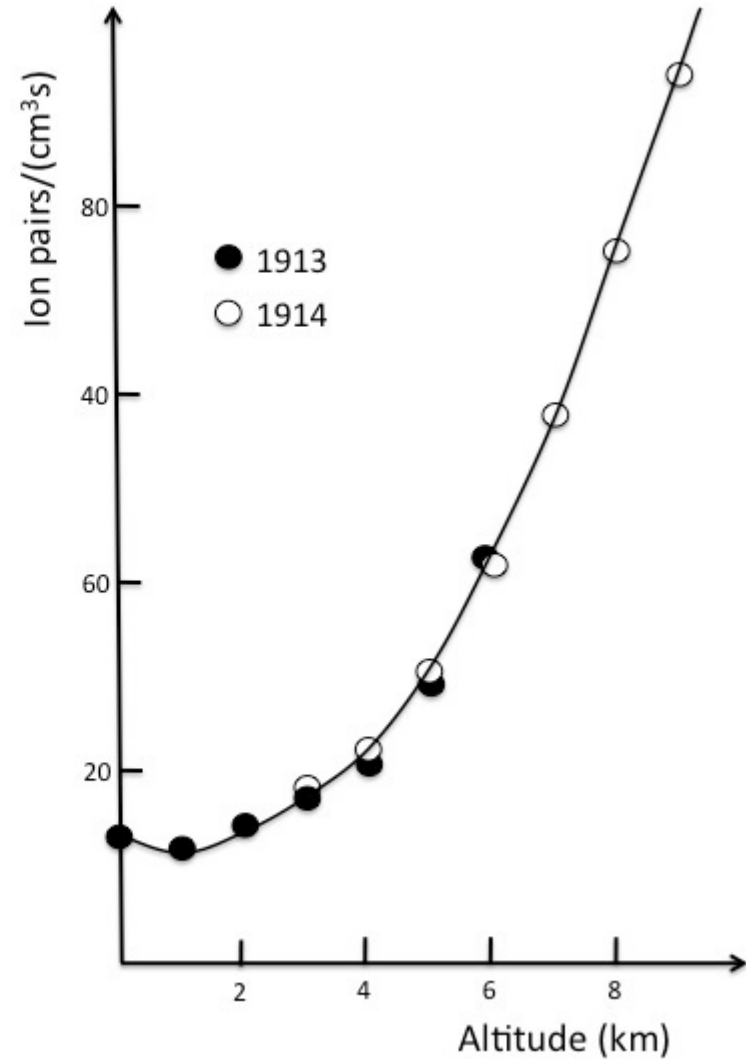
Further reading...

- C. Pitrou, A. Coc, P. Uzan & E. Vangioni, *Physics Reports* (2018)
- NPAC, cosmology course

3. Cosmic rays nucleosynthesis



Hess (center) lands after his balloon flight in 1912



Ionization as a function of altitude (Hess)



What is the origin of LiBeB isotopes?

What are the processes producing ${}^6,7\text{Li}$, ${}^9\text{Be}$ and ${}^{10,11}\text{B}$?

- **Big-Bang Nucleosynthesis**

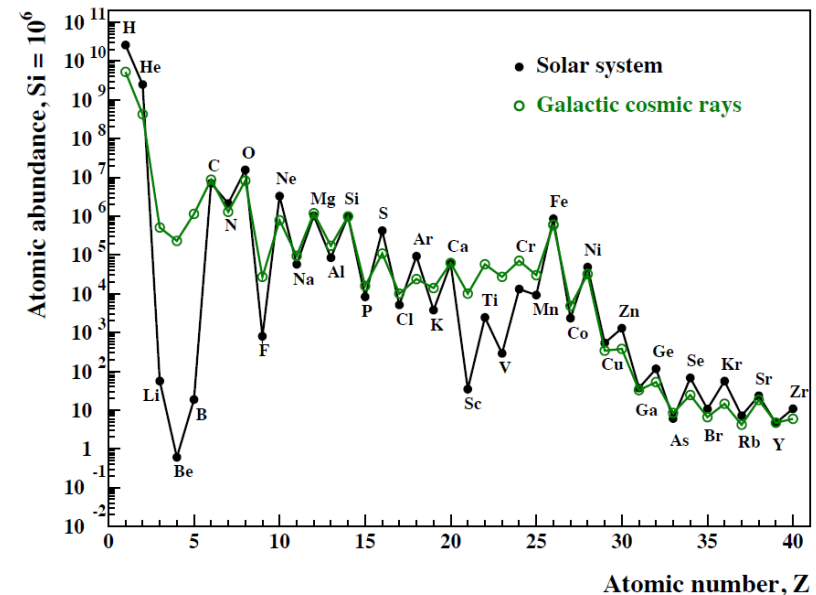
- significant amount of ${}^7\text{Li}$
- ${}^6\text{Li}$, ${}^9\text{Be}$ and ${}^{10,11}\text{B}$ abundances predicted from BBN are at least 3 orders of magnitude below the abundances measured in metal-poor stars

- **Stellar nucleosynthesis**

- Light elements are fragile enough (relatively low binding energy per nucleon) to be destroyed in stars during quiescent burning
- ${}^7\text{Li}$ in classical novae (explosive), AGB (?)
- ${}^7\text{Li}$, ${}^{11}\text{B}$ by ν -induced spallation reactions

- **Galactic Cosmic Rays (GCR)**

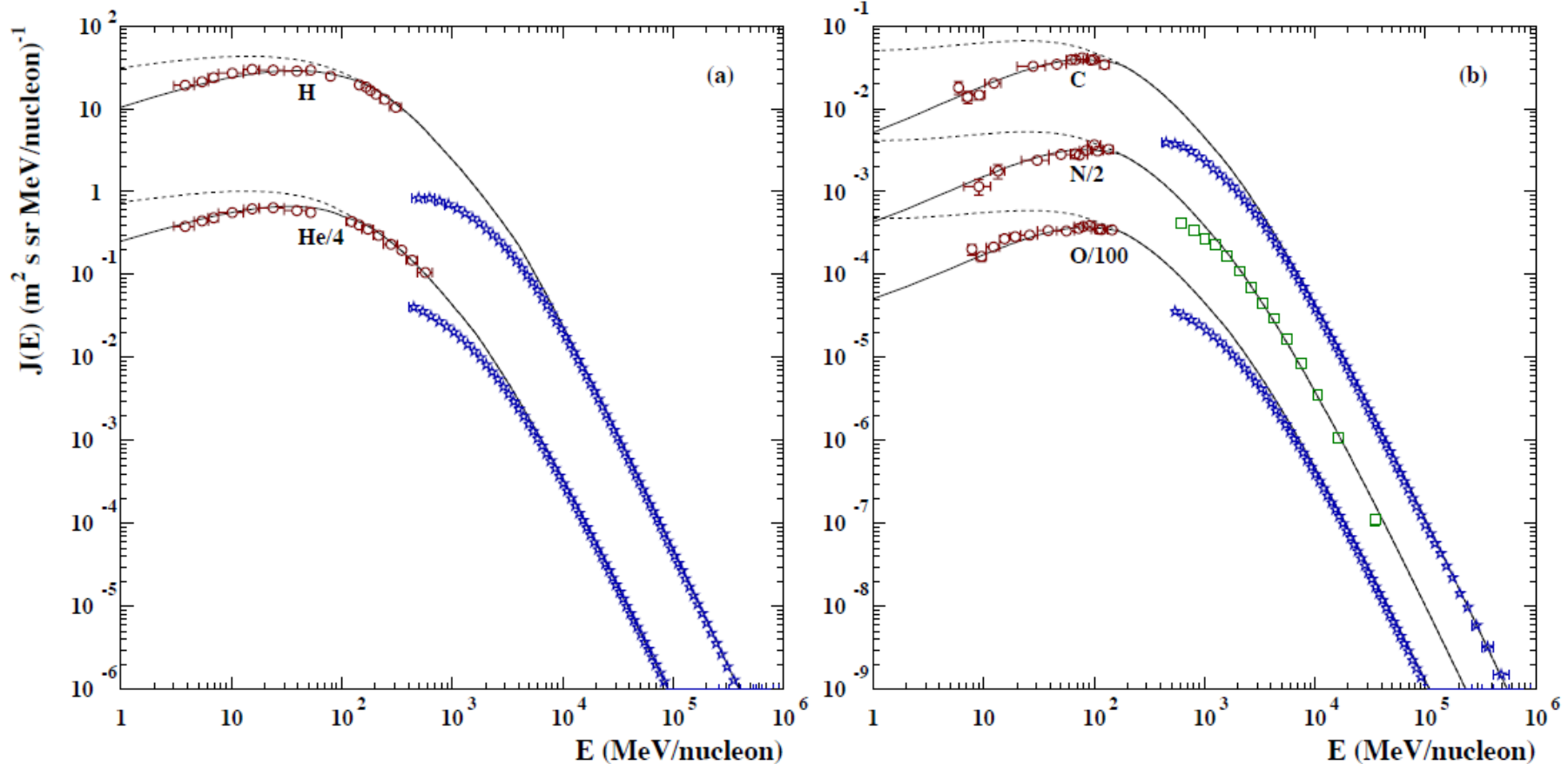
- Similar abundances than solar system with notable exception for LiBeB!!



Cosmic rays properties

Composition: H (90 %), He (9 %), C, N, O, e⁻ (1 %)

Cosmic rays are not in thermodynamic equilibrium → power law spectrum

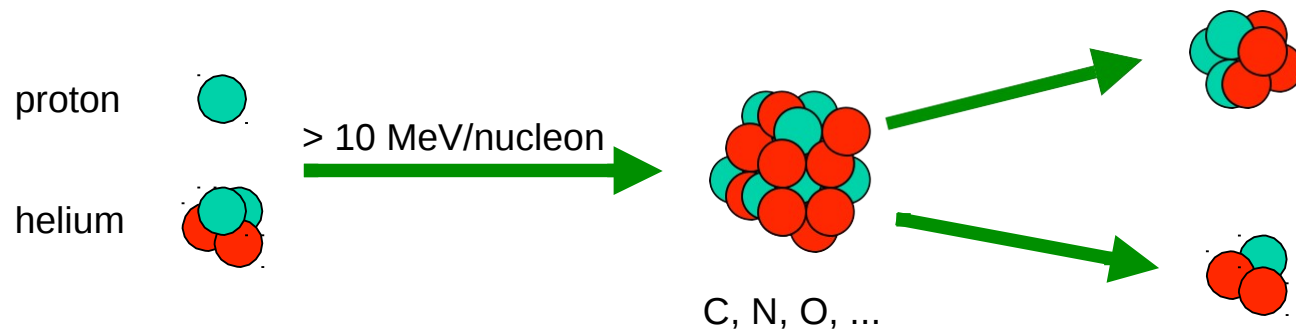


Data from *Voyager 1* probe (red circles), AMS-02 experiment (blue stars) and HEAO-3-C2 (green squares)

Spallogenic nucleosynthesis

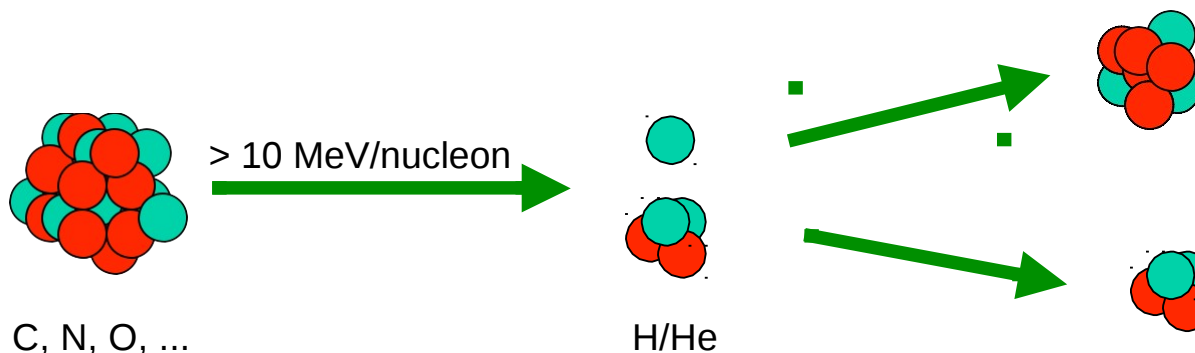
Non thermal nucleosynthesis induced by cosmic rays

Spallation: “heavy” nucleus (C, N, O, ...) emits lighter fragments (Li, Be, B, ...) as a result of a collision with a high-energy particle (H, He)



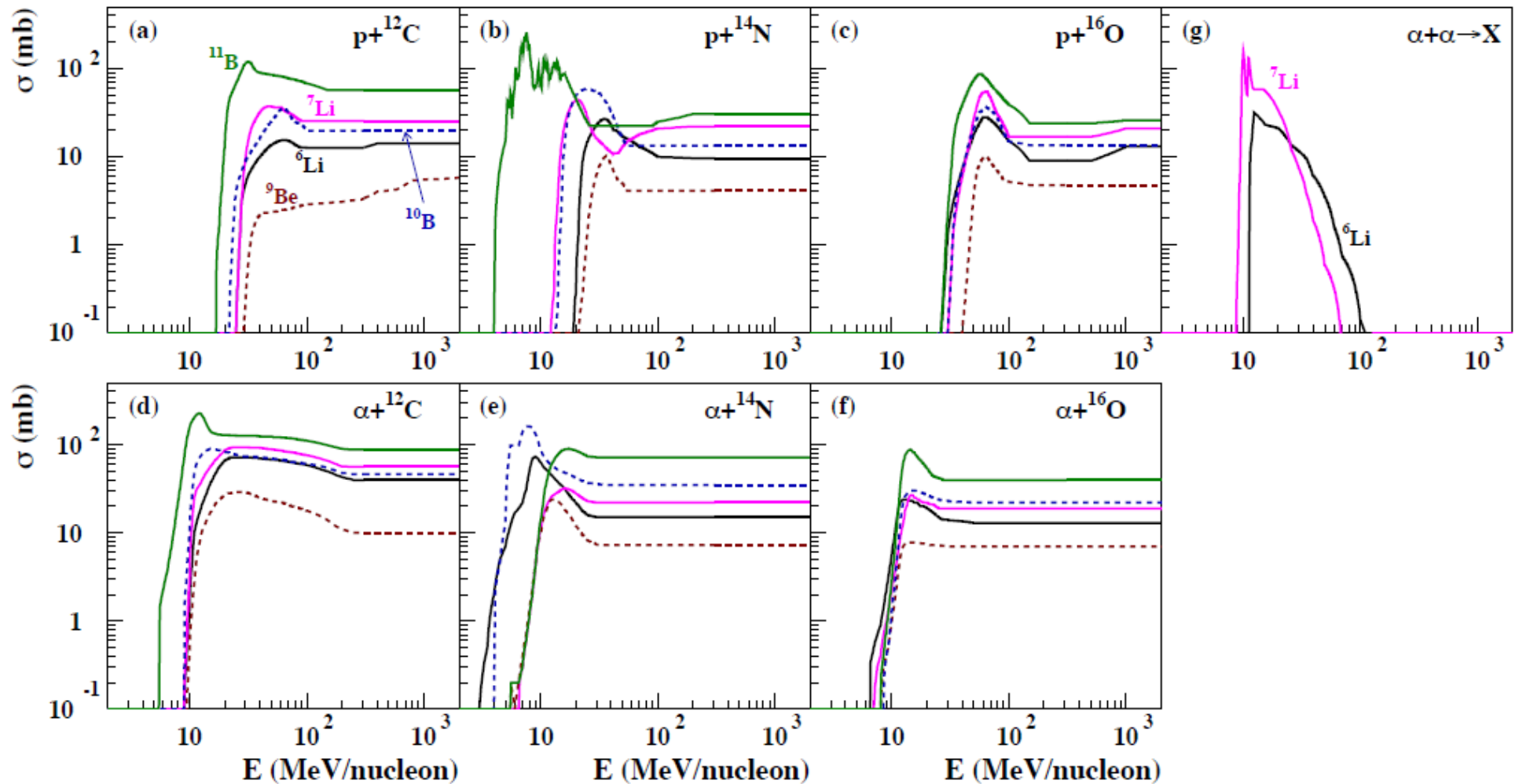
LiBeB emitted at much lower energy than incident H/He

Inverse spallation: heavy nucleus impinges light nucleus



LiBeB emitted at about same energy per nucleon as incident C, N, O, ...
→ must slow down to rest (small survival probability)

Spallation cross-sections



- The decreasing sequence of B, Li and Be matches the B, Li and Be GCR abundances
- $\alpha + \alpha$ reactions important for production of $^6,7\text{Li}$ isotopes

Summary

Galactic Cosmic Rays play a major role in the production of the LiBeB elements

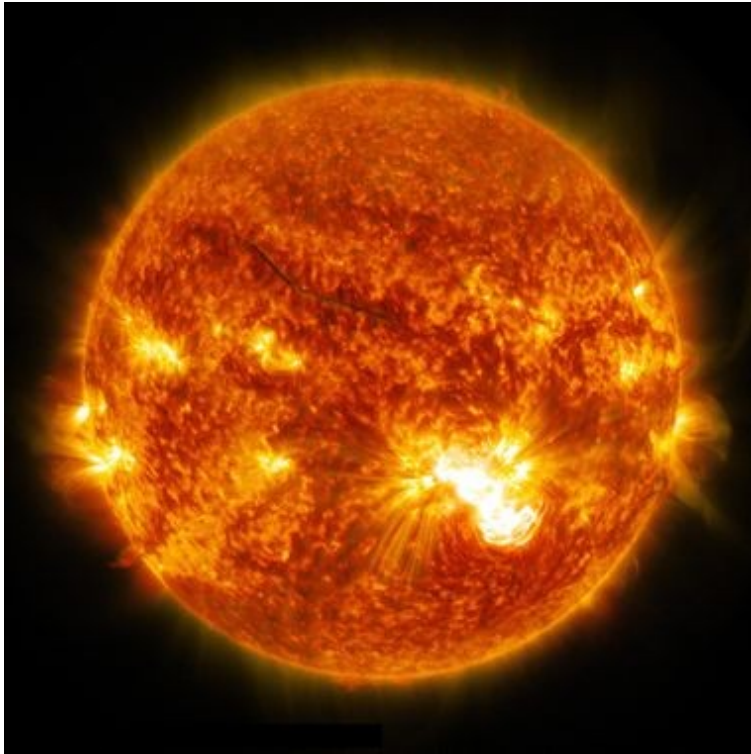
	BBN	GCR	ν in core-collapse supernovae	Low-mass stars
${}^6\text{Li}$		100 %		
${}^7\text{Li}$	12 %	18 %	< 20 %	50 – 70 %
${}^9\text{Be}$		100 %		
${}^{10}\text{B}$		100 %		
${}^{11}\text{B}$		70 %	30 %	

Further reading...

- V. Tatischeff & S. Gabici, *Annual Reviews* (2018)
- N. Prantzos, *Astronomy & Astrophysics* 542, A67 (2012)

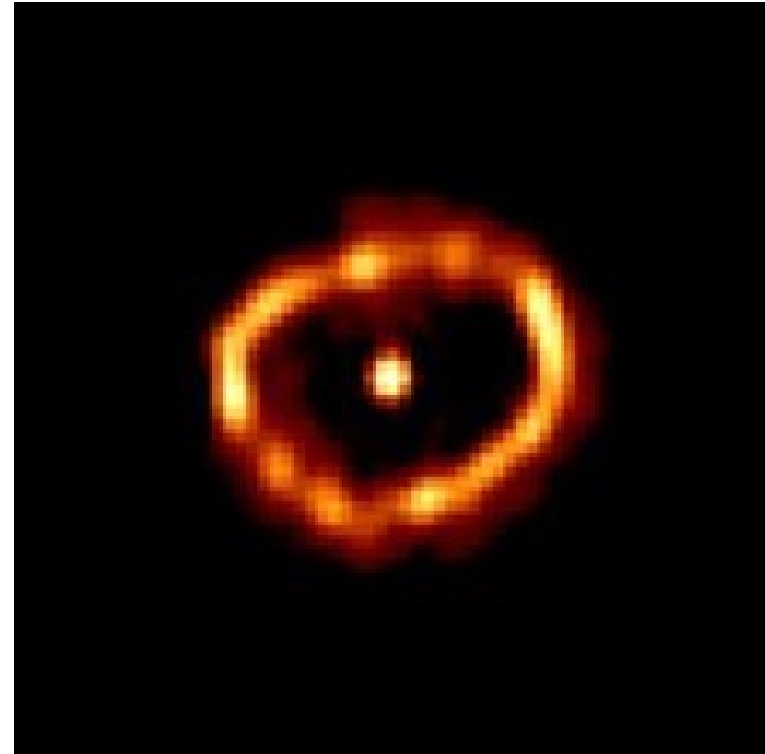
4. Stellar nucleosynthesis

Quiescent (hydrostatic)
stellar burning



Sun, Solar Dynamics Observatory

Explosive
stellar burning



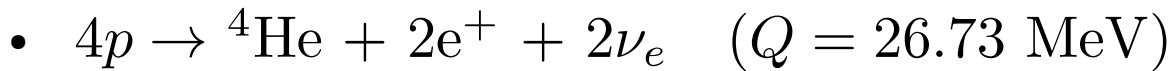
Classical nova, Nova Cygni 1992, HST

4.1 Quiescent hydrogen burning

- Where does it take place?

- Core of main-sequence stars (8 – 55 MK)
- Core of the Sun (15.6 MK)
- Burning shell in AGB stars (45 – 100 MK)

- How does it work?



↓
ashes

↓
energy source

- Probability for the simultaneous interaction of 4 protons far too small → reactions sequence

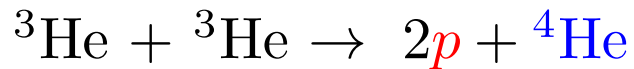
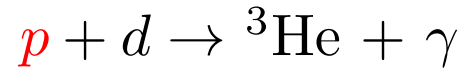
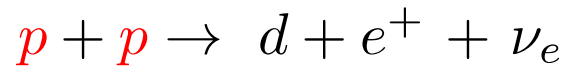
- Who & when?

- Bethe & Critchfield (1938)
 - von Weizsaecker (1938)
 - Bethe (1939)
- } pp chain
- CNO cycle

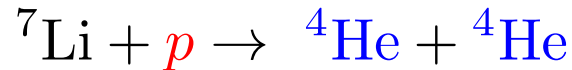
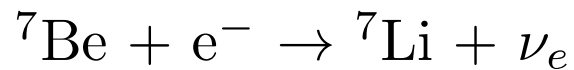
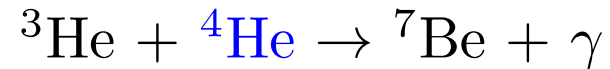


Hans Bethe (1906 – 2005)

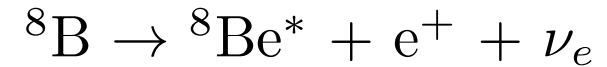
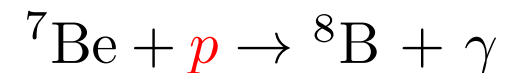
The proton – proton (pp) chains



pp1



pp2

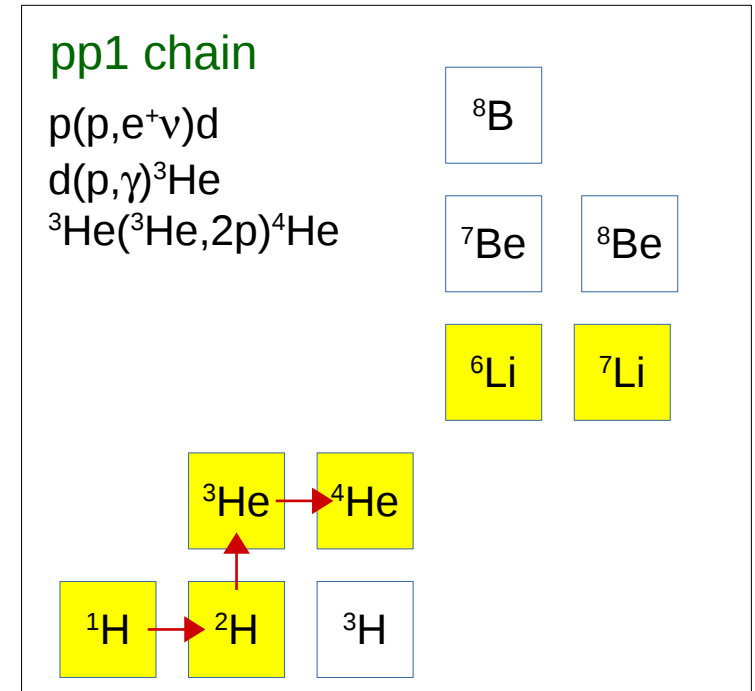


pp3

Note: neutrinos provide direct evidence that nuclear reactions occur (see later)

The pp1 chain (1)

- Succession of 3 reactions producing almost 90 % of Sun's energy
- First reaction: $p + p \rightarrow d + e^+ + \nu$ ($Q = 1.44$ MeV)
 - strong + weak interactions
 - cross-section is about 20 orders of magnitude smaller than for nuclear (strong) interaction!!
 - cannot be measured
 - can be calculated



- All subsequent reactions involve nuclear and electromagnetic interactions
 - much faster
- Second reaction: $p + d \rightarrow {}^3\text{He} + \gamma$ ($Q = 5.49$ MeV)
 - many measurements since 1962, including one at LUNA in 2002 (see lecture 4)

The pp1 chain (2)

- Deuterium abundance in the core of the Sun

- Temporal evolution of deuterium = **production** [p(p,e⁺ν)d]
– **destruction** [d(p,γ)³He]

$$\frac{dN_d}{dt} = \frac{N_H^2}{2} \langle \sigma v \rangle_{p(p,e^+\nu)} - N_H N_d \langle \sigma v \rangle_{d(p,\gamma)}$$

- At equilibrium:

$$\left(\frac{N_d}{N_H} \right)_e = \frac{\langle \sigma v \rangle_{p(p,e^+\nu)}}{2 \langle \sigma v \rangle_{d(p,\gamma)}}$$

For $T = 15.6$ MK (Sun)

$$\langle \sigma v \rangle_{p(p,e^+\nu)} = 1.5 \times 10^{-43} \text{ cm}^3 \text{ s}^{-1}$$

$$\langle \sigma v \rangle_{d(p,\gamma)} = 2.0 \times 10^{-26} \text{ cm}^3 \text{ s}^{-1}$$

$$\left(\frac{N_d}{N_H} \right)_e = 7.5 \times 10^{-18}$$

Solar D/H $\approx 2 \times 10^{-5}$
→ D from BBN

- Lifetime of a proton and a deuterium in the core of the Sun

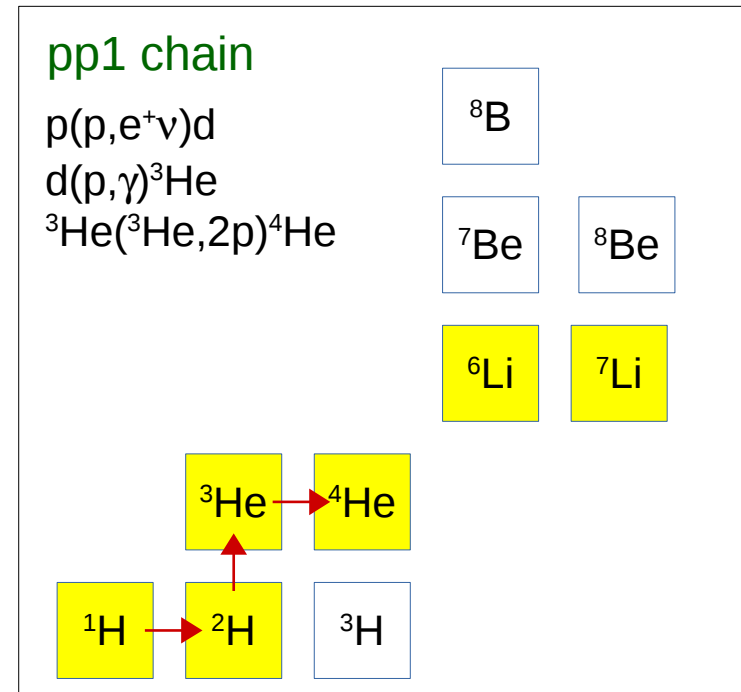
we consider $\rho_c = 150 \text{ g cm}^{-3}$ and $X_H \sim X_{\text{He}} \sim 0.5 \rightarrow N_H = 4.5 \times 10^{25} \text{ cm}^{-3}$

$$\tau_H = \frac{1}{N_H \langle \sigma v \rangle_{p(p,e^+\nu)}} = 4.7 \times 10^9 \text{ yr} \quad \tau_d = \frac{1}{N_H \langle \sigma v \rangle_{d(p,\gamma)}} = 1.1 \text{ s}$$

The pp1 chain (3)

Possible reactions for ^3He burning

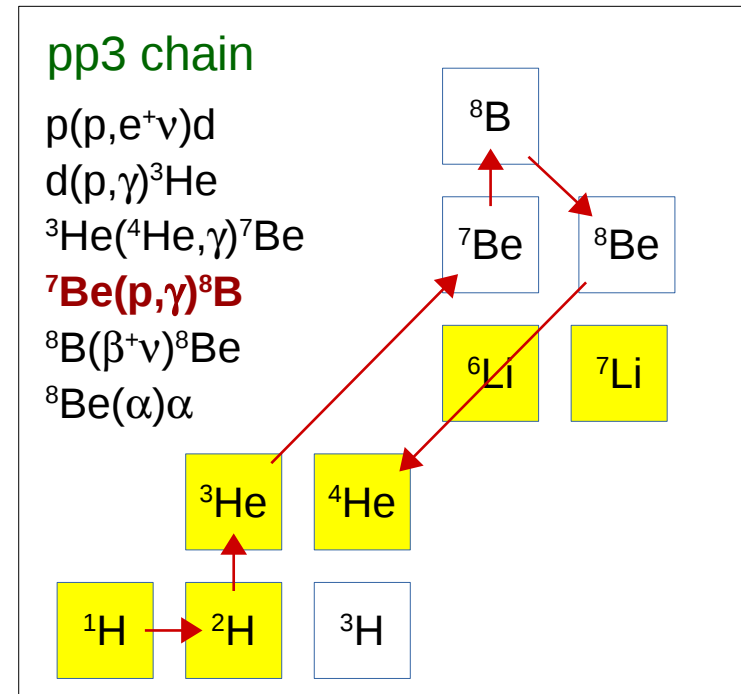
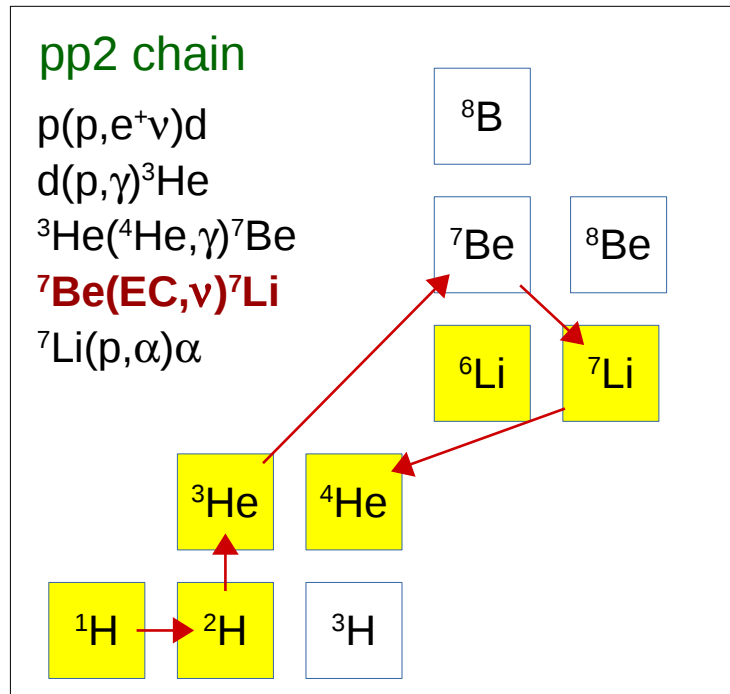
Reaction	Q (MeV)	S(0) (keV b)
$^3\text{He}(d,\gamma)^5\text{Li}(p)^4\text{He}$	16.39	~ 0.3
$^3\text{He}(d,p)^4\text{He}$	18.35	6240
$^3\text{He}(^3\text{He},\gamma)^6\text{Be}(2p)^4\text{He}$	11.50	~ 0.8
$^3\text{He}(^3\text{He},2p)^4\text{He}$	12.86	5320 (80)
$^3\text{He}(^4\text{He},\gamma)^7\text{Be}$	1.59	0.57 (4)



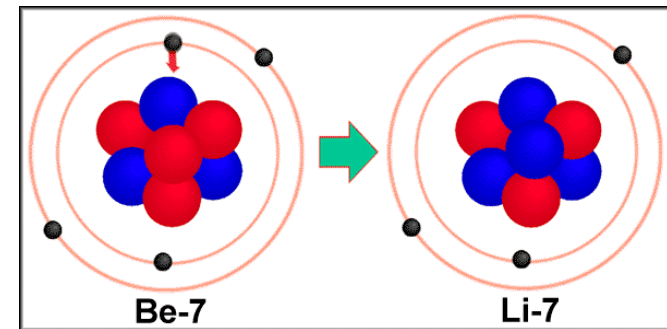
- $^3\text{He} + p \rightarrow ^4\text{Li} \rightarrow ^3\text{He} + p$ ($\tau = 10^{-22}$ s)
- $^3\text{He} + d$ negligible given the low deuterium abundance
- $^3\text{He} + ^3\text{He} \rightarrow 2p + ^4\text{He}$ ($Q = 12.86$ MeV) \rightarrow **Third reaction of the pp1 chain**
 \rightarrow has been measured in LUNA (see lecture 4)
- If $N(^4\text{He}) \gg N(^3\text{He})$ [factor $> 10^4$] then $^3\text{He}(^4\text{He},\gamma)^7\text{Be}$ is activated
 \rightarrow **pp2 & pp3 chains**

The pp2 and pp3 chains

^7Be destruction: competition between **electronic capture (EC)** and **proton capture**

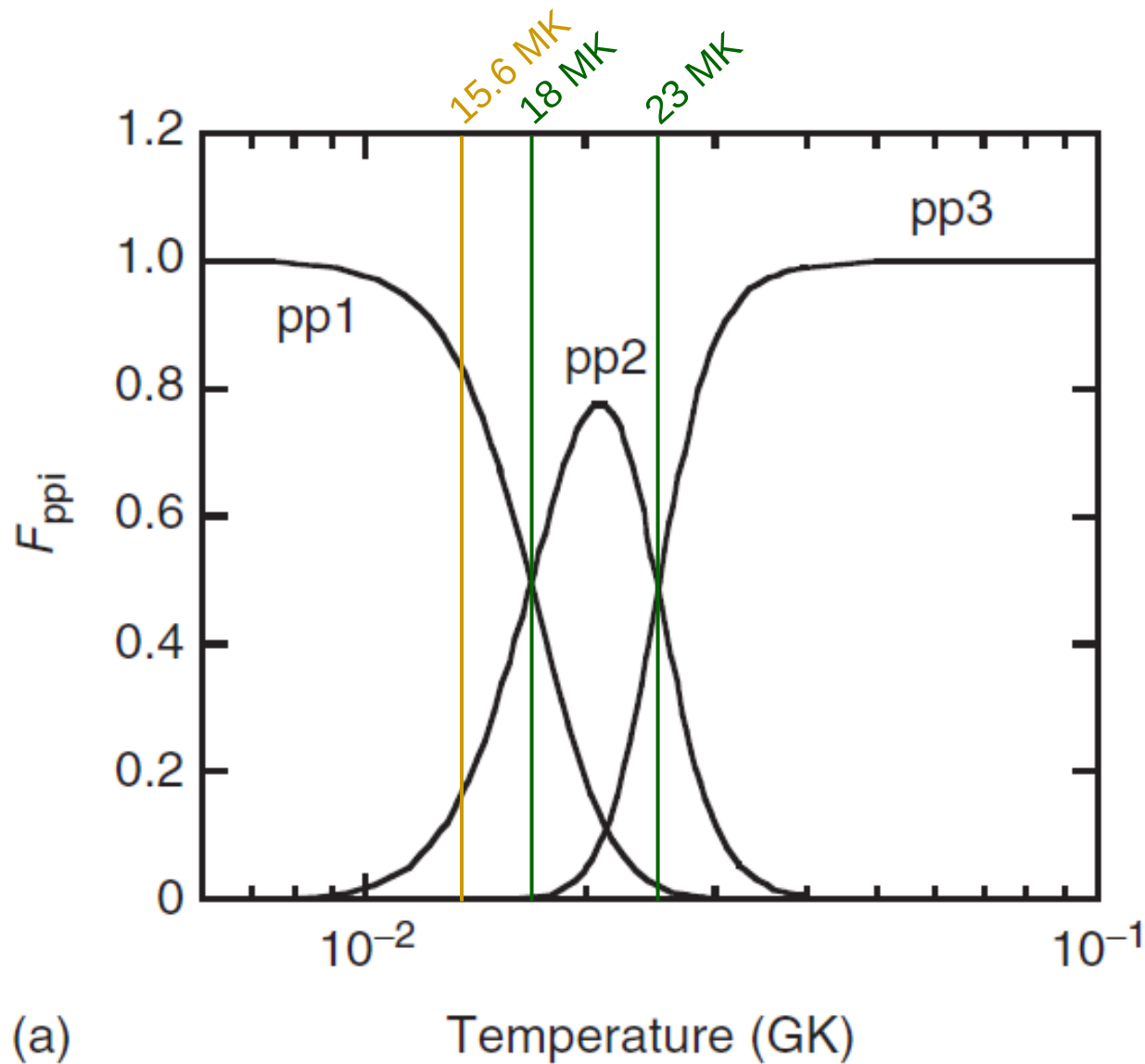


- ^7Be decays by EC and its lifetime depends on its charge state
- In stars, ^7Be fully ionized and then capture free electrons, so τ depends on n_e and T . In the Sun's core $\tau_s = 1.6 \tau_{\text{lab}} = 120$ days



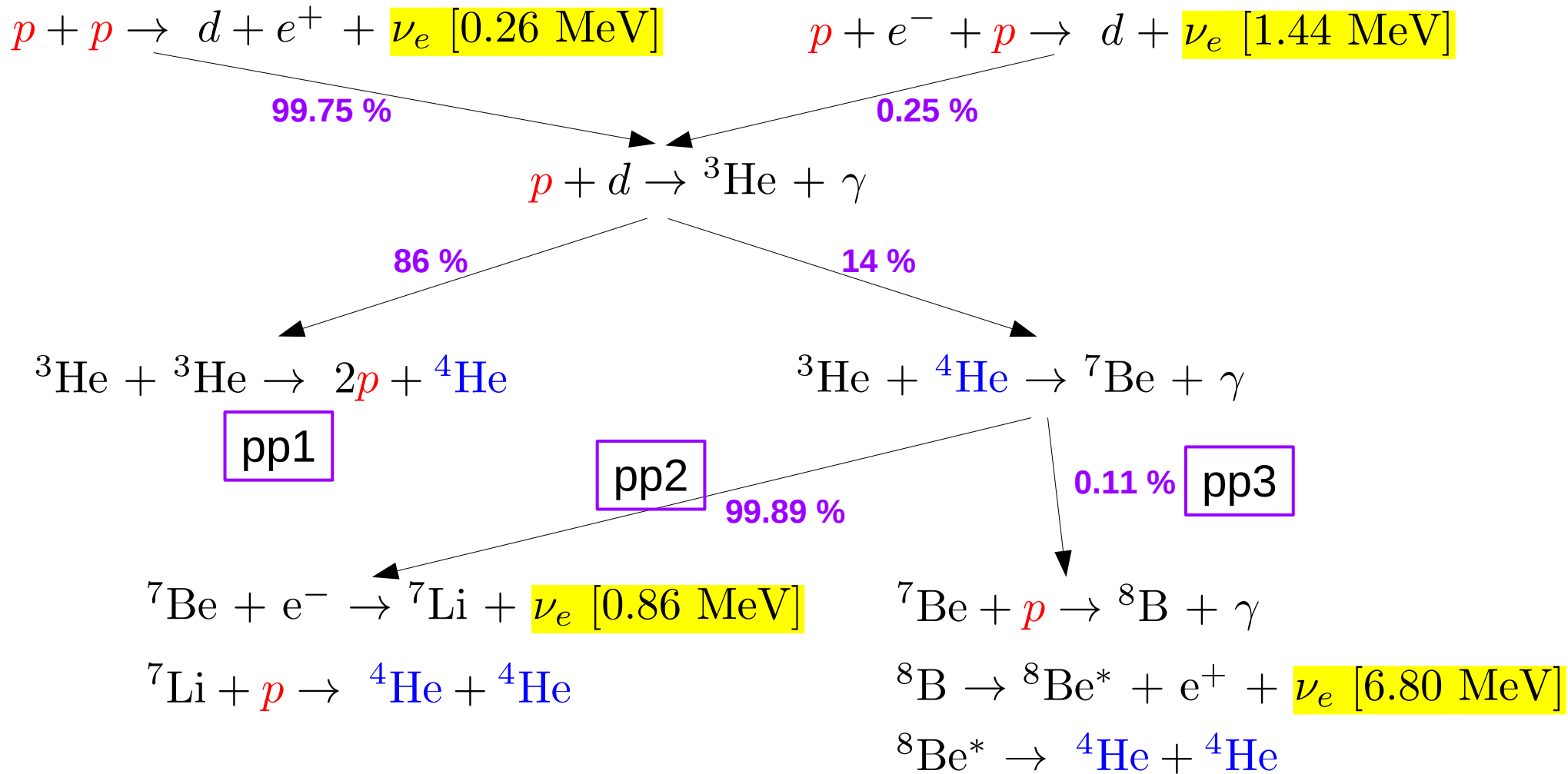
- The $^7\text{Be}(p, \gamma) ^8\text{B}$ reaction is faster than ^7Be EC for $T > 25$ MK \rightarrow pp3 chain

Relative contribution of the 3 pp chains



- $T < 18$ MK
→ pp1 chain
- 18 MK $< T < 23$ MK
→ pp2 chain
- $T > 23$ MK
→ pp3 chain
- Sun ($T = 15.6$ MK)
→ pp1 (84 %) + pp2 (14 %)

The pp chains in the Sun

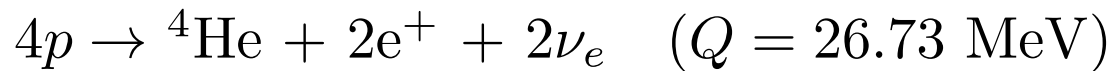


The effective energy given to the Sun is smaller than $Q = 26.73 \text{ MeV}$ because of the **escape of the neutrinos**

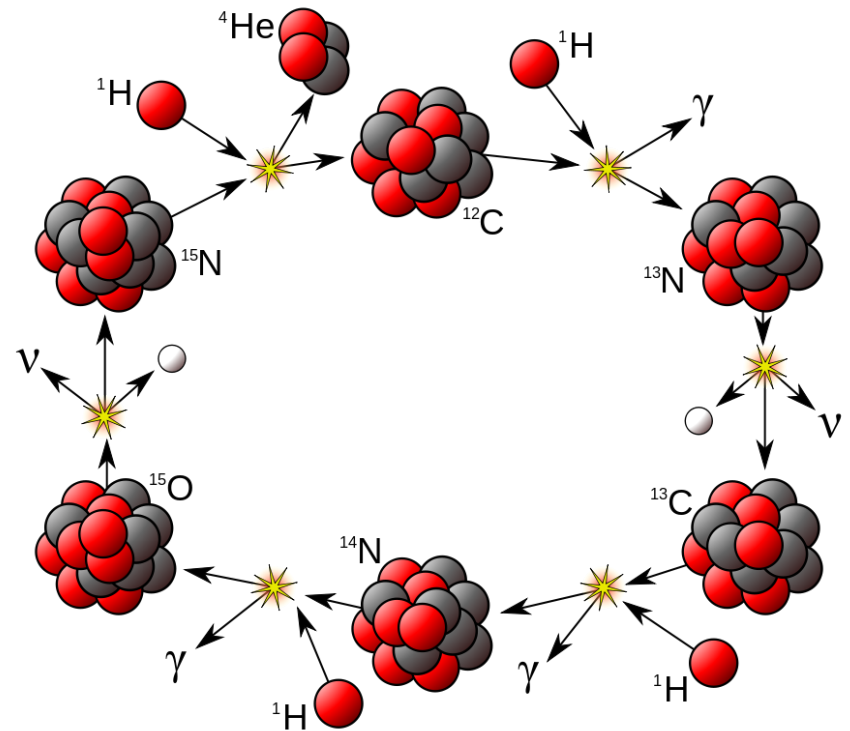
pp1 $Q_{eff} = Q - 2\bar{E}_\nu(p + p) = 26.20 \text{ MeV}$
 pp2 $Q_{eff} = Q - \bar{E}_\nu(p + p) - \bar{E}_\nu({}^7\text{Be}) = 25.61 \text{ MeV}$
 pp3 $Q_{eff} = Q - \bar{E}_\nu(p + p) - \bar{E}_\nu({}^8\text{B}) = 19.67 \text{ MeV}$

The CNO cycle (1)

- In **population I stars** (second, third... generation of stars), the elements C, N and O serve as **catalysts** of the transformation:



- There are four sets of reactions converting H to He \rightarrow 4 CNO cycles \rightarrow we will focus on the CNO-1 cycle

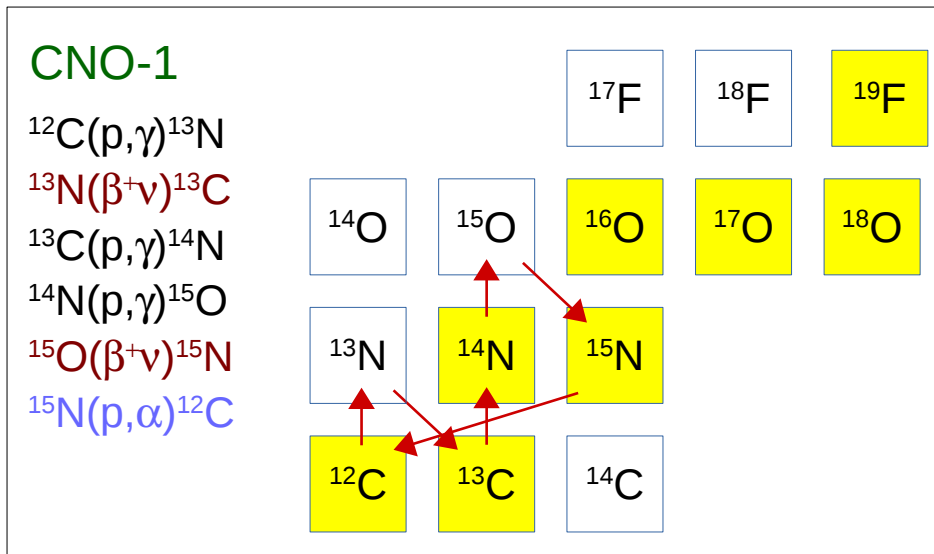


$$T_{1/2}({}^{13}\text{N}) = 9.965 \text{ min}$$

$$T_{1/2}({}^{15}\text{O}) = 122.24 \text{ s}$$

$$T_{1/2}({}^{17}\text{F}) = 64.49 \text{ s}$$

$$T_{1/2}({}^{18}\text{F}) = 109.77 \text{ min}$$



The CNO cycle (2)

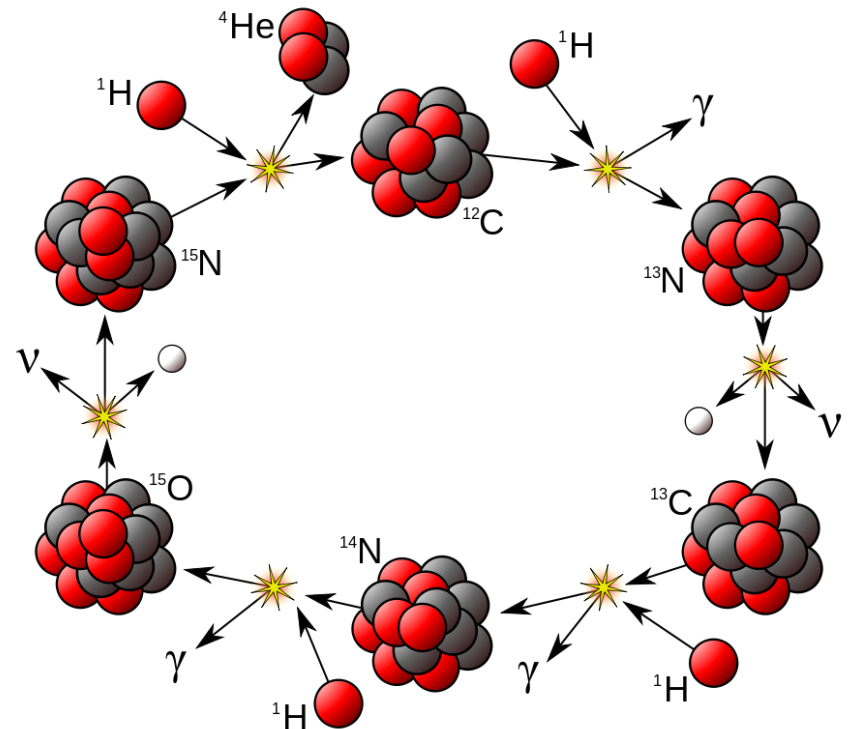
- The slowest reaction $^{14}\text{N}(p,\gamma)^{15}\text{O}$ of the CNO cycle fixes:

- the energy production rate $\epsilon \propto Q_{\text{CNO}}/\tau_{\text{CNO}}$
- the cycle duration

- $$\tau_{\text{CNO}} = \tau_p(^{12}\text{C}) + \tau_p(^{13}\text{C}) + \tau_p(^{14}\text{N}) + \tau_p(^{15}\text{N})$$

$$\cong \tau_p(^{14}\text{N})$$

- For $\rho_c = 100 \text{ g.cm}^{-3}$, $X_{\text{H}} = 0.5$ and $T_c = 60 \text{ MK}$
 - $\rightarrow \tau(^{12}\text{C}) = 6.1 \times 10^9 \text{ yr}$, $\tau(^{13}\text{C}) = 1.1 \times 10^9 \text{ yr}$,
 - $\tau(^{14}\text{N}) = 2.1 \times 10^{12} \text{ yr}$, $\tau(^{15}\text{N}) = 1.0 \times 10^8 \text{ yr}$



- The $^{14}\text{N}(p,\gamma)^{15}\text{O}$ reaction has been measured directly by the LUNA collaboration (see lecture 4)

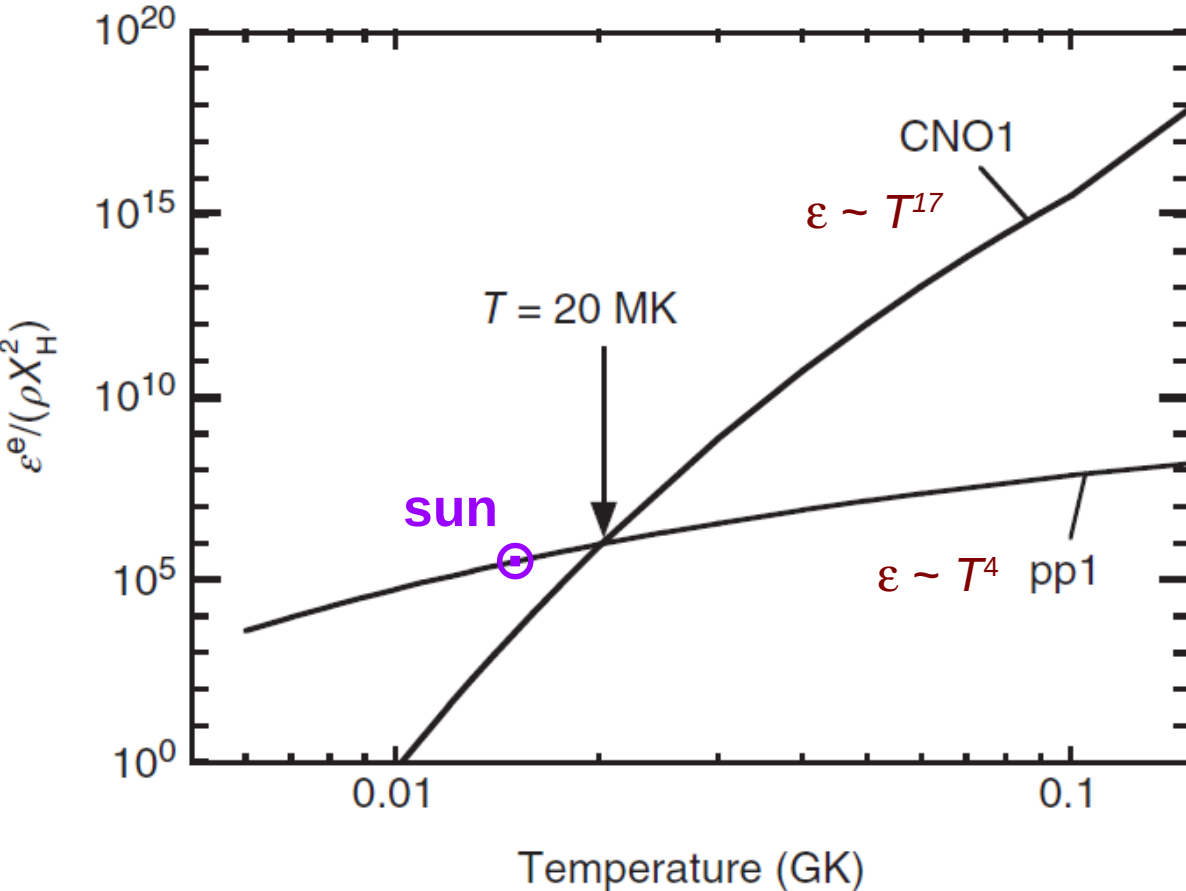
\rightarrow impact on the age of Globular Clusters (turn-off age; see lecture 1)

(Imbriani+, A&A, 2013)

- CNO cycle in AGB stars is the main source of ^{13}C and ^{14}N in the Universe

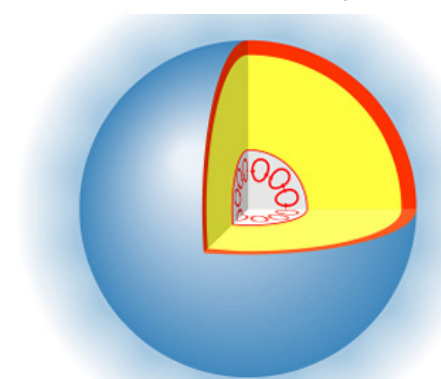
The CNO cycle (3)

Energy production rate

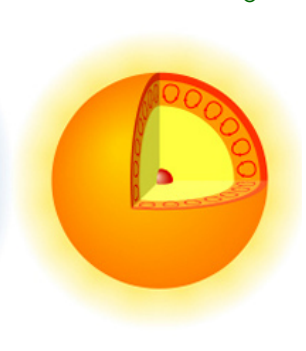


- CNO cycle has a steeper temperature dependence than pp chain (see lecture 3)
- pp1 chain dominates in low mass stars ($\sim M_{\odot}$), while CNO cycles dominates for higher mass stars (few M_{\odot})
- Above $T = 20$ MK, CNO1 faster than pp1
 - change in stellar structure at $1.15 M_{\odot}$, e.g. different radiative / convective zones

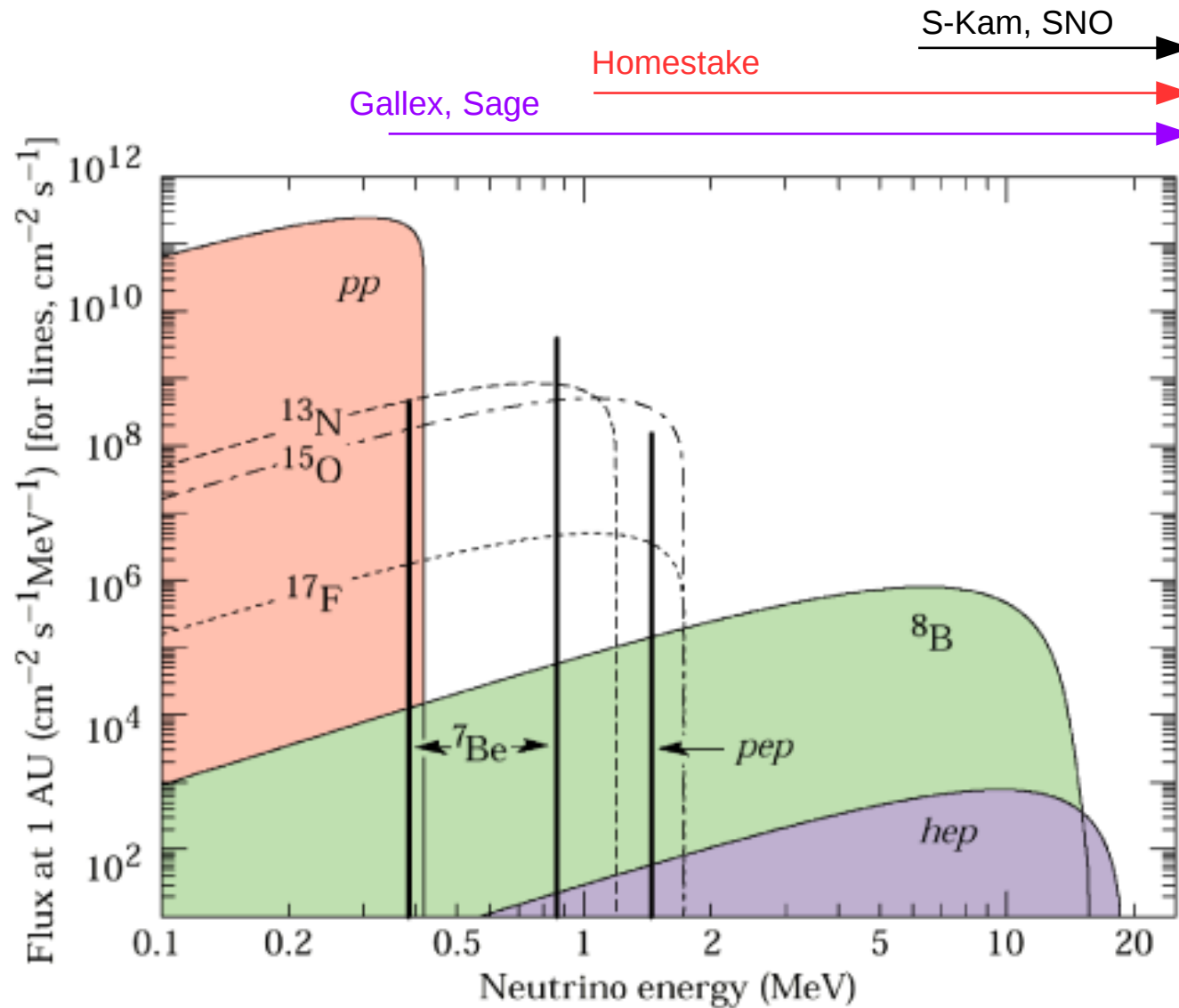
$M > 1.15 M_{\odot}$



$M < 1.15 M_{\odot}$



The solar neutrino spectrum



The detection of solar neutrinos (1)

The pioneering experiment (1964- 2001) of R. Davis (Nobel price in 2002) and J. Bahcall

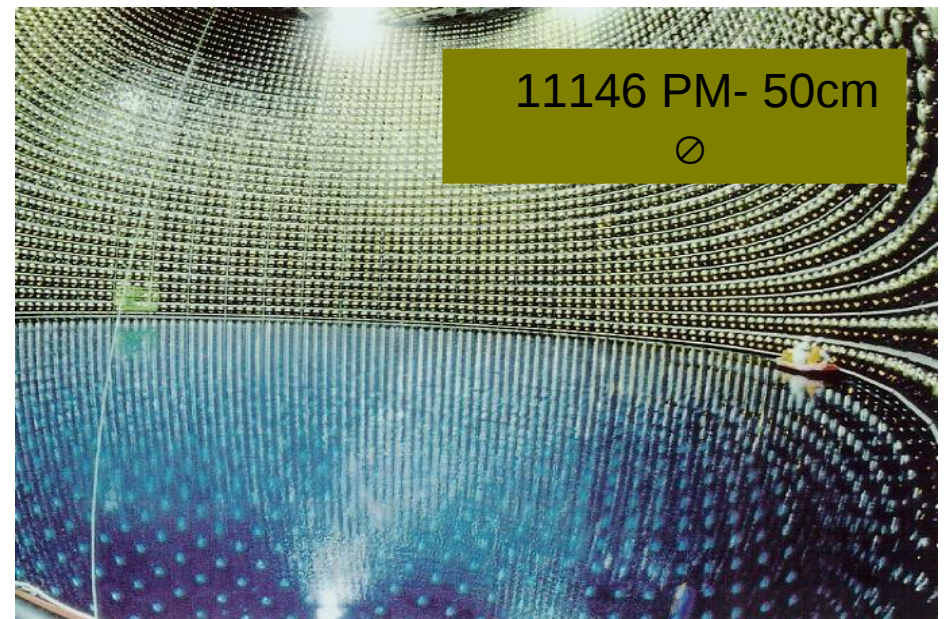
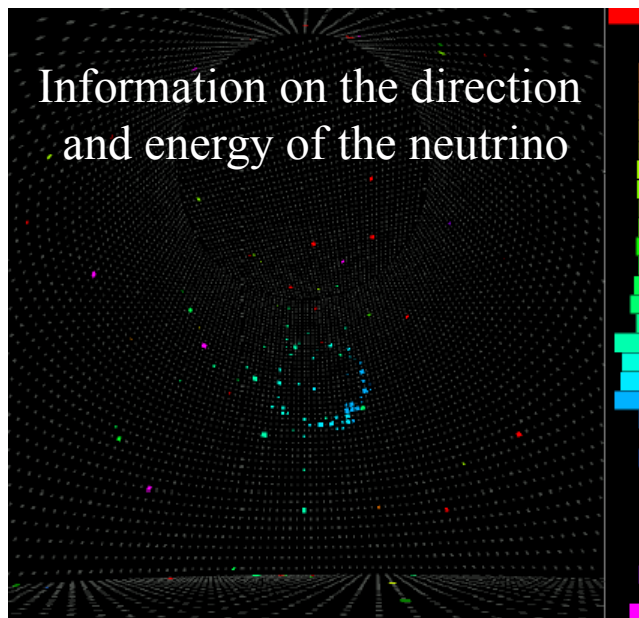
- 680 tons of perchloroethylene (C_2Cl_4) in the Homestake gold mine (1.5 km deep)
- $\nu_e + {}^{37}Cl \rightarrow {}^{37}Ar (T_{1/2} = 35 \text{ days}) + e^-$
- Production of ${}^{37}Ar$: ~ 0.5 atom per day
- Radiochemical separation: extraction of the ${}^{37}Ar$ nuclei every 100 days, counting (EC \rightarrow Auger electrons) in a gas detector
- Result: 2.56 ± 0.16 (stat) ± 0.16 (sys) **SNU**
→ 30 % of the expected signal
- Solar model (Bahcall 2004): 8.5 ± 0.18 SNU



1 SNU (Solar Neutrino Unit) = 10^{-36} capture per second and target atom

The detection of solar neutrinos (2)

- Radiochemical experiments with gallium: **SAGE** and **GALLEX**
 - Reaction: $\nu_e + {}^{71}\text{Ga} \rightarrow {}^{71}\text{Ge} (T_{1/2} = 11.4 \text{ d}) + e^-$ (threshold $E_\nu = 0.23 \text{ MeV}$)
 - sensitive to pp neutrinos
 - Results: 40 % of the expected signal
- Real-time detection of (mostly) e- neutrinos: **Kamiokande** (700 tons of water, 1983 – 1996), **Super-Kamiokande** (50 kt, 1996 –)
 - Reaction: $\nu_e + e^- \rightarrow \nu_e + e^-$ (emission of Cherenkov light)
 - Results: 40 % of the expected signal



Solution to the solar neutrino problem

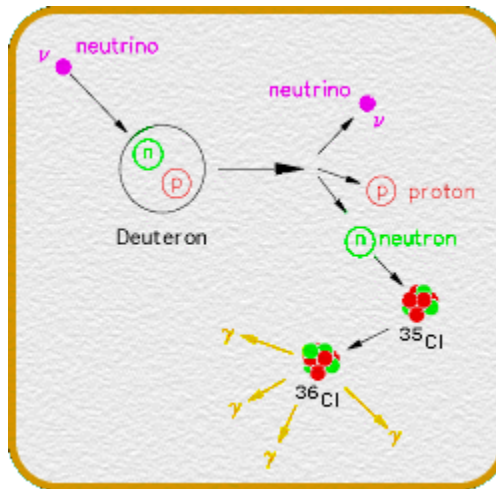
Possible origin of the deficit

- Problem with the standard solar model? (3% of error on $T_c \rightarrow$ a factor of 2 in N_ν)
- Problem with the nuclear data? ${}^7\text{Be}(p,\gamma){}^8\text{B}$ cross-section
- New physics of neutrino \rightarrow **oscillation** $\nu_e \rightarrow \nu_\mu, \nu_\tau$?

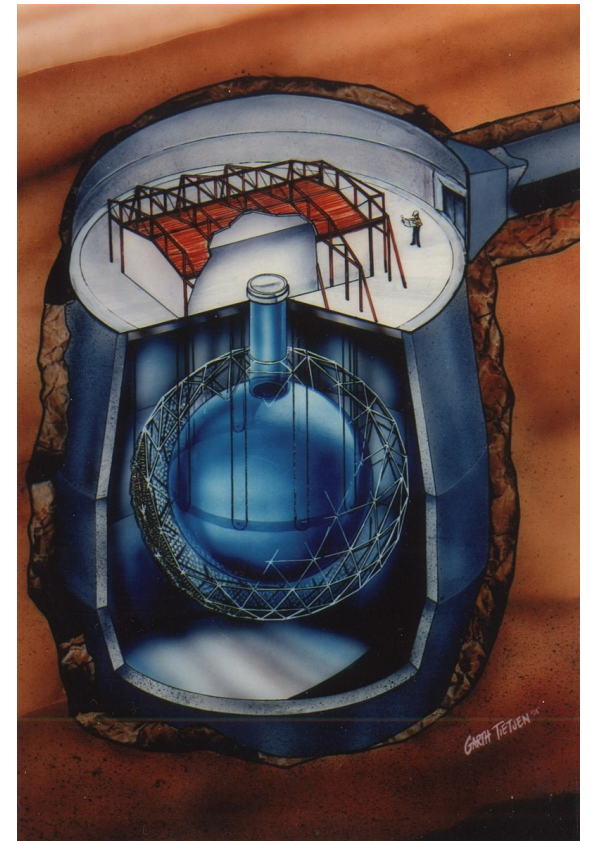
SNO: Sudbury Neutrino Observatory

- 1100 tons of D_2O (99.9%)
- Sensitive to the three neutrino flavors
 $\rightarrow \nu_x + d \rightarrow p + n + \nu_x$
(neutral current)

(Bellerive+, NPB, 2016)



- Results: $\phi_{\text{NC}} = 5.21 \pm 0.27$ (stat) ± 0.39 (sys) SNU
in agreement with $\phi_{\text{SSM}} = 5.05^{+1.01}_{-0.81}$ SNU



4.2 Quiescent helium burning

- **Where does it take place?**
 - Core of horizontal branch stars (100 – 400 MK)
 - Burning shell in AGB stars (45 – 100 MK)
- **Main nucleosynthesis products**
 ^4He transformed in ^{12}C and ^{16}O for stars of more than $\sim 0.5 M_{\odot}$
- **How does it work?**
Mainly three reactions:
 - $\alpha + \alpha + \alpha \rightarrow ^{12}\text{C}$ $Q = 7.3 \text{ MeV}$
 - $^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$ $Q = 7.2 \text{ MeV}$
 - $^{16}\text{O}(\alpha, \gamma)^{20}\text{Ne}$ $Q = 4.7 \text{ MeV}$
- **Who & when?**
 - Triple alpha process: Öpik (1951), Salpeter (1952)
 - The “Hoyle” state in ^{12}C : Hoyle (1953)



Fred Hoyle (1915 – 2001)

The triple alpha process

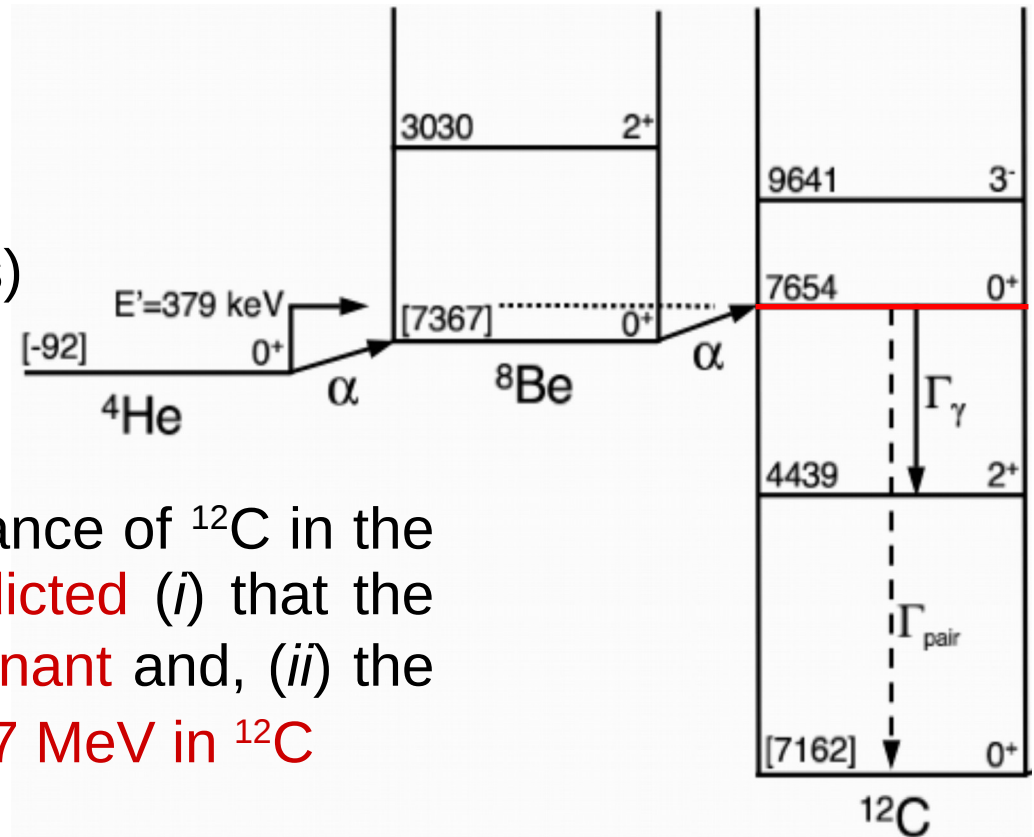
How are synthesized elements heavier than ${}^4\text{He}$, given that there are **no stable isotopes** for mass $A = 5$ ($p+\alpha$) and $A = 8$ ($\alpha+\alpha$)?

- Fusion of 3α in ${}^{12}\text{C}$ in two steps

- $\alpha + \alpha \leftrightarrow {}^8\text{Be}$ $Q = -92 \text{ keV}$

(${}^8\text{Be}$ is unstable $\tau = 9.7 \times 10^{-17} \text{ s}$)

- $\alpha + {}^8\text{Be} \rightarrow {}^{12}\text{C}^*$



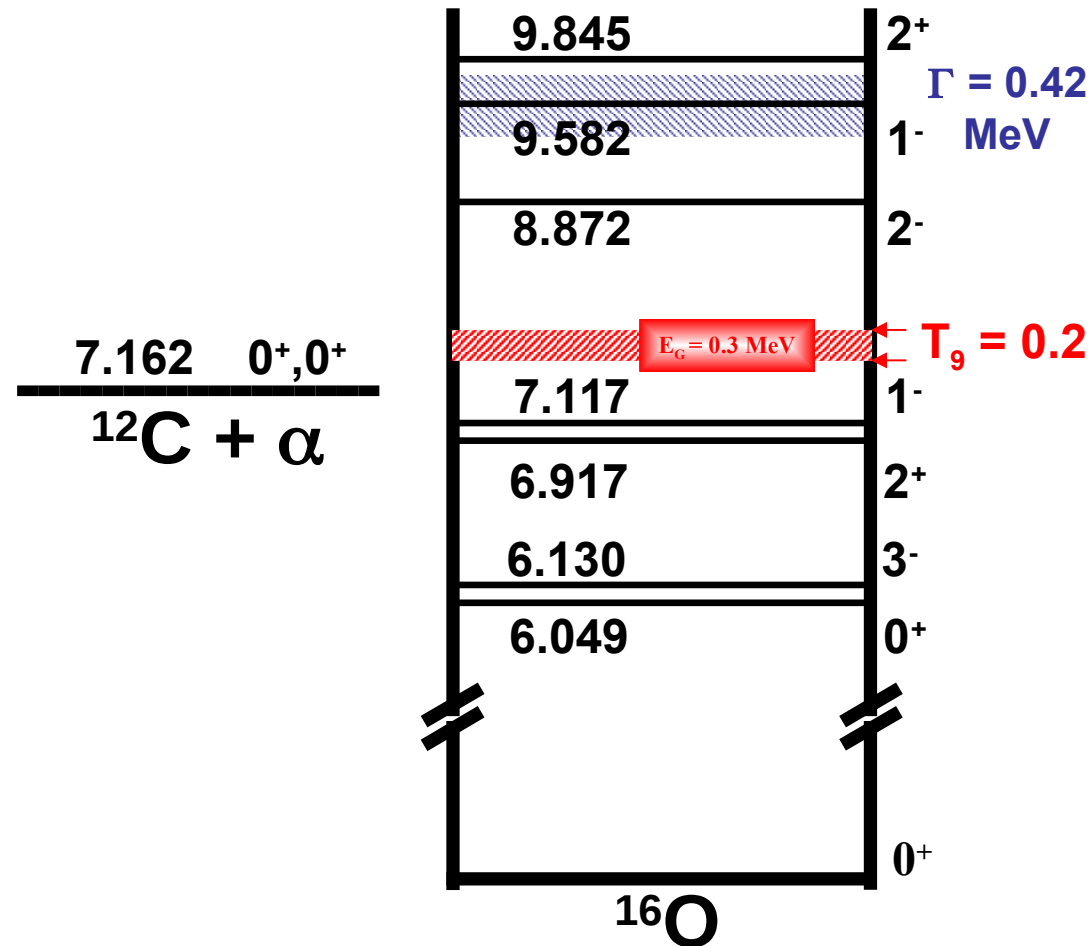
- In view of the significant abundance of ${}^{12}\text{C}$ in the Universe (!), Hoyle (1953) **predicted** (i) that the reaction $\alpha + {}^8\text{Be} \rightarrow {}^{12}\text{C}^*$ is **resonant** and, (ii) the **existence of a $J^\pi = 0^+$ state at 7.7 MeV in ${}^{12}\text{C}$**

- Experimental verification in 1953 and 1957

The $^{12}\text{C}(\alpha,\gamma)^{16}\text{O}$ reaction

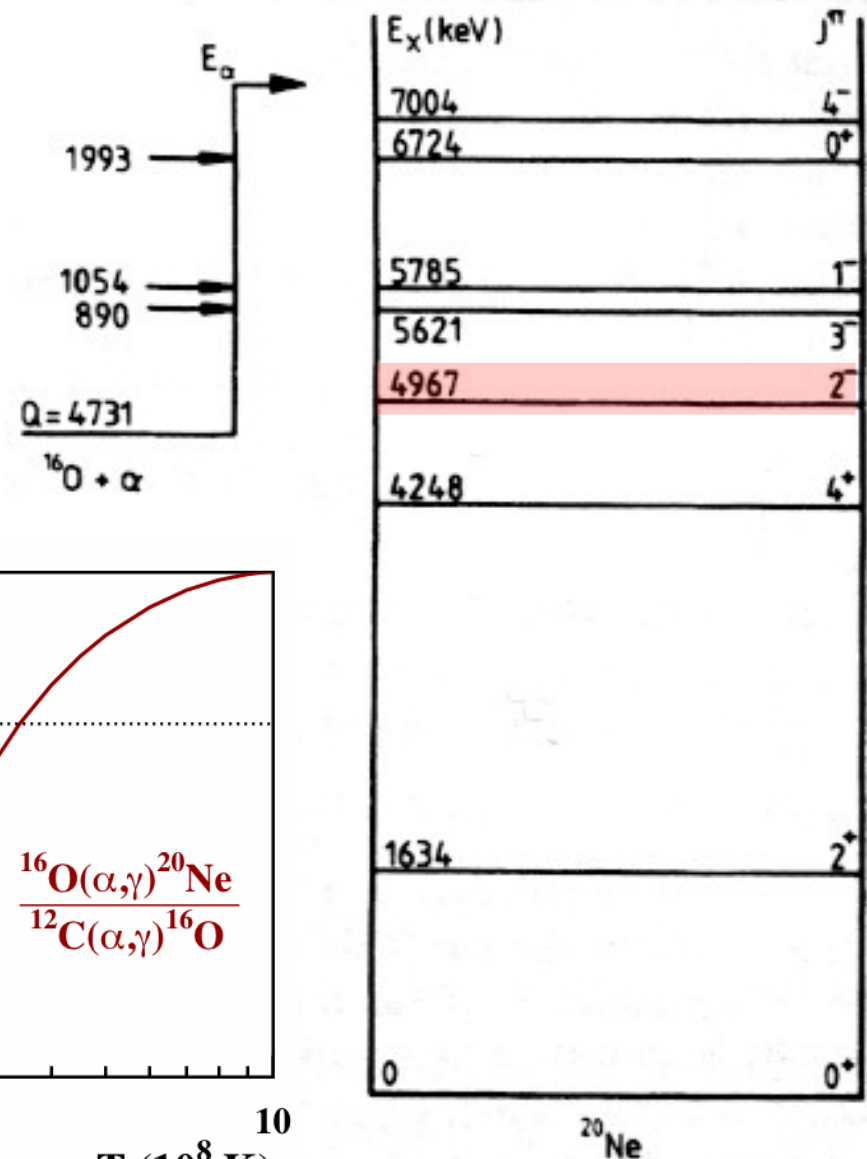
Slow and crucial reaction → Holy Grail in nuclear astrophysics

- The rate of this reaction determines the $^{12}\text{C}/^{16}\text{O}$ ratio at the end of the helium burning phase, and thus the subsequent burning stages in massive stars
- $^{12}\text{C}/^{16}\text{O}$ influences the nature of the remnant (neutron star? Black hole?) left after a core-collapse supernova
- A difficult case: contribution from a broad state, two sub-threshold resonances and the direct capture process.
- Cross-section at 300 keV
→ $\sigma \approx 10^{-17}$ b! (can't be measured, less than 1 event per year)



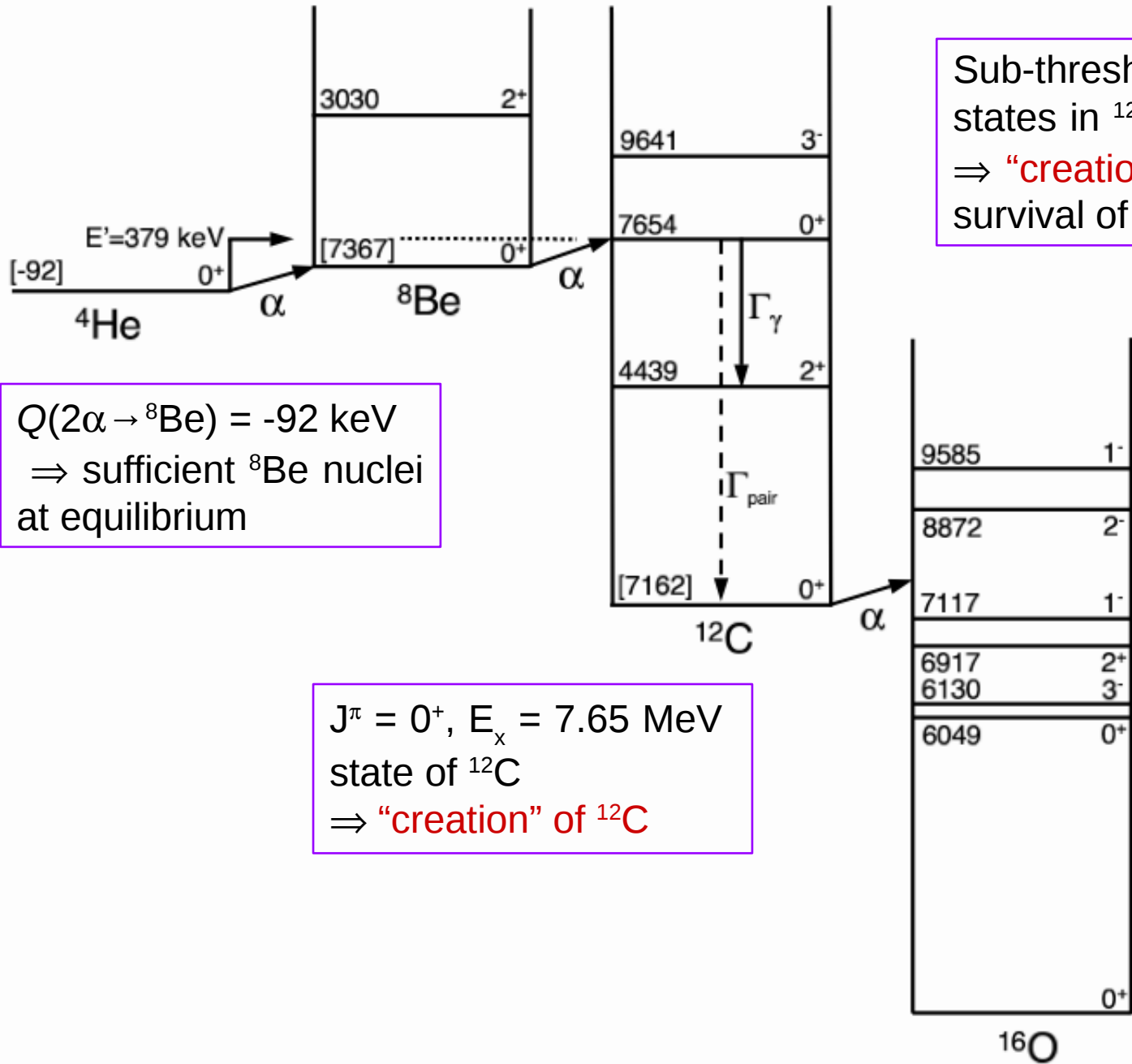
The $^{16}\text{O}(\alpha, \gamma)^{20}\text{Ne}$ reaction

- **Very slow reaction** because no resonant state in the energy range of interest $5.0 \text{ MeV} < E_x(^{20}\text{Ne}) < 5.2 \text{ MeV}$ (the $J^\pi = 2^-$ state at $E_x = 4967 \text{ keV}$ being of **non-natural parity**)



- Reaction rate \ll rate of $^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$ for $T < 0.3 \text{ GK}$
 - \Rightarrow **end of the helium burning phase** in stellar cores
 - \Rightarrow **survival of ^{16}O**

How insignificant we are!



Sub-threshold 1^- and 2^+ states in $^{12}\text{C} + \alpha \rightarrow ^{16}\text{O} \Rightarrow$ "creation" of ^{16}O but survival of ^{12}C

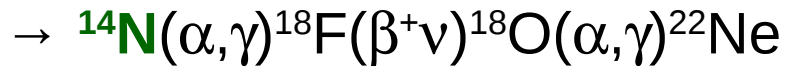
$Q(2\alpha \rightarrow ^8\text{Be}) = -92$ keV \Rightarrow sufficient ^8Be nuclei at equilibrium

$J^\pi = 0^+$, $E_x = 7.65$ MeV state of $^{12}\text{C} \Rightarrow$ "creation" of ^{12}C

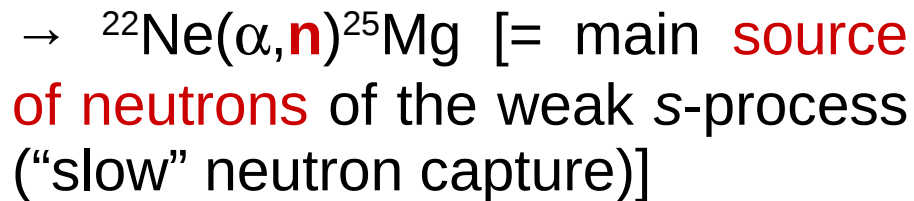
^{20}Ne state at 4.97 MeV of non-natural parity (2^-) \Rightarrow survival of ^{16}O

Other reactions

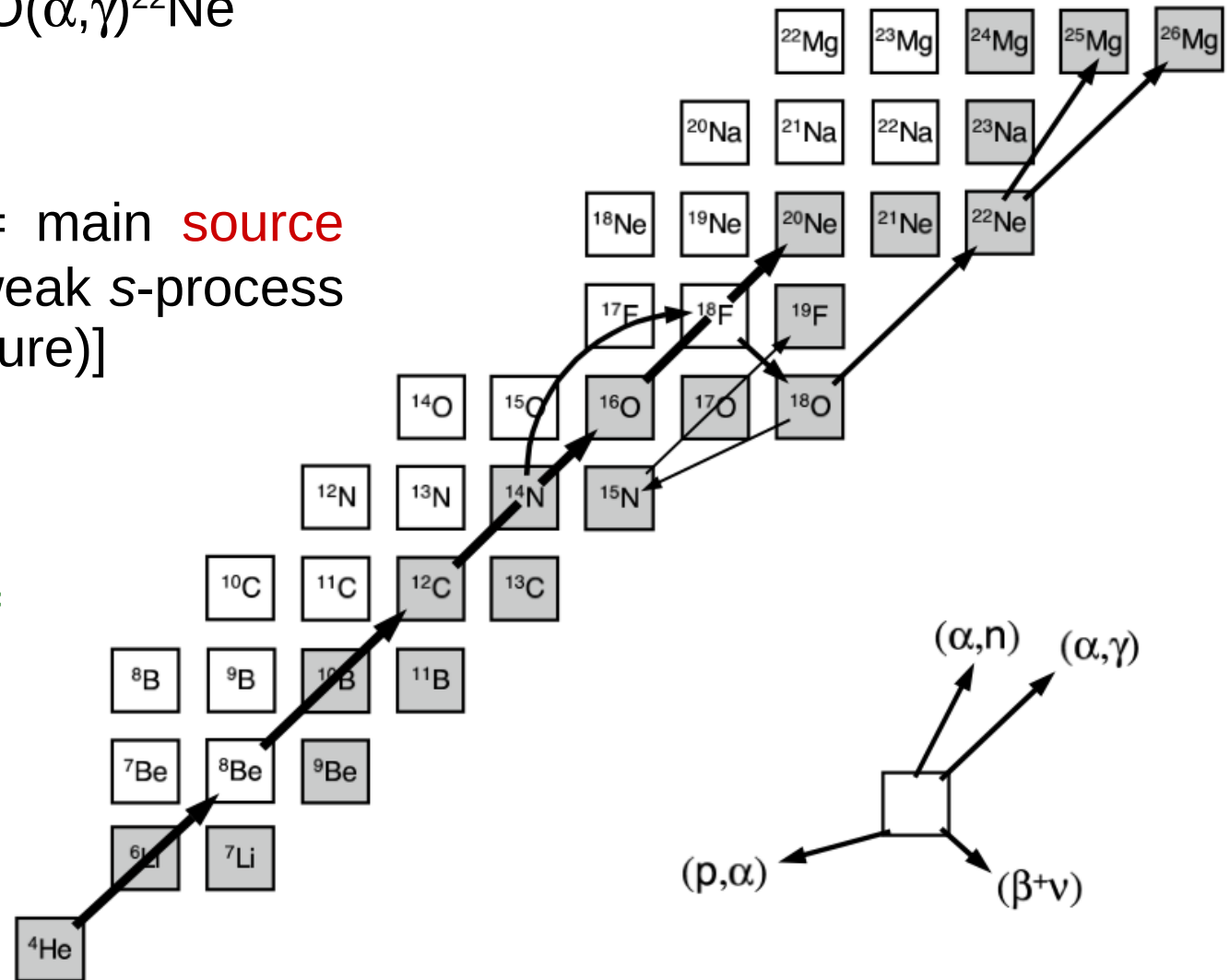
- ^{14}N is the main “ash” from the CNO cycle, and accounts for 1-2% of the mass of the fusion core at the end of H burning (pop I stars)



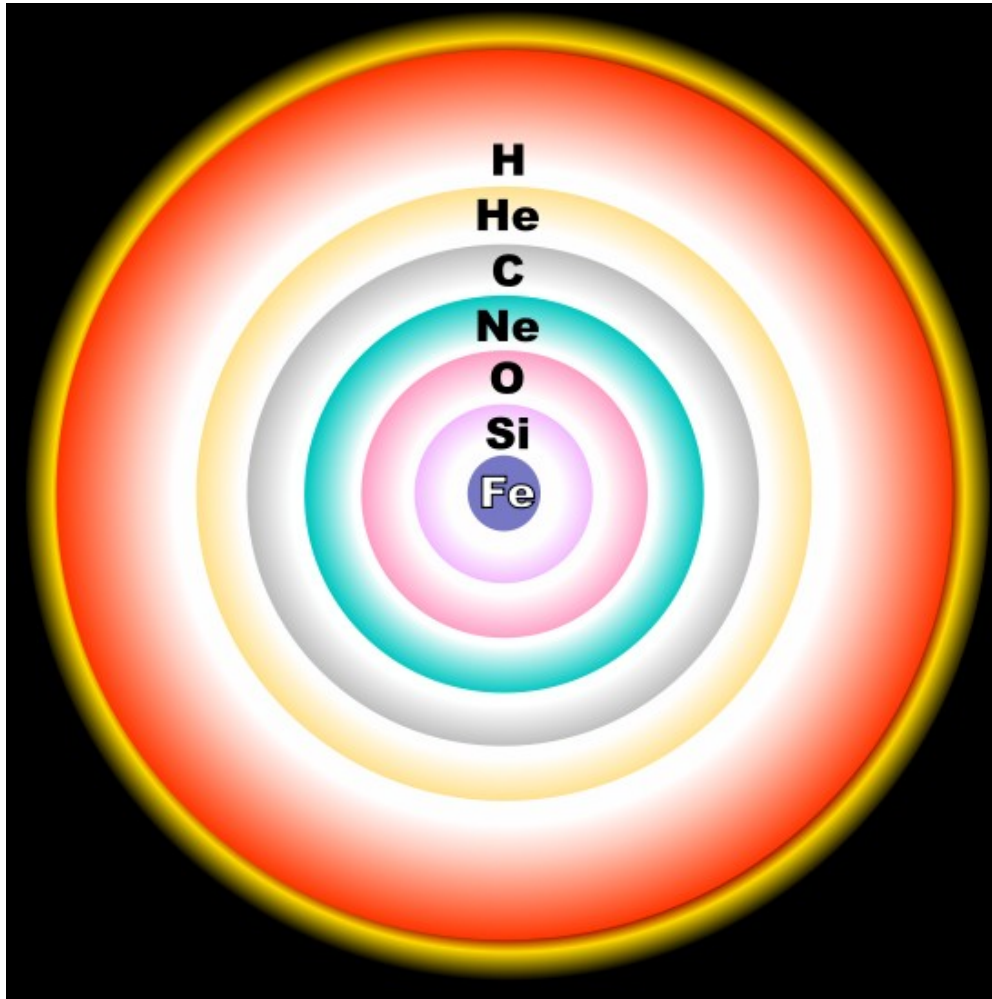
followed by



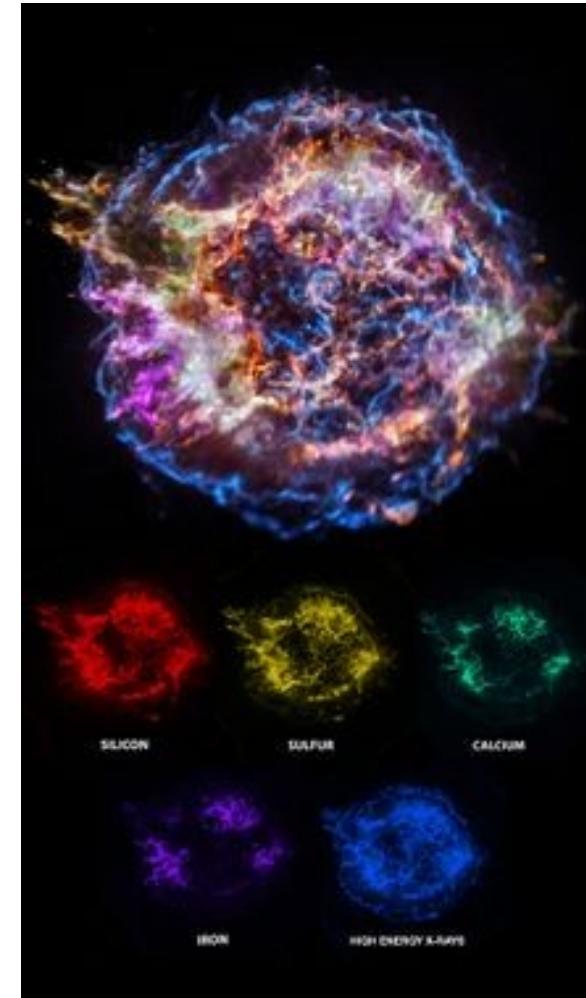
- Helium burning is the main source of ^{12}C , ^{16}O , ^{18}O and ^{22}Ne in the Universe



4.3 Advanced nuclear burning phases



Schematic diagram of the “onion-skin” structure of a pre-supernova



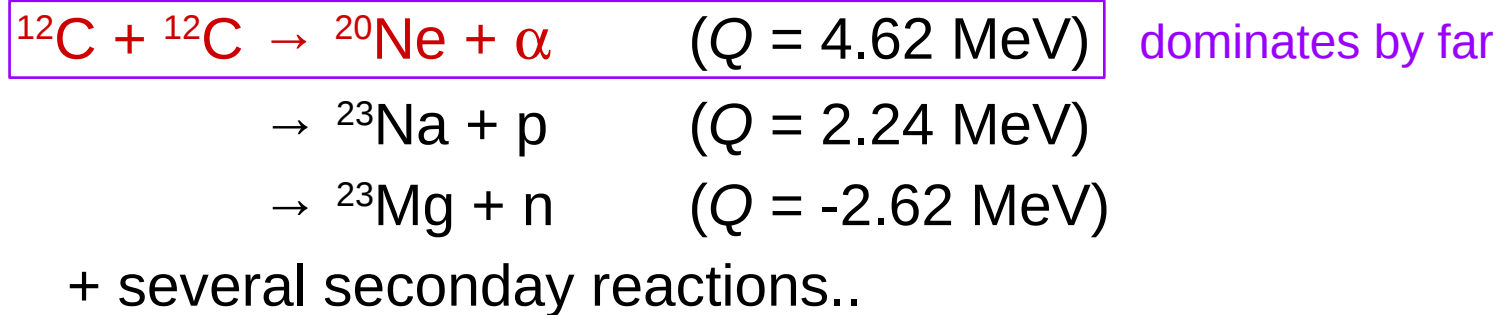
Chandra X-ray observatory image of the SN remnant Cassiopeia A

Carbon burning

- When?

- He exhausted in the stellar core → mainly ^{12}C and ^{16}O ashes → gravitational contraction → increase of temperature
- $T_c \sim (5 - 9) \times 10^8 \text{ K}$ and $\rho > 2 \times 10^5 \text{ g cm}^{-3}$ for $M \geq 8 M_\odot$

- Major reaction sequences



- Composition at the end of core carbon burning

- Mainly ^{20}Ne with some $^{21,22}\text{Ne}$, ^{23}Na , $^{24,25,26}\text{Mg}$ and $^{26,27}\text{Al}$
- ^{16}O not burning yet.... → amount comparable with ^{20}Ne

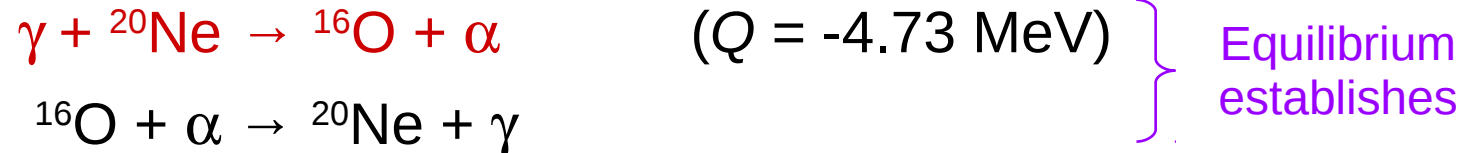
Neon burning

- When?

- After carbon burning → mainly ^{20}Ne ashes → the core further contracts → increase of temperature
- $T_c \sim (1 - 2) \times 10^9 \text{ K}$ and $\rho \sim 10^6 \text{ g cm}^{-3}$ for $M \geq 11 M_\odot$

- Major reaction sequences

Temperatures are high enough to initiate **photodisintegration processes**



followed by e.g. the ${}^{20}\text{Ne}(\alpha, \gamma){}^{24}\text{Mg}(\alpha, \gamma){}^{28}\text{Si}$ sequence

- Composition at the end of core neon burning

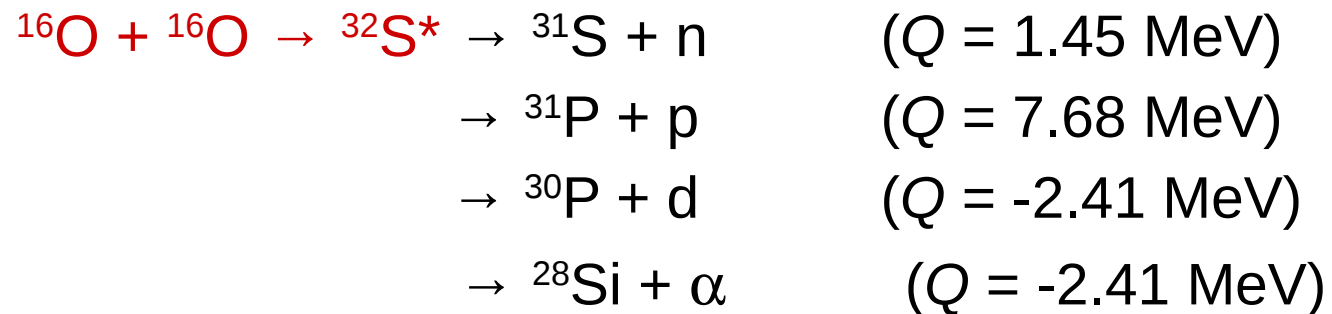
- Mainly ${}^{16}\text{O}$ with some ${}^{24}\text{Mg}$ and ${}^{28}\text{Si}$

Oxygen burning

- When?

- After neon burning the core further contracts
- $T_c \sim (2 - 3) \times 10^9$ K and $\rho \sim 3 \times 10^6$ g cm⁻³ for $M \geq 11 M_\odot$

- Major reaction sequences



+ recapture of n, p, d and α -particles

- Composition at the end of oxygen burning

- The most abundant nuclides are ${}^{28}\text{Si}$ and ${}^{32}\text{S}$

Silicon burning

- **When?**

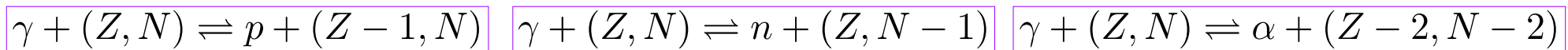
- After oxygen burning the core further contracts and the temperature increases
- $T_c \sim (2.8 - 4.1) \times 10^9$ K and $\rho \sim 3 \cdot 10^7$ g cm⁻³ for $M \geq 11 M_\odot$

- **Photodisintegration**

- Starts with ²⁸Si: $^{28}\text{Si}(\gamma, \alpha)^{24}\text{Mg}(\gamma, \alpha)^{20}\text{Ne}(\gamma, \alpha)\dots$
- **Photodisintegration rearrangement**: destruction of less tightly bound species and capture of released n, p, α -particles to synthesize more tightly bound species

- **Nuclear Statistical Equilibrium (NSE)** is achieved for many reactions

- NSE = both photodisintegration and capture rates are fast



- Equilibrium drives towards $A = 56$ → most stable nuclide (higher binding energy)
- **Synthesis of nuclei from Si to Zn (“iron peak” elements Ti to Zn)**
- **Composition at the end of silicon burning: ⁵⁶Fe** → formation of an iron core

Summary

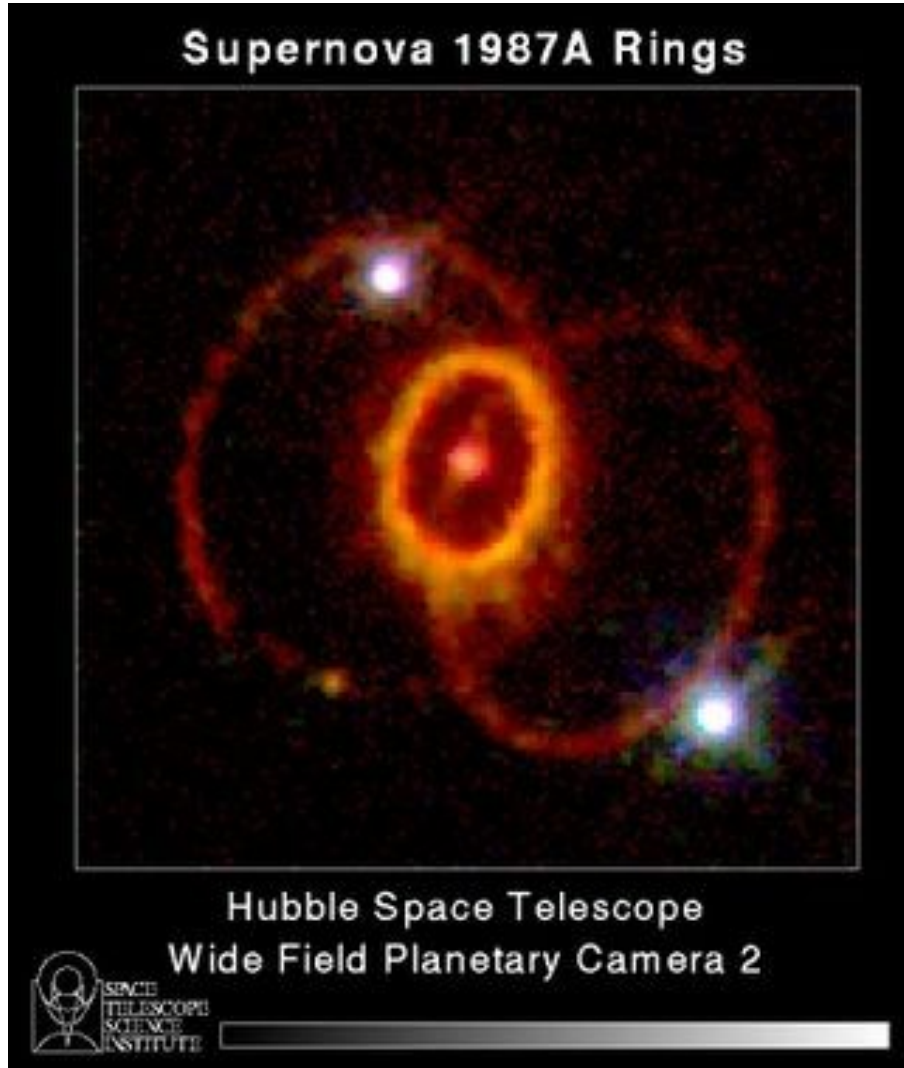
Stellar mass (M_{\odot})	Stage reached
< 0.08	no thermonuclear fusion
0.1 - 0.5	H burning
0.5 - 8	He burning
8 - 11	C burning
> 11	all stages

Evolution stages of a 25 M_{\odot} star

Stage reached	Timescale	T_{core} (10^9 K)	Density (g cm^{-3})
H burning	7×10^6 y	0.06	5
He burning	5×10^5 y	0.23	7×10^2
C/O burning	600 y / 6 months	0.93 – 2.3	$2 \times 10^5 - 1 \times 10^7$
Si melting	1 d	4.1	3×10^7
Explosive burning	0.1 – 1 s	1.2 - 7	varies

4.4 Explosive nucleosynthesis

Massive stars

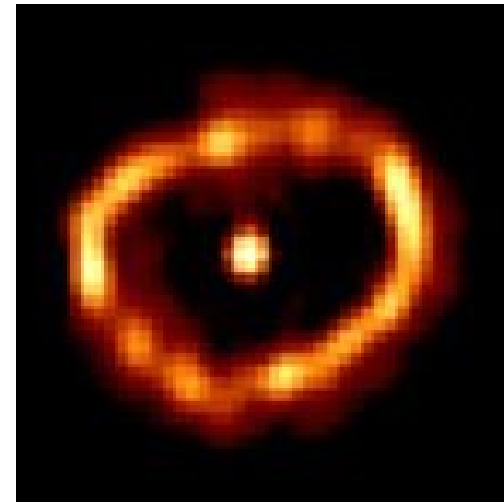


Binary systems



Type Ia supernova

G299 (Chandra X-ray observatory)

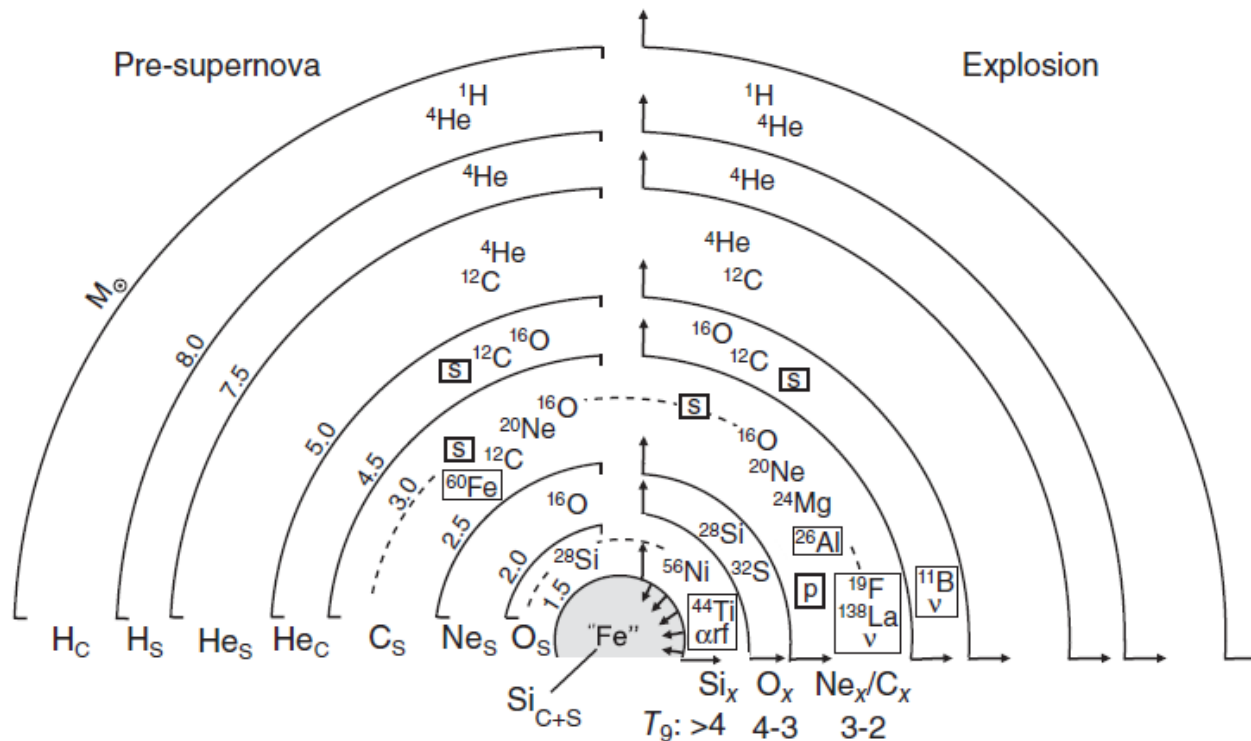


Classical nova

Nova Cygni 1992 (HST)

Core collapse supernova (1)

“Onion shell” structure of massive stars



Explosion:

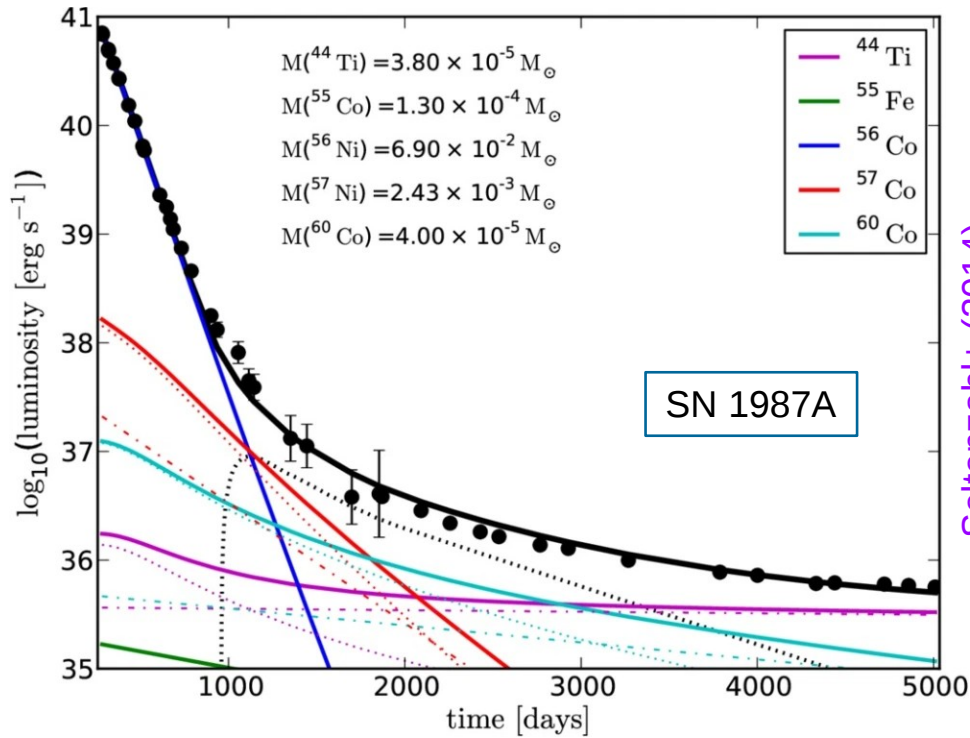
- **Core in NSE**, grows in mass until $\sim 1.4 M_{\odot}$, electron degeneracy pressure unable to counteract gravity...
- Collapse starts, enhanced by photodisintegration (e.g. $\gamma + ^{56}\text{Fe} \rightarrow 13 ^4\text{He} + 4n$) and electron capture ($e^- + (Z,N) \rightarrow \nu_e + (Z-1,N+1)$)
- When $\rho \sim 10^{14} \text{ g/cm}^3$ nuclei feel short-range nuclear force \rightarrow inner part of core rebounds \rightarrow **outward moving shock**

Explosive nucleosynthesis: induced by **neutrinos** and **outward moving shock** (mainly in Si, O and Ne/C layers)

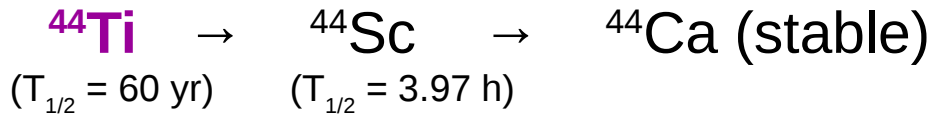
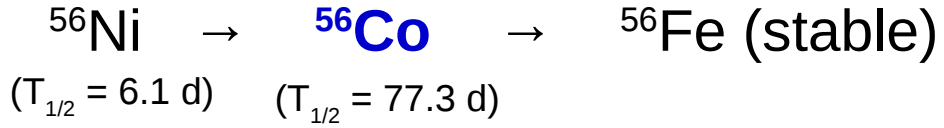
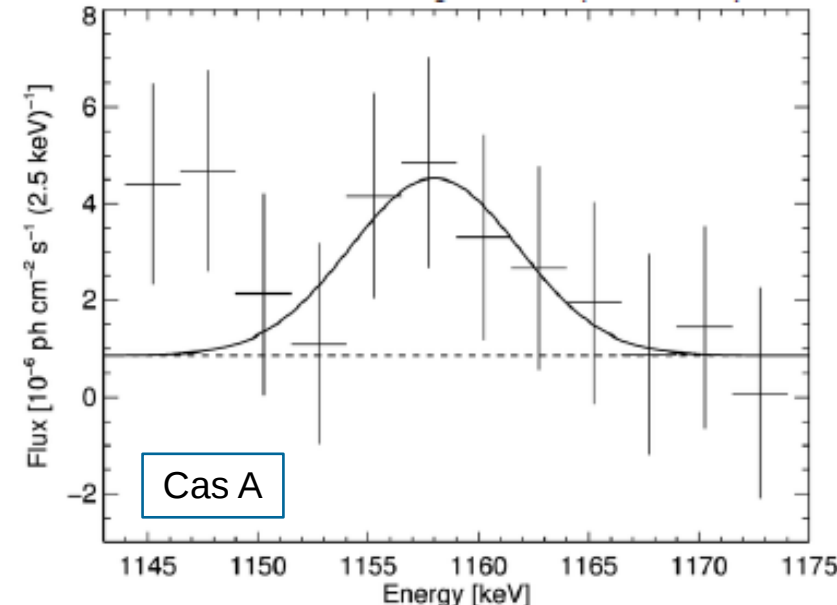
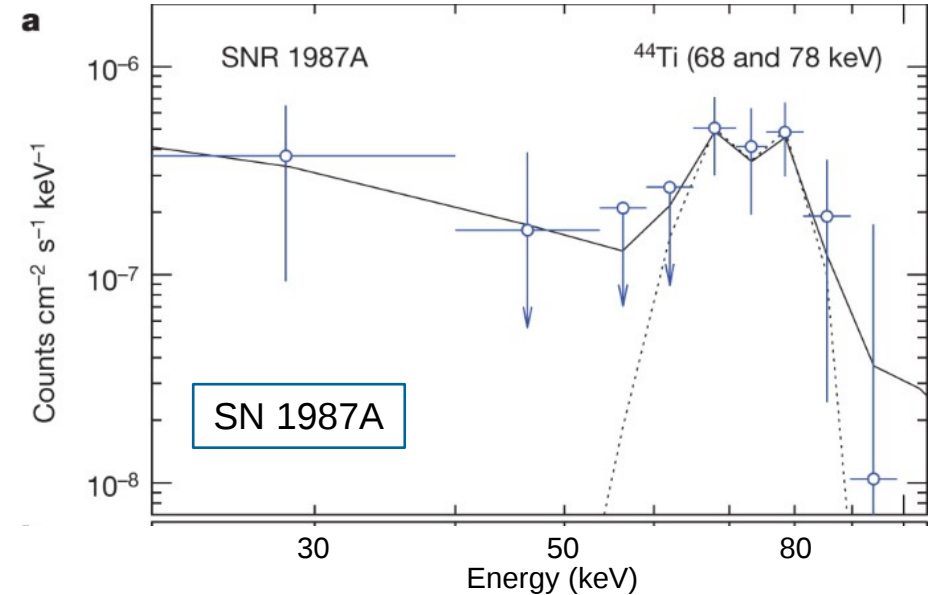
Core collapse supernova (2)

Light curve powered by radioactive decay

^{44}Ti observations from SN remnants



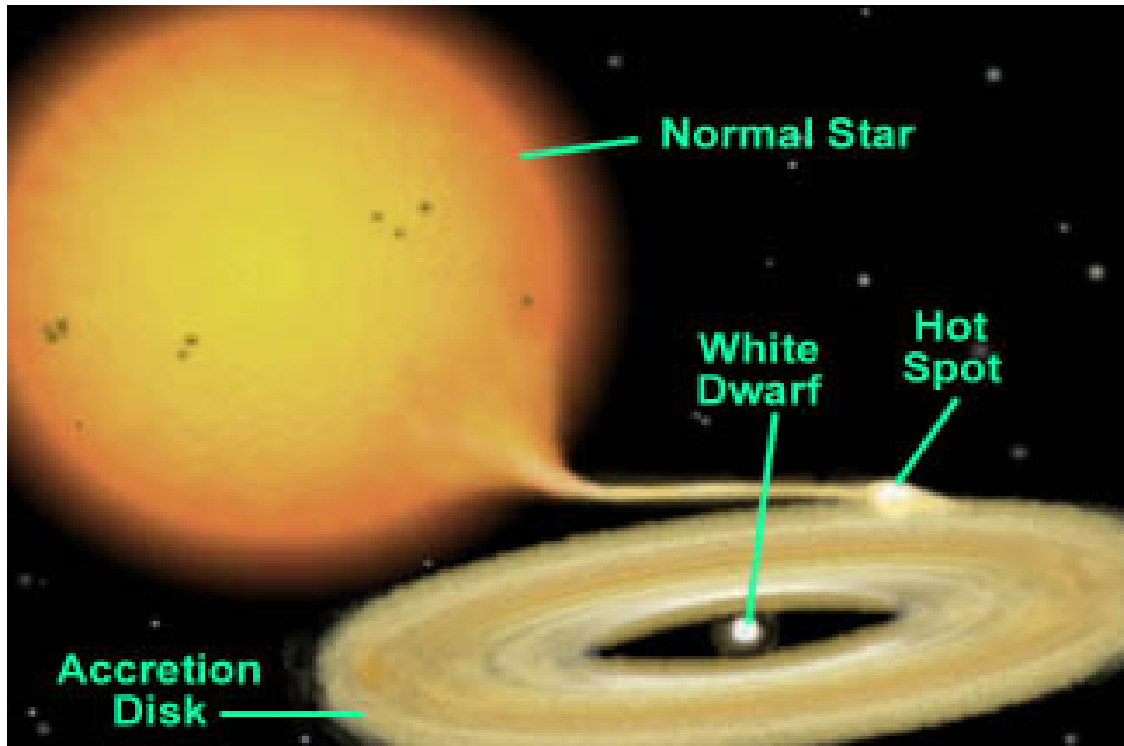
Seltenzahl+ (2014)



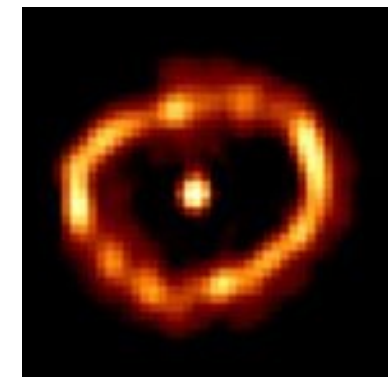
Classical novae (1)

Sudden increase in star's luminosity ($L \sim 10^4 - 10^6 L_{\odot}$, and $t \sim 1\text{h} - 1\text{d}$)

Final evolution of a close binary system



- **H-rich material transfer** from normal star to white dwarf (WD)
- T and ρ increase at surface of WD
- Start and **thermonuclear runaway** ($T \approx 50 - 300 \text{ MK}$)
→ cataclysmic explosion
- **Ejection** of part of the accreted material

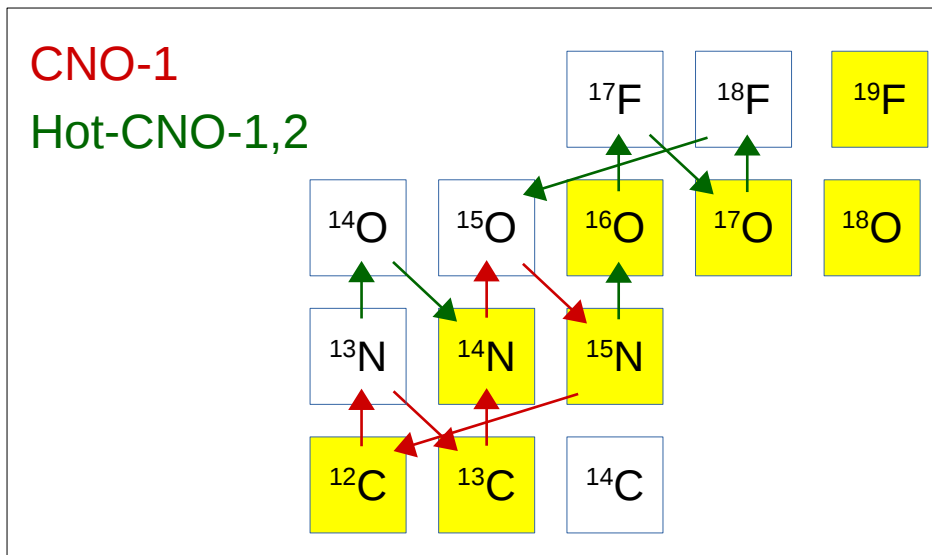


	novae	ccSN
$M_{\text{ej}} (M_{\odot})$	$\sim 10^{-5}$	~ 10
$f (\text{yr}^{-1} \text{ galaxy}^{-1})$	~ 30	$\sim 10^{-2}$
$L (L_{\odot})$	$\sim 10^5$	$\sim 10^{11}$
Nucleosynthesis	$^{13}\text{C}, ^{15}\text{N}, ^{17}\text{O}$	$\sim \text{all}$

Classical novae (2)

Shell ejection

The energy release from the β^+ -decays (^{13}N , ^{14}O , ^{15}O , ^{17}F) throughout the envelope helps to eject the material from the WD



$$T_{1/2}(^{13}\text{N}) = 9.965 \text{ min}$$

$$T_{1/2}(^{15}\text{O}) = 122.24 \text{ s}$$

$$T_{1/2}(^{17}\text{F}) = 64.49 \text{ s}$$

$$T_{1/2}(^{18}\text{F}) = 109.77 \text{ min}$$

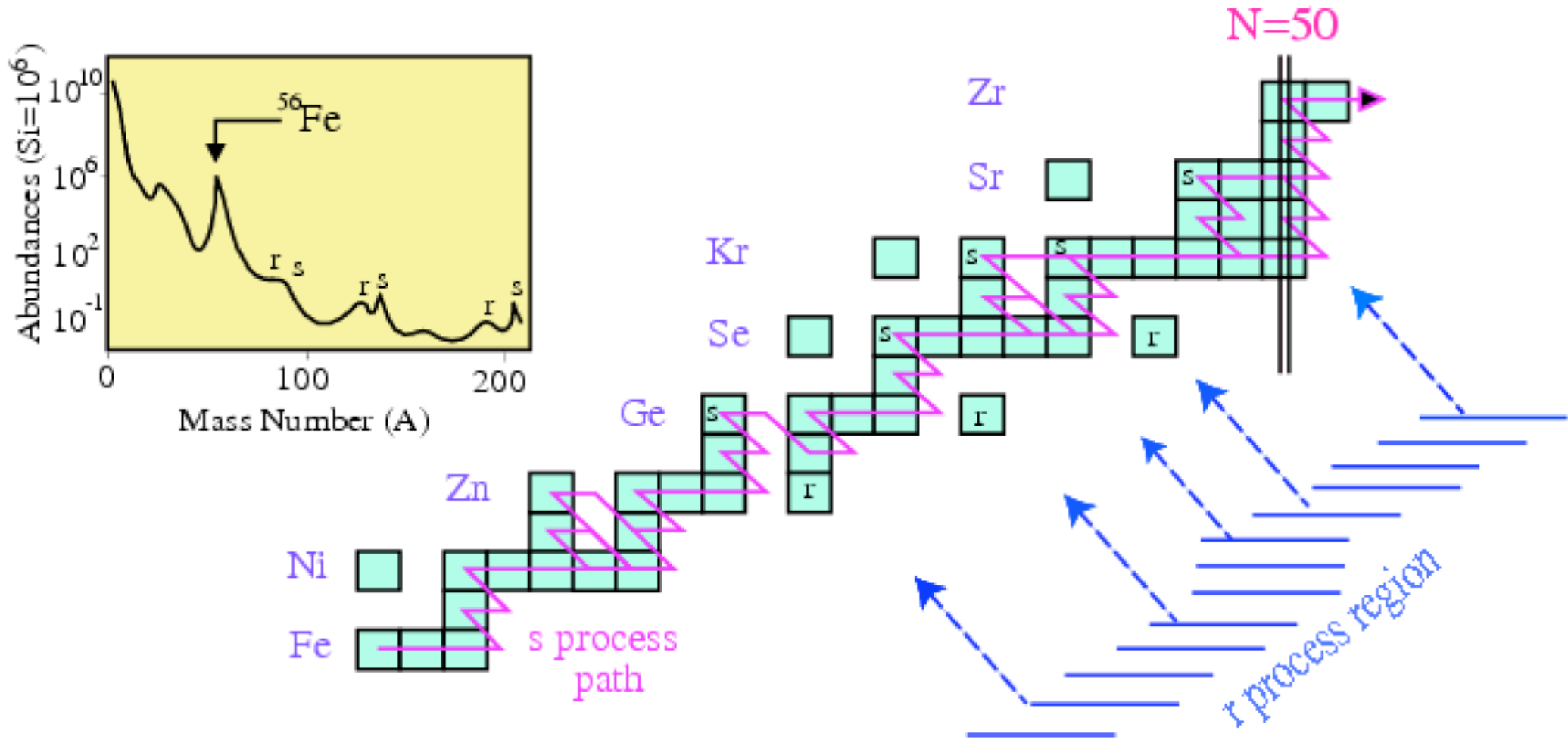
End-point of nucleosynthesis: $A \sim 40$ (Ca)

- $T_{peak} \sim 300 - 400 \text{ MK}$
- **(p, γ) reactions** on the proton-rich side
- Coulomb barrier too high to overcome for $A \geq 40$

Nucleosynthesis of γ -ray emitters

- ^{18}F ($T_{1/2}=110 \text{ min}$); 511 keV
- ^{22}Na ($T_{1/2}=2.6 \text{ yr}$); 1275 keV
- ^{26}Al ($T_{1/2}=0.7 \text{ Myr}$); 1809 keV

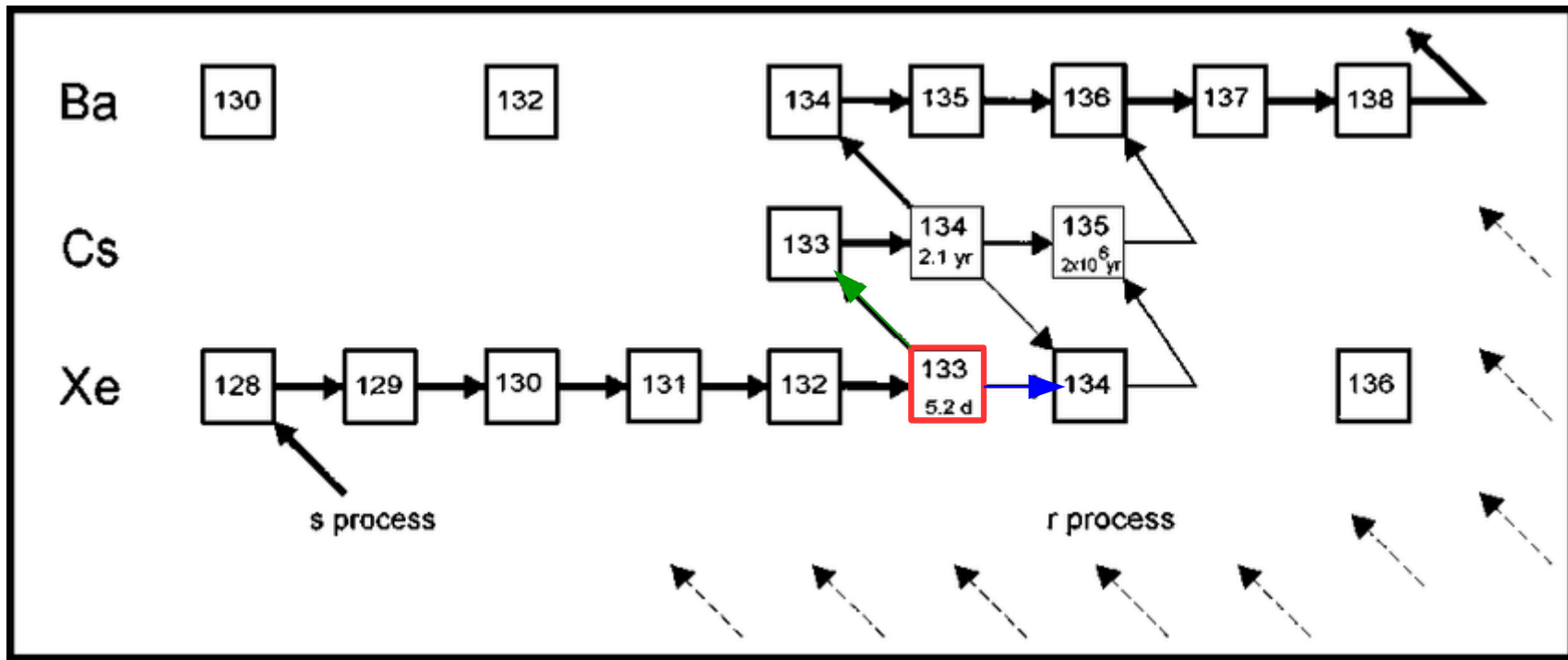
4.5 Nucleosynthesis beyond iron



Elements heavier than iron can't be synthesized by fusion reactions

Neutron capture reactions

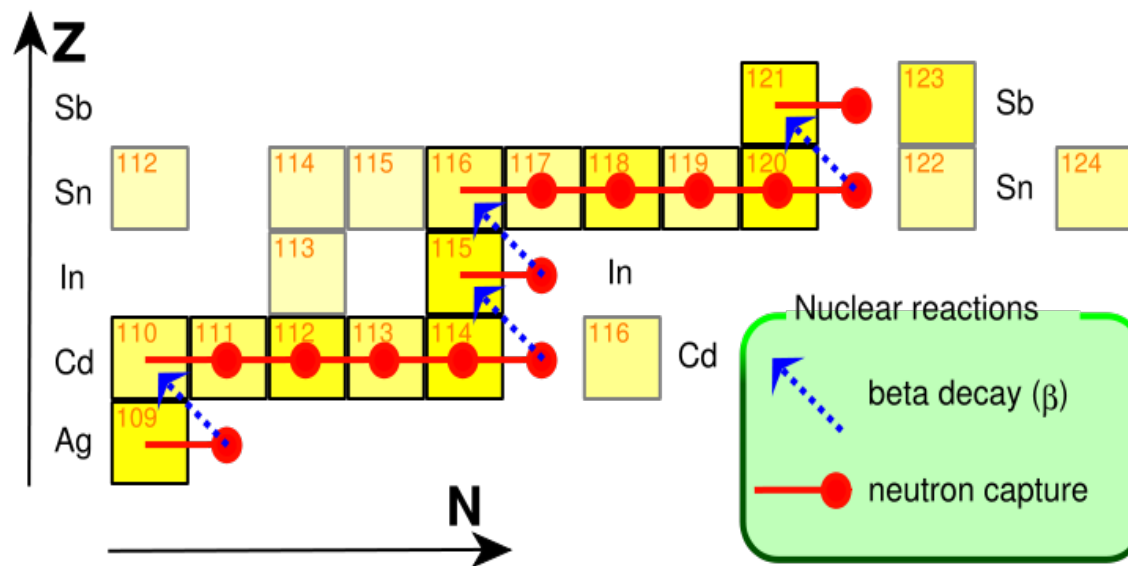
- Radiative neutron captures [(n,γ) reactions] in competition with β⁻ decay
- Process starts with Fe seeds



- Mean lifetime for neutron capture $\tau_n = \frac{1}{N_n \langle \sigma v \rangle}$ to be compared to β⁻-decay lifetime τ_β (from seconds to years)
 - If $\tau_n > \tau_\beta \rightarrow$ unstable nuclide decays
 - if $\tau_n < \tau_\beta \rightarrow$ neutron capture
- s-process: “slow”
r-process: “rapid”

s-process

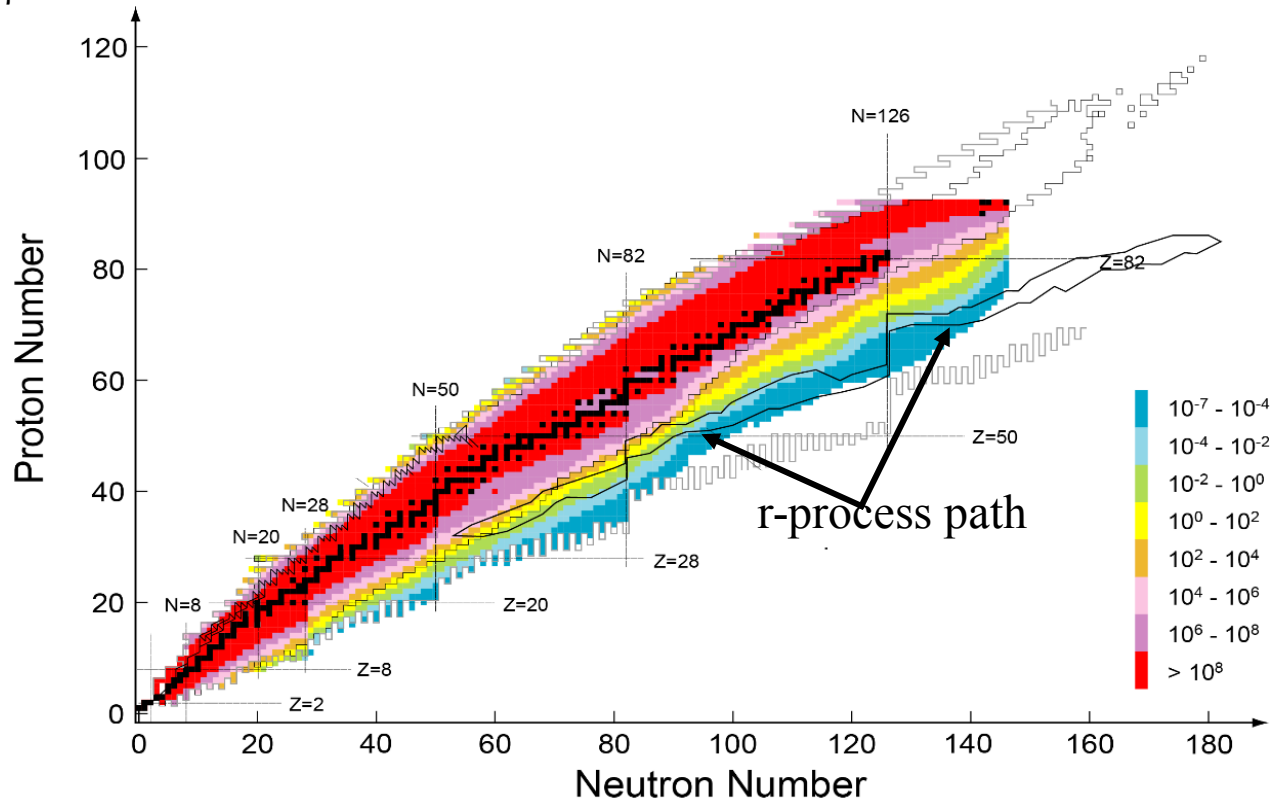
- **Slow neutron capture process**
 - Unstable nucleus decays **before** capturing another neutron
 - $\tau_n \gg \tau_\beta \iff N_n \sim 10^8 \text{ n/cm}^3$



- **Nucleosynthesis:** path along the valley of β^- stability up to ^{209}Bi (long time scale $\sim 10^4$ yr)
- **Neutron source:** $^{13}\text{C}(\alpha, n)^{16}\text{O}$ and/or $^{22}\text{Ne}(\alpha, n)^{25}\text{Mg}$
- **Quiescent scenarios:**
 - **AGB stars;** main s-process; “Ba/Pb” peaks
 - **Massive stars;** weak s-process; “Sr-Y” peak

r-process

- Rapid neutron capture process
 - Unstable nucleus captures neutron before decaying
 - $\tau_n \ll \tau_\beta \iff N_n \gg 10^{22} \text{ n/cm}^3$



- **Nucleosynthesis:** path far from the valley of β^- stability (short time scale \sim seconds)
- **Explosive scenarios:** but where?

Astrophysical site for r -process?

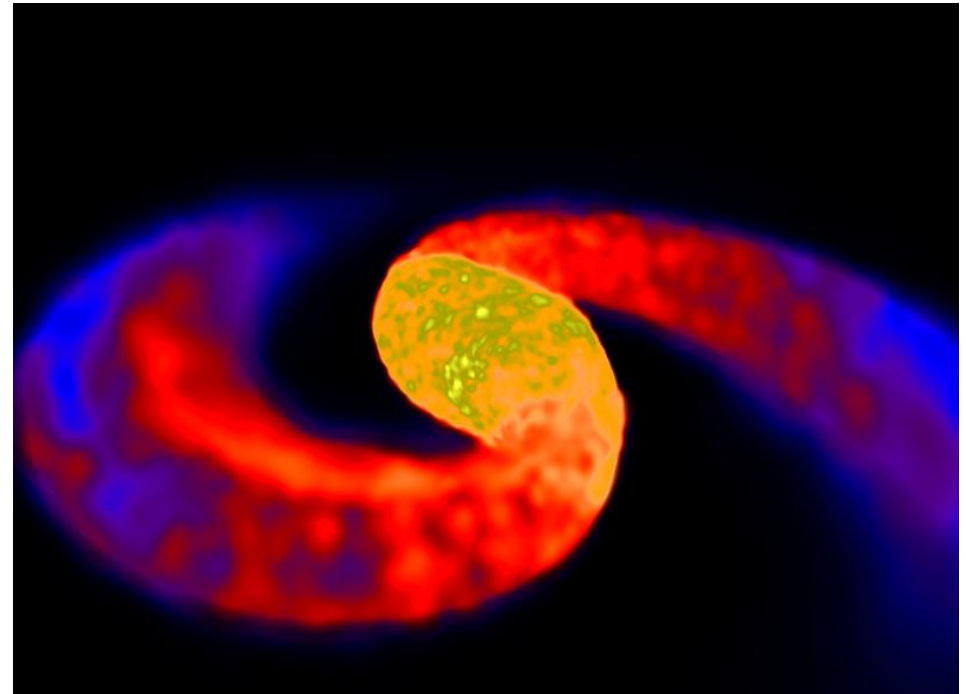
Core-collapse Supernovae?



Supernova SN1987A

- Dynamical ejecta of prompt explosions (of O-Ne-Mg cores)
- **Neutrino-driven wind** from proto-neutron stars
- ...

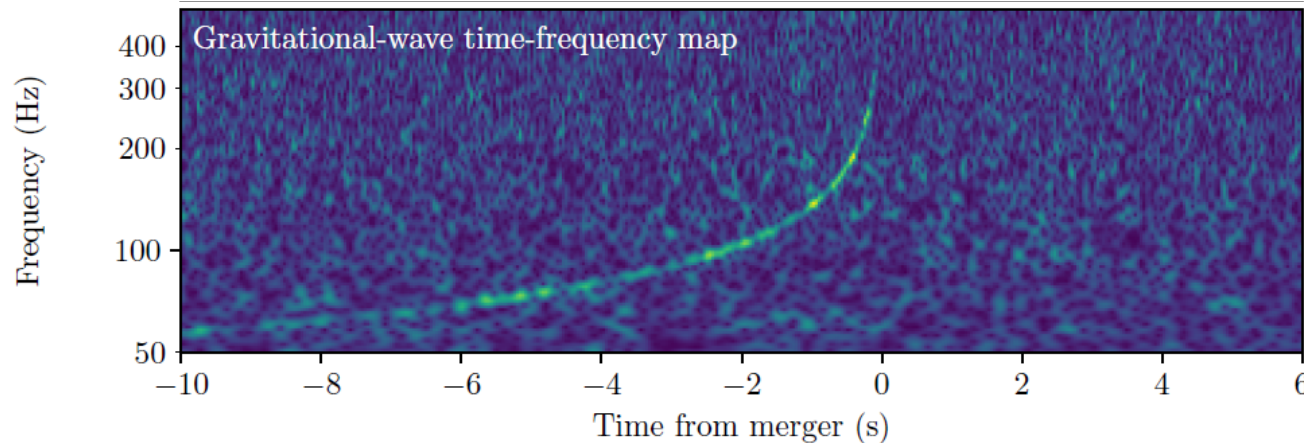
Neutron star merger?



- Mergers are expected to eject $\sim 0.01 M_{\odot}$ of very neutron-rich material
- Sources of **gravitational waves**
- Electromagnetic emission from **radioactive decay** of r -process nuclei \rightarrow **kilonova**

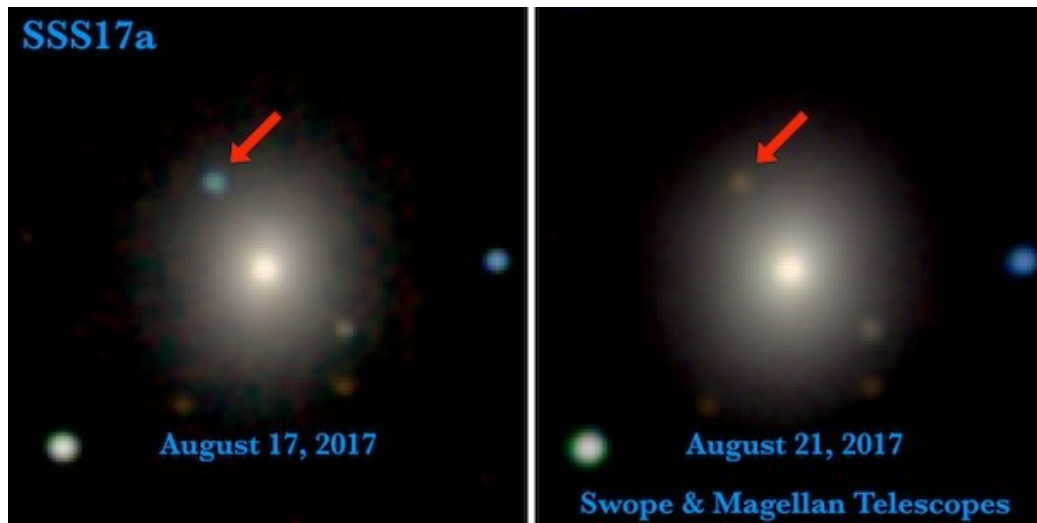
Neutron star merger GW170817

- Gravitational waves from neutron star merger detected by LIGO/VIRGO



Two neutron stars of $0.86 M_{\odot}$ and $2.26 M_{\odot}$

- Optical transient source counterpart SSS17a (Swope Supernova Survey)

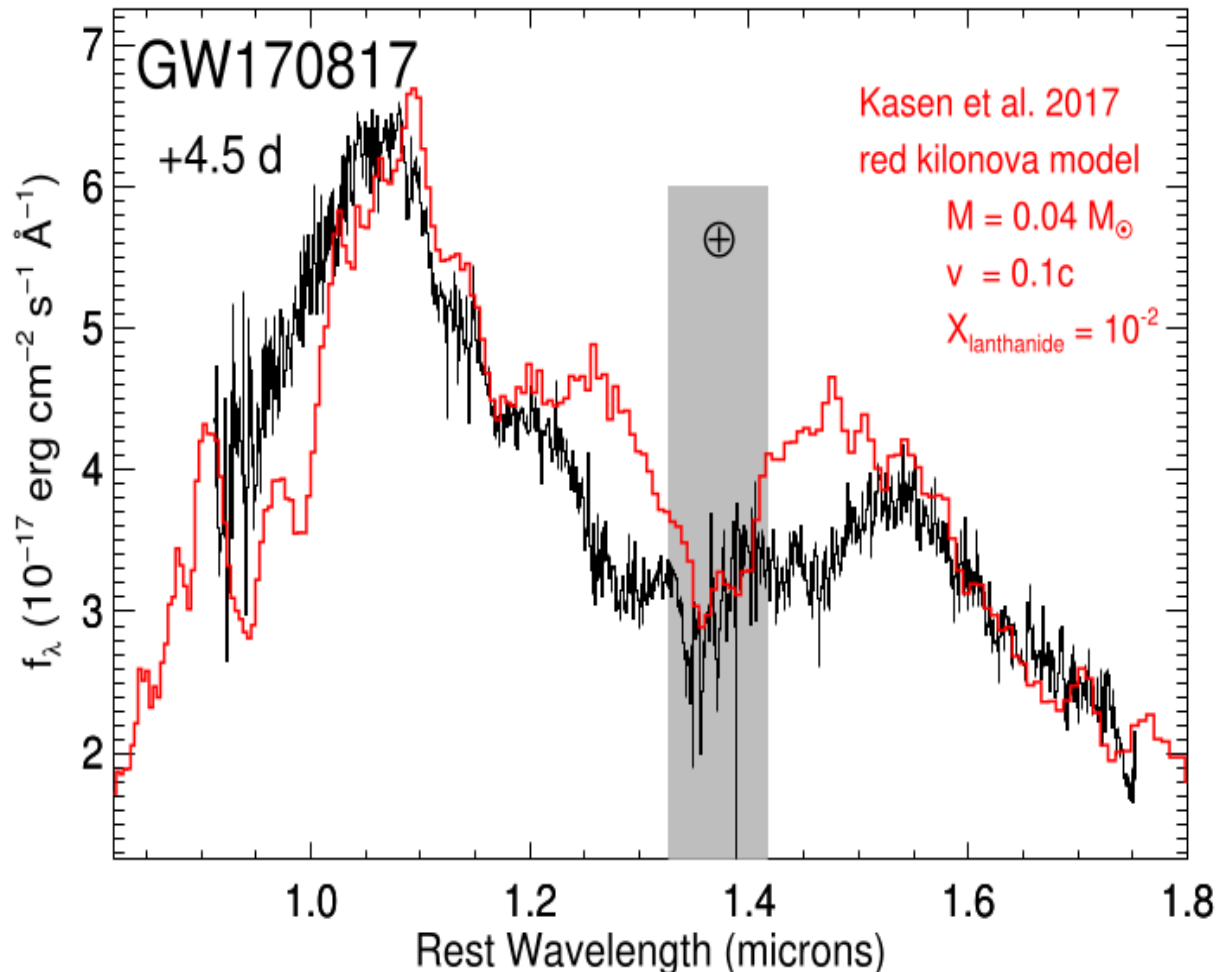


Counterpart in galaxy NGC4993 at ~ 40 Mpc

- First day
→ blue and bright
- Four days later
→ red and fainter

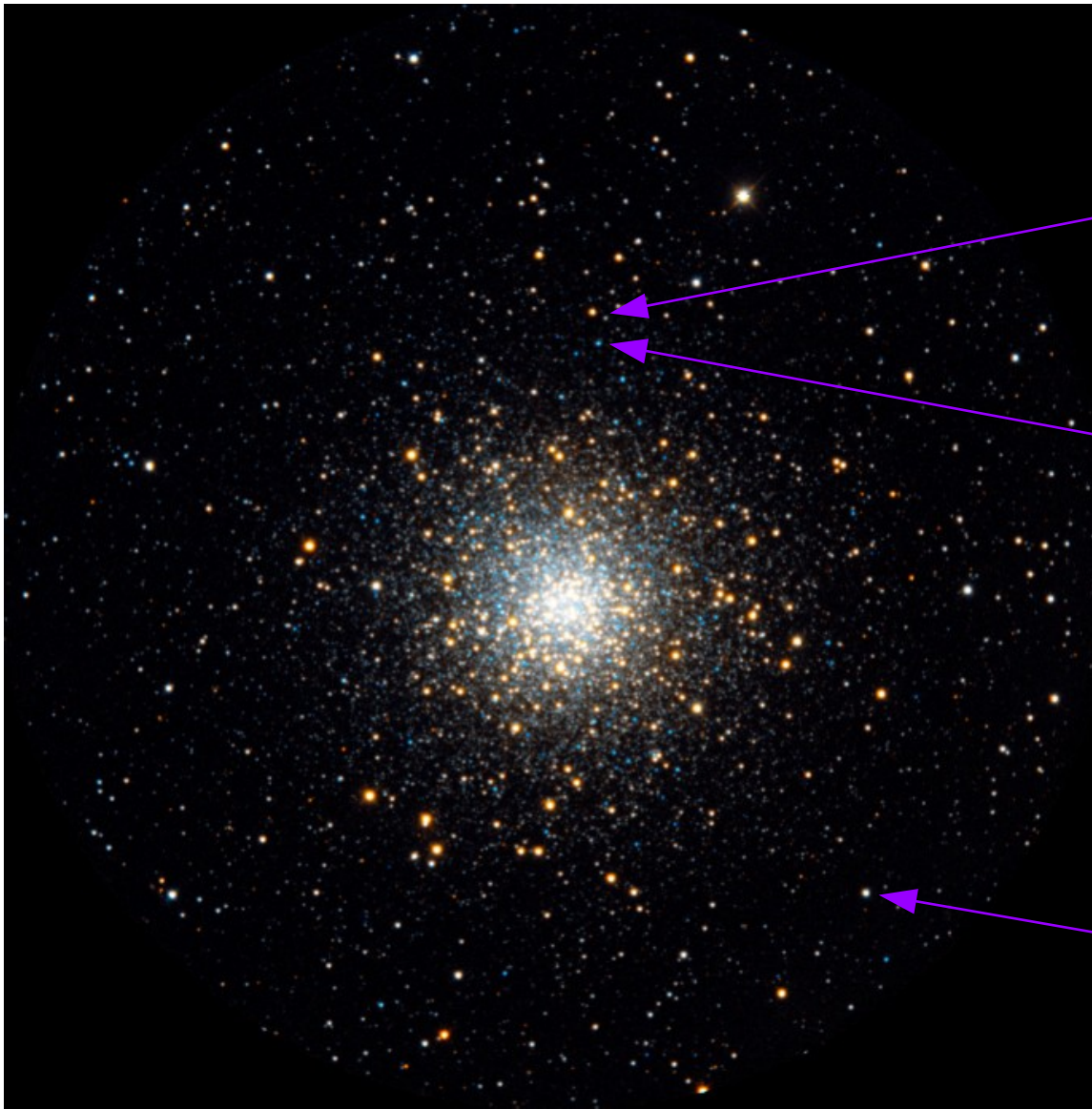
Near-infrared emission

Comparison of the measured near-infrared spectrum counterpart of the binary neutron star merger GW170817 with a “red” kilonova model



- The **two bumps** in the near infrared spectrum is a signature of **very heavy elements**
- Effect of **opacity** induced by lanthanide elements
- **Lanthanides** ($\sim 1\%$)
→ **r-process**

5. Back to the HR diagram



Globular cluster M10

Red giant star:
H \rightarrow He shell burning
via the CNO cycle

Horizontal branch star:
He \rightarrow C, O core burning
+ H \rightarrow He shell burning

Main sequence star:
H \rightarrow He core burning
via the pp chains

Red giant stars (1)

- Stars of mass $0.5 - 10 M_{\odot}$ (if $M \geq 10 M_{\odot} \rightarrow$ red supergiants)
- Inert He core (no energy source) surrounded by a H burning shell

- From the Virial theorem

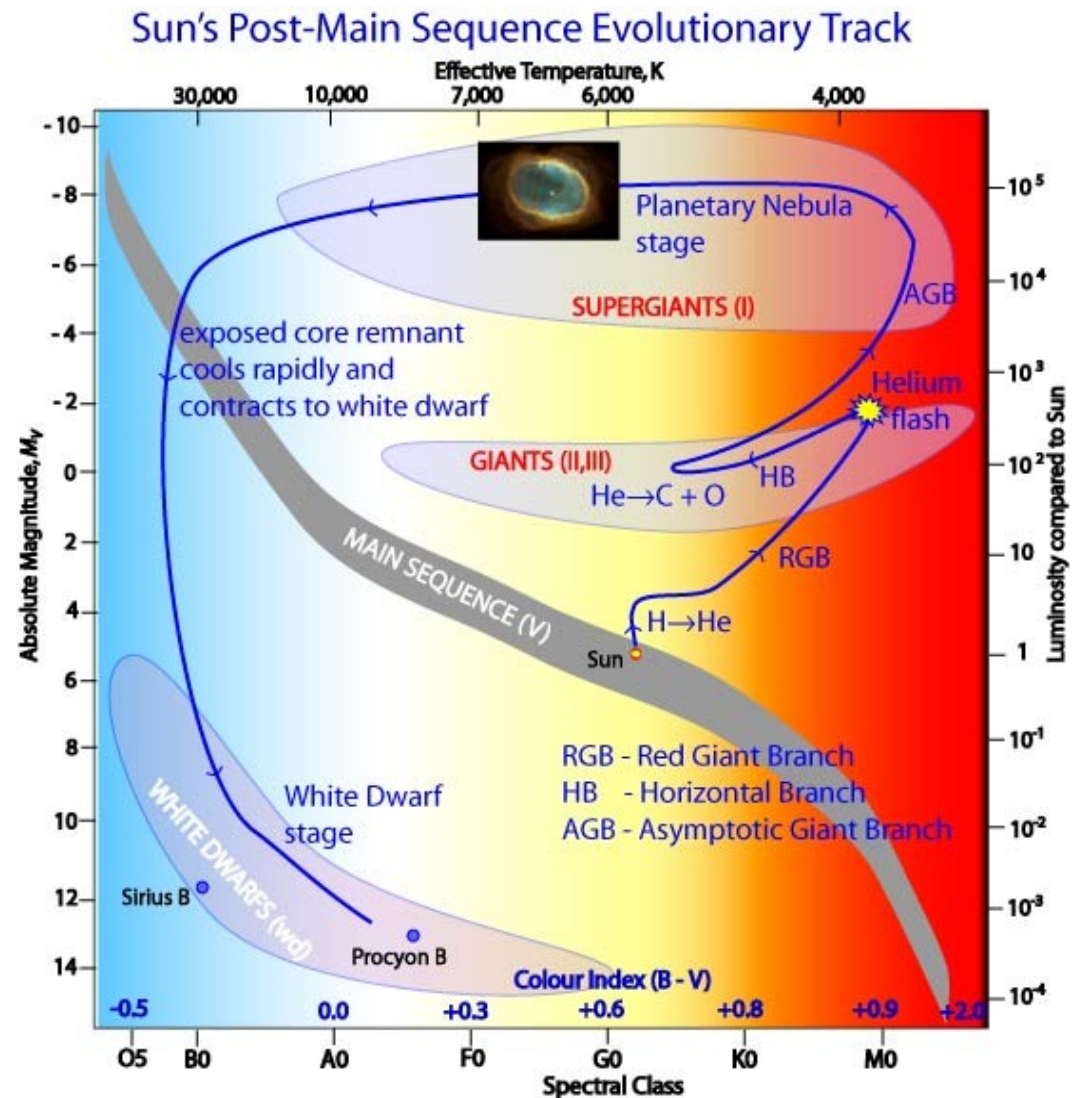
$$E = K + \Omega = \Omega/2 = -K$$

If $E \sim \text{cte}$, Ω and K also

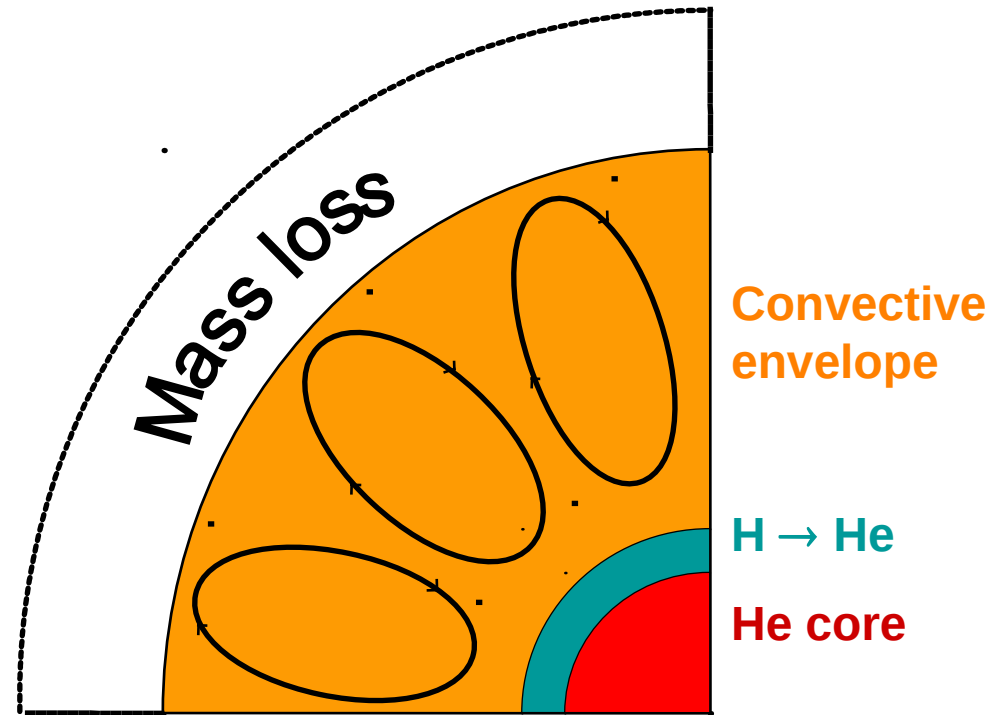
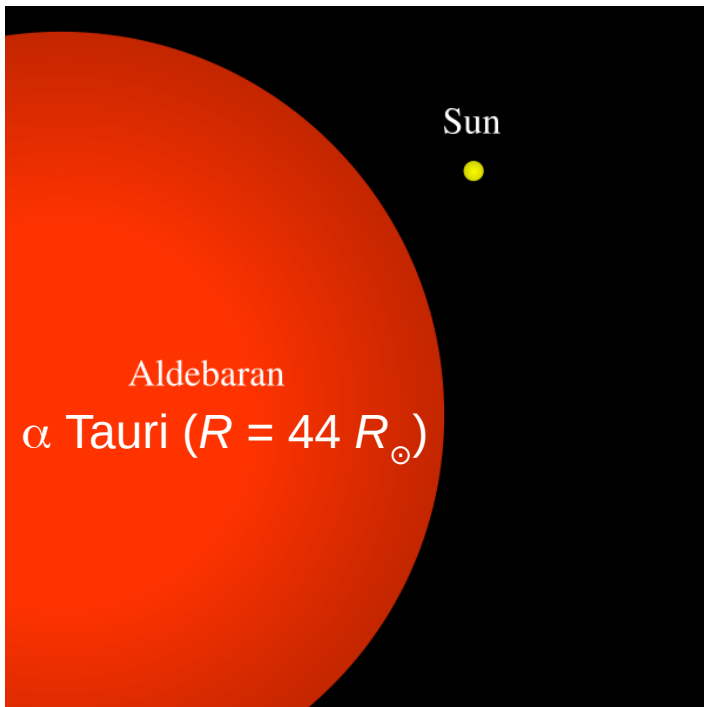
\rightarrow contraction of the core must be accompanied by expansion of the envelope ($\Omega \sim \text{cte}$) up to $50 R_{\odot}$ (\sim Mercury)

\rightarrow core heating must result in cooling of the envelope ($K \sim \text{cte}$) $\rightarrow T_{\text{eff}}$ decreases

$\rightarrow L = 4\pi R^2 \sigma_s T_{\text{eff}}^4$ increases



Red giant stars (2)



- Decrease of T_{eff} \rightarrow recombination in stellar atmosphere \rightarrow increase of opacity \rightarrow radiative transport less efficient \rightarrow convection settles in envelope
- Ashes of H-shell burning – ^{13}C , ^{14}N – are transported to the surface
 \rightarrow first “dredge-up”
 \rightarrow high $^{13}\text{C}/^{12}\text{C}$ and $^{14}\text{N}/^{12}\text{C}$ isotopic ratios observed in absorption spectra of red giant stars

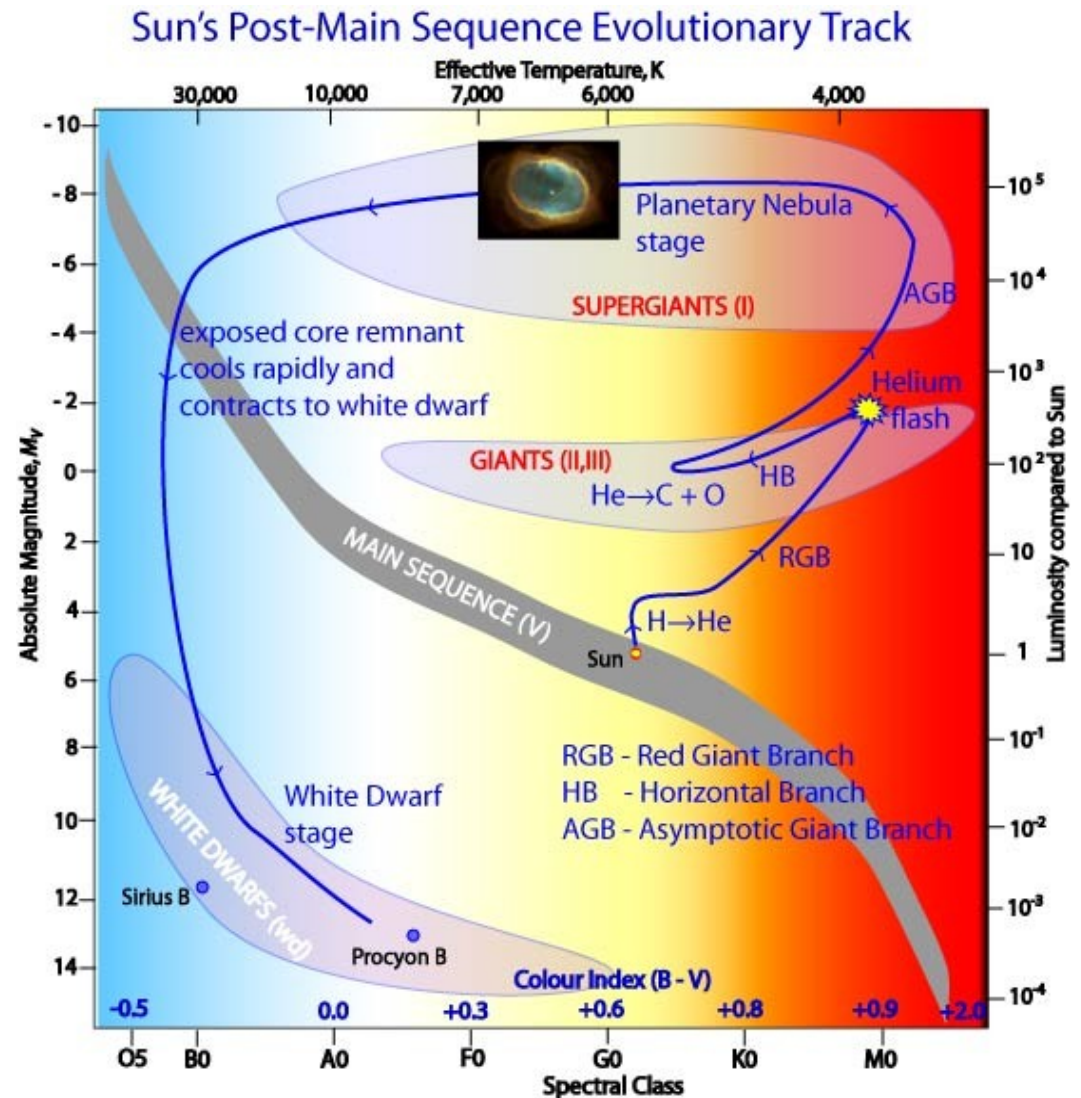
Stars of the horizontal branch (1)

Ignition of the He core at $T_c \sim 100 \text{ MK}$ → core contraction stops

- In low-mass stars ($0.7 - 2 M_\odot$) the electron gas in the core is partially degenerated → helium flash

→ release during a few seconds of $10^{10} L_\odot$ in L_{nuc} ! but invisible from the surface

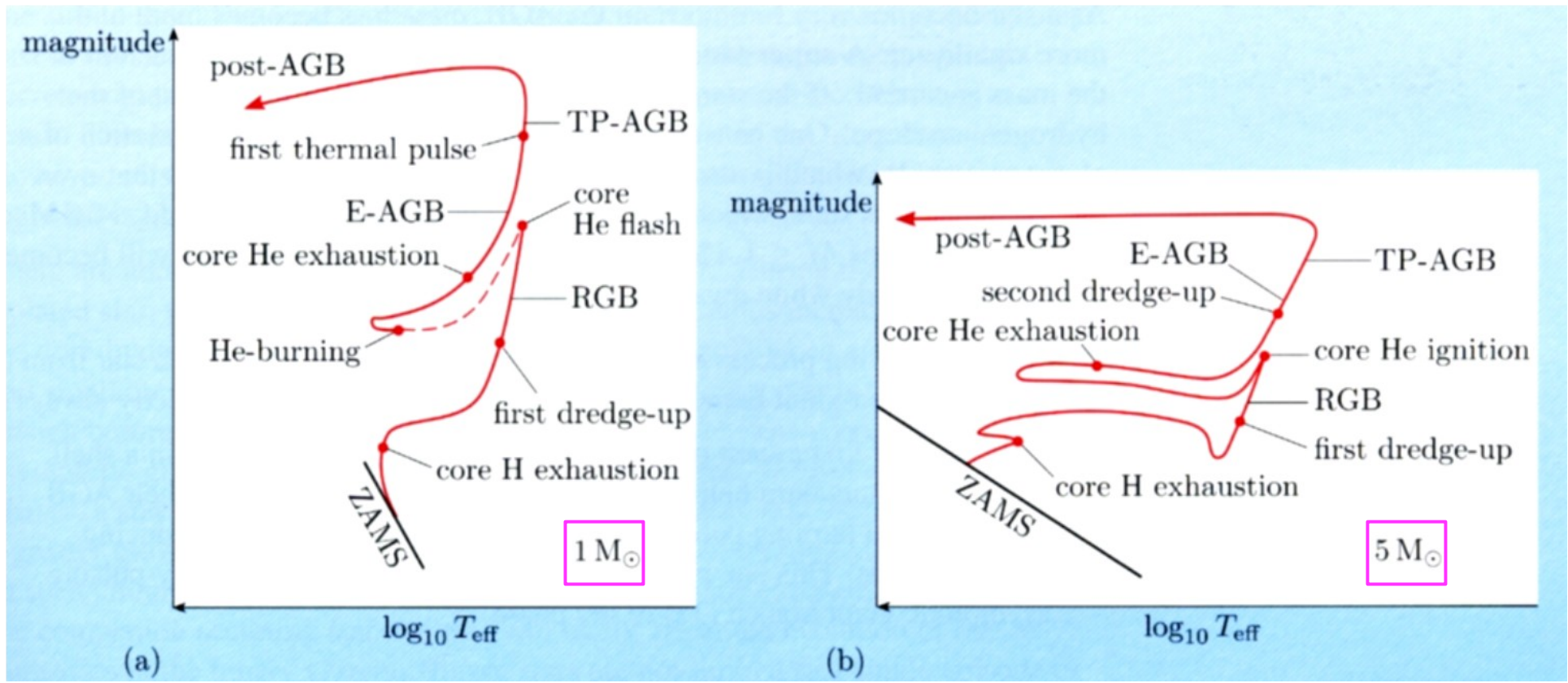
→ expansion and cooling of the core result in the contraction and heating of the envelope



Stars of the horizontal branch (2)

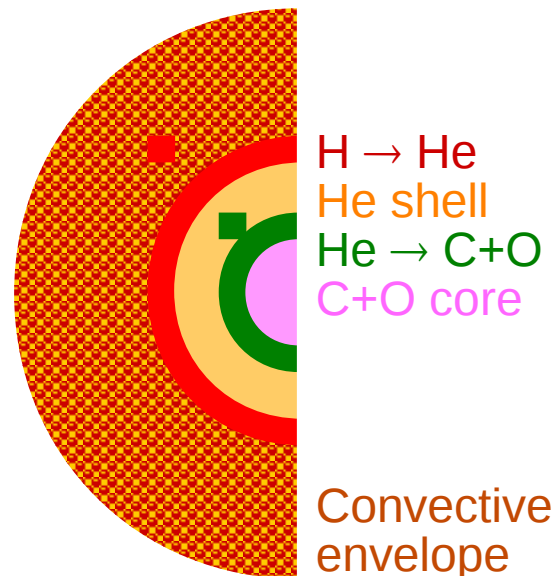
Ignition of the He core at $T_c \sim 100 \text{ MK}$ \rightarrow core contraction stops

- Quiet ignition of the He core (convective) for intermediate-mass stars ($2 - 10 M_\odot$)

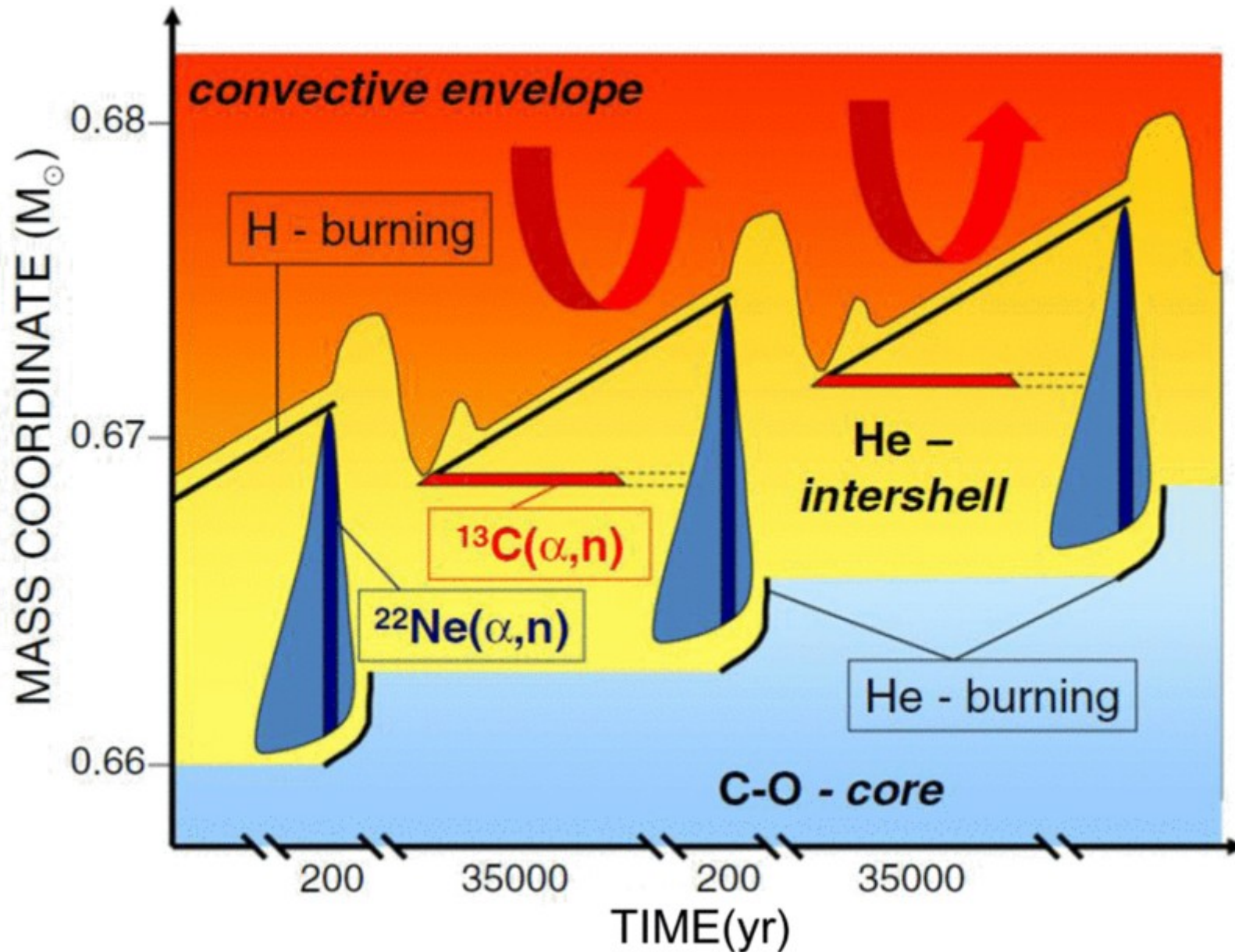


AGB stars

- **Asymptotic Giant Branch (AGB)**; E-AGB = early AGB
 - **Inert C/O core** (no energy source) left after He core burning
 - **He burning shell + H burning shell**
 - Convective envelope → **second “dredge-up”** (H-burning ashes are brought to the surface by convection)
- As for red giant phase, radius is increasing..... up to **200 R_{\odot}** (~ Earth)!



TP-AGB stars (Thermal Pulses)



- **Mixing** of ashes from H and He burning
- Site of the **main s-process**

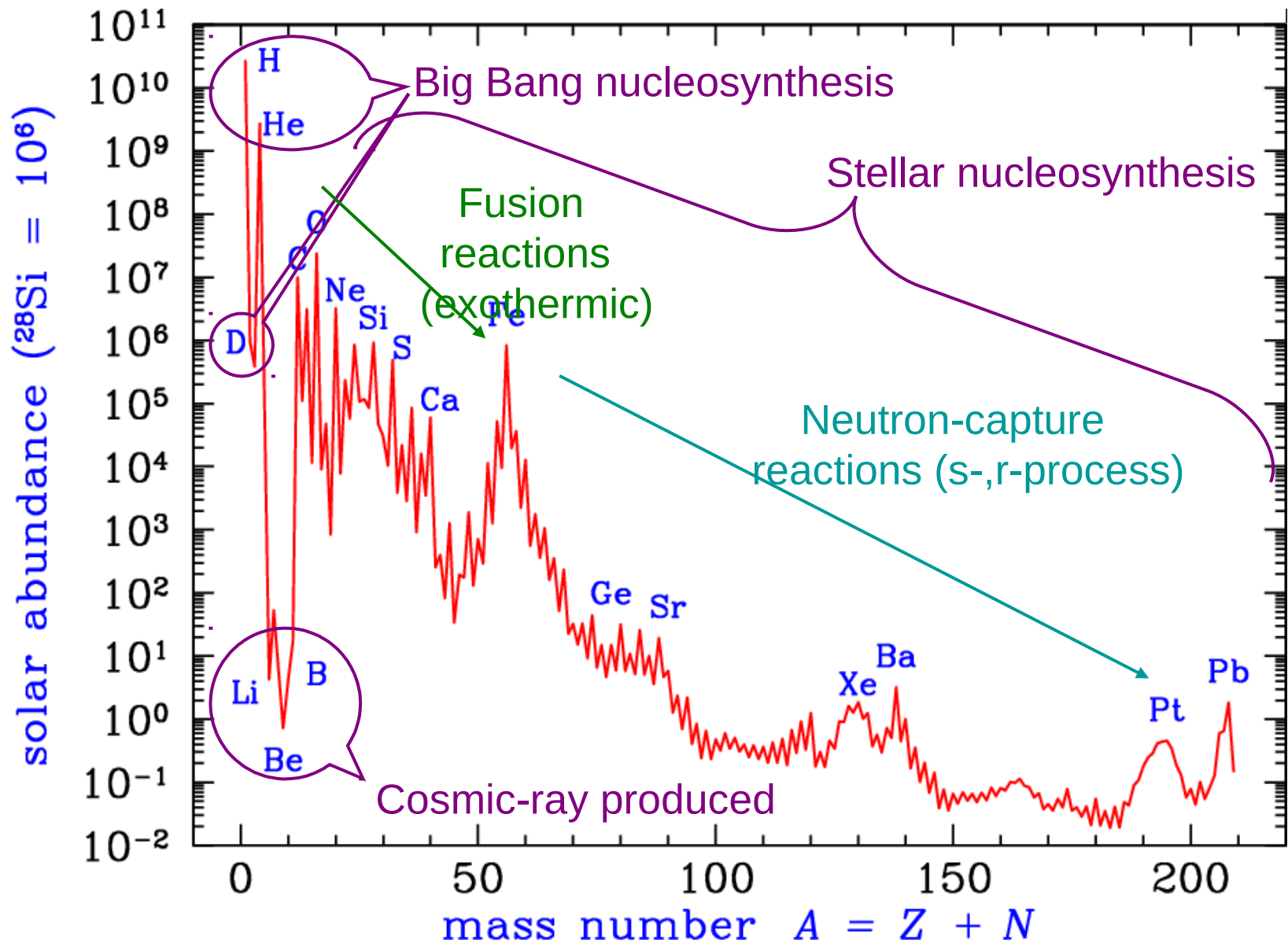
Evolution of a solar-type star

Time until the next stage (year)	T_c (MK)	T_{eff} (K)	ρ_c (g cm ⁻³)	Radius (R_\odot)	Stellar stage
10^{10}	15	6000	10^2	1	Main sequence
10^8	50	4000	10^4	3	Subgiant
10^5	100	4000	10^5	50	Helium flash
5×10^7	200	5000	10^4	10	Horizontal branch
10^4	250	4000	10^5	200	AGB
10^5	300	100 000	10^7	0.01	Compact star enriched in C, O (planetary nebula)
-	100	50 000	10^7	0.01	White dwarf

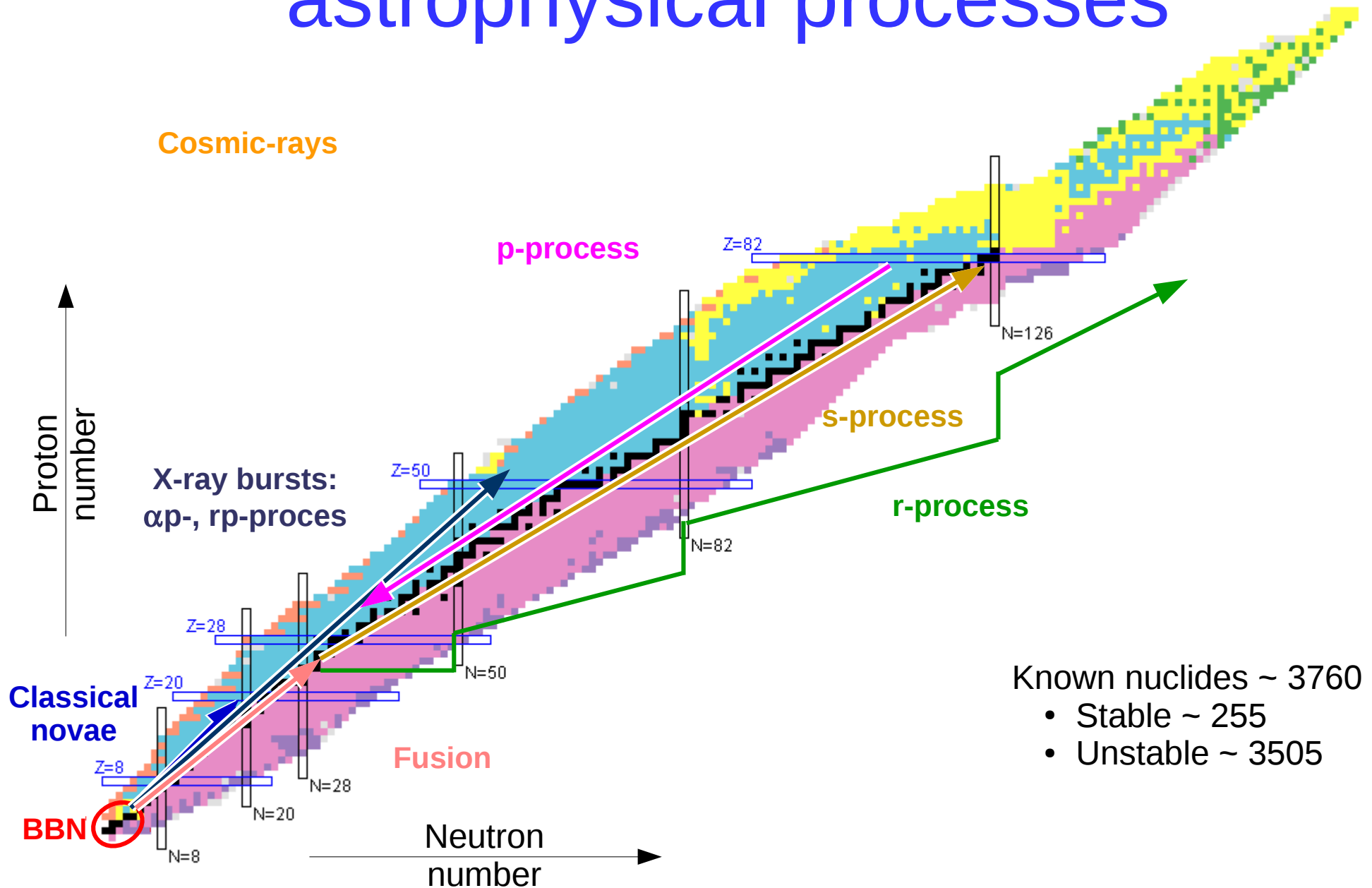


Summary

Abundance curve and processes



Nuclear landscape and astrophysical processes



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